

Calculation of Expansibility Factor of Gas at Its Flow Through an Orifice Plate With Flange Pressure Tappings

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Received: October 9, 2015. Revised: February 26, 2016. Accepted: December 26, 2016

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Abstract

The values of expansibility factor of gas were defined more accurately based on the values obtained by Seidl in CEESI using the equation of mass flowrate and on the basis of experimental data (differential pressure across the orifice plate, mass flowrate, absolute static pressure and temperature of air) for orifice plates with flange pressure tappings and diameter ratios of 0.242, 0.363, 0.484, 0.5445, 0.6655, 0.728 and pipe internal diameter of 52.48 mm (2.066 in.). When obtaining the values of expansibility factor of gas, the Stolz equation was used by Seidl to calculate the discharge coefficient for Reynolds numbers equal to infinity. New values of expansibility factor of gas are defined more accurately by us with taking into account the Reader-Harris/Gallagher equation for calculating the discharge coefficient for the actual Reynolds numbers of gas in the pipe. Based on these new more accurate data a new equation for calculating the expansibility factor of gas for orifice plate with flange pressure tappings is developed. The comparison and analysis of the expansibility factor calculated according to the equation given in ISO 5167:2-2003 and according to the new developed equation is presented in the paper. The equation in ISO 5167:2-2003 for computing the gas expansibility factor is developed for all three types of pressure tappings arrangement. In this case the scattering of discharge coefficient values being applied for deriving the expansibility factor equation is large for the same set of input data. It is shown that the shortcomings mentioned above are eliminated in the new equation and the standard deviation of the expansibility factor calculated according to the new equation from the new accurate experimental values is smaller. New formula for calculating the relative expanded uncertainty of expansibility factor for orifice plate with flange pressure tappings is also presented in the paper.

Keywords: expansibility factor; flowrate measurement; orifice plate; flange tappings.

1. Introduction

The pressure differential method with a standard primary device is the most widespread method for measurement of flowrate and volume of fluid energy carriers. One of the ways to improve the accuracy of flowrate and volume measurement is development and application of new formulae for calculating the coefficients of the flowrate equation to provide reduction of uncertainty when calculating these coefficients. The expansibility factor of gas is a part of the flowrate equation and improvement of accuracy of this factor is very important. This work deals with defining the experimental values of the expansibility factor for gas more accurately and the new equation for calculating the gas expansibility factor more accurately is developed.

2. Analysis of recent research works and publications

The first experimental research works for expansibility factor of gas were carried out in Los Angeles in 1929. Based on these works Buckingham [1] derived an equation for defining the gas expansibility factor ε_B as follows

$$\varepsilon_B = 1 - (0.41 + 0.35\beta^4) \frac{\Delta p}{p \cdot \kappa}, \quad (1)$$

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where β is diameter ratio of orifice plate; Δp is differential pressure across the orifice plate; p is absolute pressure; κ is isentropic exponent.

The equation (1) was included in the following normative documents ISO 5167–91 [2], RD 50–213–80 [3] and GOST 8.563.1–97 [4].

But the influence of Reynolds number on discharge coefficient of orifice plate was neglected by Buckingham when analyzing the experimental data. He considered that discharge coefficient for Reynolds numbers higher than $2 \cdot 10^5 \cdot \beta$ is constant. According to the recent experimental data [5]–[9] the discharge coefficient varies at $Re > 2 \cdot 10^5 \cdot \beta$. Nevertheless the general structure of this equation was the basis for other equations for calculation of gas expansibility factor.

Thibessard [10] has proposed another structure of equation for calculating the gas expansibility factor ε_T

$$\varepsilon_T = 1 - (a + b\beta^4) \left(1 - \tau^{\frac{1}{\kappa}} \right)^c, \quad (2)$$

where τ is defined according to the equation

$$\tau = 1 - \frac{\Delta p}{p}. \quad (3)$$

The value of coefficient c is equal to 0.935. This value was later taken equal to unity by Reader-Harris [11].

Experimental research works on air expansibility factor were carried out by Reid J. [12] at National Engineering Laboratory (NEL) for pipe internal diameter of 100 mm (4-inch), for three diameter ratios (0.2006; 0.57; 0.7501), for orifice plate with various types of tappings and for absolute pressure of air in the range of 140 to 800 kPa. The mass flowrate of air was set by means of reference sonic nozzle. It provided the Reynolds number of air flow which could be considered to be constant. The Reynolds number deviations were not more than 2% of the mean value of Reynolds number. During the experiments [12] the expansibility factor was defined a

$$\varepsilon_1 = \frac{(C\varepsilon_1)_g}{C_w}, \quad (4)$$

where $(C\varepsilon_1)_g$ is the measured value of product of discharge coefficient and expansibility factor of air for the same orifice plate, C_w is the orifice plate discharge coefficient calculated for water according to Stolz equation [2].

Based on the experimental data, a new formula for gas expansibility factor ε_1 was proposed by NEL [12]

$$\varepsilon_1 = 1 - a - b \cdot f \left(\frac{\Delta p}{p}, \kappa \right). \quad (5)$$

The coefficient b in equation (5) is the slope coefficient which depends on the orifice plate diameter ratio.

The experimental data for orifice plate diameter ratio of $\beta = 0.2006$ were later defined more accurately by NEL [13] and a new formula for calculating the gas expansibility factor ε_2 was derived as follows

$$\varepsilon_2 = \frac{\varepsilon_1}{1 - a} = 1 - b^* \cdot f \left(\frac{\Delta p}{p}, \kappa \right), \quad (6)$$

where b^* is the coefficient which depends on the orifice plate diameter ratio and is defined as follows

$$b^* = \frac{b}{1 - a}. \quad (7)$$

Experimental data for air expansibility factor were obtained by Seidl [14] for orifice plates with flange pressure tappings with the diameter ratios of 0.242, 0.363, 0.484, 0.5445, 0.6655 and 0.726, for pipe with the internal diameter of 52.48 mm and the absolute pressure of air in the range of 115 to 2150 kPa.

The experimental data were obtained for orifice plate installed upstream of reference sonic Venturi nozzle. The inlet pressure and temperature of air upstream of the reference sonic Venturi nozzle were regulated to maintain the constant value of mass flowrate of air and the Reynolds number. The heat exchanger was installed upstream of orifice plate to provide minimal variations of temperature and of Reynolds number correspondingly.

Since the mass flowrate of air was maintained constant, the main part of the uncertainty of flowrate measurement was caused by measurement of static pressure of air and by measurement of differential pressure across the orifice plate. The static pressure of air was measured by means of a quartz manometer of overpressure with the uncertainty of measurement of $\pm 0.012\%$. The differential pressure across the orifice plate was measured by means of two intellectual measuring transducers. The ambient temperature variations and variations of static pressure of air in the pipe were compensated by these measuring transducers. The differential pressure measuring transducers were made by two different companies and the result of differential pressure measurement was the mean value of the readings of the two measuring transducers. The uncertainty of differential pressure measurement was equal $\pm 0.1\%$. The air temperature was measured by means of a thermoelectric couple with the uncertainty of $\pm 0.1\text{ }^\circ\text{C}$.

The expansibility factor ε_s was defined by Seidl according to the following equation [14]

$$\varepsilon_s = \frac{4 \cdot q_m}{\pi \cdot C_\infty \cdot \beta^2 \cdot D^2} \cdot \sqrt{\frac{1 - \beta^4}{2 \cdot \rho_1 \cdot \Delta p}}, \quad (8)$$

where q_m is the air mass flowrate which was set by means of reference sonic Venturi nozzle, C_∞ is discharge coefficient calculated for incompressible fluid according to Stolz equation at Reynolds number equal to infinity, ρ_1 is air density upstream of the orifice plate with flange pressure tappings at absolute pressure p and thermodynamic temperature T .

Based on the equations (2) and (3), a new formula for calculating expansibility factor of gas at its flow through an orifice plate with any type of pressure tapping arrangement was derived by Reader-Harris [11]. This equation was included in ISO 5167-2:2003 [15]. The gas expansibility factor ε_{RH} for orifice plates with any type of pressure tapping arrangement according to [11] is calculated as follows

$$\varepsilon_{RH} = 1 - (0.351 + 0.256\beta^4 + 0.93\beta^8) \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{k}} \right], \quad (9)$$

Based on the analysis of the existing formulae for the calculation of expansibility factor ε and by comparing these formulae with the existing experimental data, we defined that all the formulae do not provide minimal errors and minimal systematic errors in particular due to the following factors:

- equations (1) and (9) for calculation of gas expansibility factor are derived by Buckingham [1] and Reader-Harris [11] with application of Stolz equation but not with application of the more accurate Reader-Harris/Gallagher equation [5, 6] for calculation of orifice plate discharge coefficient;
- the experimental values of gas expansibility factor were defined for orifice plate discharge coefficients C_∞ calculated for Reynolds numbers equal to infinity but not for the actual Reynolds numbers;
- equations (1) and (9) for calculation of gas expansibility factor were derived for orifice plates with any type of pressure tapping arrangement but for various types of pressure tapping arrangement the values of discharge coefficients vary considerably at the same input data which makes influence on the gas expansibility factor.

All these factors lead to overstatement of gas expansibility factors calculated according to equations (1) and (9) in comparison to the experimental data obtained by Seidl [14] for gas flow through an orifice plate with flange pressure tappings. The calculated results of gas expansibility factors according to equations (1) and (9) include a systematic component error which is not desirable for calculation of gas flowrate and volume.

The objective of this work is to define the experimental values of gas expansibility factor more accurately based on the experiments carried out by Seidl [14] and to develop a new equation for calculation of expansibility factor of gas at its flow through an orifice plate with flange pressure tappings in order to provide higher accuracy of flowrate calculation.

3. Correction of experimental data

Let's recalculate the experimental values of expansibility factor ε_S of air obtained by Seidl [14], using Reader-Harris/Gallagher equation [15] for discharge coefficient C_{RH} for orifice plates with flange pressure tappings according to the following equation

$$\varepsilon_{Ne} = \varepsilon_S \frac{C_\infty}{C_{RH}}. \quad (10)$$

The value of discharge coefficient C_∞ for an orifice plate with flange pressure tappings was calculated according to Stolz equation [2] for Reynolds number equal to infinity as follows

$$C_\infty = 0.5959 + 0.0312\beta^{2.1} - 0.184\beta^8 + 0.09L_1 \frac{\beta^4}{1-\beta^4} - 0.0337 \cdot L_2\beta^3, \quad (11)$$

where L_1 and L_2 for orifice plates with flange pressure tappings are calculated in the following way

$$L_1 = \begin{cases} 0.4333 & \text{for } D \leq 0.05862 \text{ m;} \\ \frac{0.0254}{D} & \text{for } D > 0.05862 \text{ m;} \end{cases} \quad (12)$$

$$L_2 = \frac{0.0254}{D}. \quad (13)$$

The value of discharge coefficient C_{RH} for an orifice plate with flange pressure tappings was calculated according to Reader-Harris/Gallagher equation [15] for the actual Reynolds numbers as follows

$$\begin{aligned} C_{RH} = & 0.5961 + 0.0261\beta^2 - 0.216\beta^8 + \\ & + 0.000521 \left(\frac{10^6 \beta}{Re} \right)^{0.7} + (0.0188 + 0.0063A)\beta^{3.5} \left(\frac{10^6}{Re} \right)^{0.3} + \\ & + (0.043 + 0.08e^{-10L_1} - 0.123e^{-7L_1})(1 - 0.11A) \frac{\beta^4}{1-\beta^4} - \\ & - 0.031(M'_2 - 0.8 \cdot M_2'^{1.1})\beta^{1.3} + M_3, \end{aligned} \quad (14)$$

where

$$\begin{aligned} A = & \left(\frac{19000\beta}{Re} \right)^{0.8}; \quad L_1 = L_2 = \frac{0.0254}{D}; \quad M'_2 = \frac{2L_2}{1-\beta}; \\ M_3 = & \begin{cases} 0 & \text{for } D \geq 0.07112 \text{ m;} \\ 0.011(0.75 - \beta) \left(2.8 - \frac{D}{0.0254} \right) & \text{for } D < 0.07112 \text{ m.} \end{cases} \end{aligned}$$

The experimental values of air expansibility factor ε_S [14] and the new corrected values of air expansibility factor ε_{Ne} calculated according to equation (10) are presented in Table 1.

Table 1. Experimental values and corrected values of air expansibility factor

#	$\beta=0.2420; C_{\infty}=0.59739$			$\beta=0.3630; C_{\infty}=0.59947$			$\beta=0.4840; C_{\infty}=0.60256$		
	ϵ_S	C_{RH}	ϵ_{Ne}	ϵ_S	C_{RH}	ϵ_{Ne}	ϵ_S	C_{RH}	ϵ_{Ne}
1	0.99901	0.60243	0.99065	0.99518	0.60347	0.98857	0.99790	0.60609	0.99209
2	0.99838	0.60242	0.99004	0.99711	0.60347	0.99051	0.99784	0.60608	0.99204
3	0.99757	0.60242	0.98924	0.99887	0.60346	0.99226	0.99772	0.60608	0.99192
4	0.99819	0.60242	0.98985	1.00094	0.60346	0.99432	0.99733	0.60609	0.99152
5	0.99624	0.60241	0.98793	0.99785	0.60345	0.99127	0.99603	0.60608	0.99024
6	0.99299	0.60241	0.98471	0.99561	0.60345	0.98904	0.99299	0.60608	0.98722
7	0.98825	0.60241	0.98001	0.99065	0.60345	0.98412	0.98655	0.60608	0.98081
8	0.97587	0.60241	0.96774	0.98438	0.60344	0.97789	0.98100	0.60608	0.97529
9	0.98860	0.60241	0.98036	0.99130	0.60344	0.98477	0.98655	0.60608	0.98081
10	0.96597	0.60241	0.95792	0.97277	0.60344	0.96636	0.96903	0.60609	0.96339
11	0.94320	0.60240	0.93535	0.96224	0.60344	0.95590	0.95927	0.60609	0.95369
12	0.93030	0.60240	0.92255	0.94871	0.60344	0.94247	0.94593	0.60608	0.94043
13	0.94270	0.60240	0.93485	0.90880	0.60344	0.90282	0.92543	0.60608	0.92005
14	-	-	-	0.94960	0.60343	0.94336	0.94530	0.60608	0.93981
#	$\beta=0.5445; C_{\infty}=0.60431$			$\beta=0.6655; C_{\infty}=0.60680$			$\beta=0.7260; C_{\infty}=0.60639$		
1	0.99911	0.60791	0.99320	0.99916	0.61212	0.99046	0.99767	0.61078	0.99050
2	0.99800	0.60790	0.99210	0.99859	0.61211	0.98992	1.00264	0.61077	0.99545
3	0.99672	0.60789	0.99084	1.00057	0.61210	0.99190	0.99970	0.61076	0.99254
4	0.99840	0.60790	0.99250	0.99797	0.61211	0.98931	1.00231	0.61077	0.99511
5	0.99484	0.60789	0.98898	0.99774	0.61209	0.98910	0.99776	0.61076	0.99061
6	0.99226	0.60788	0.98642	0.99494	0.61209	0.98634	0.99536	0.61076	0.98823
7	0.98612	0.60788	0.98032	0.99287	0.61209	0.98429	0.98578	0.61076	0.97872
8	0.98066	0.60788	0.97490	0.98846	0.61208	0.97992	0.98001	0.61076	0.97300
9	0.98624	0.60788	0.98045	0.98079	0.61208	0.97233	0.97015	0.61075	0.96321
10	0.96970	0.60788	0.96400	0.98872	0.61208	0.98019	0.97985	0.61075	0.97284
11	0.95974	0.60788	0.95410	0.97350	0.61207	0.96511	0.96330	0.61075	0.95642
12	0.94191	0.60788	0.93637	0.96539	0.61207	0.95708	0.94452	0.61075	0.93777
13	0.91182	0.60788	0.90646	0.94795	0.61206	0.93979	0.90999	0.61074	0.90350
14	0.94230	0.60788	0.93677	0.92258	0.61206	0.91465	0.94428	0.61074	0.93755
15	-	-	-	0.94822	0.61206	0.94007	-	-	-

4. Development of a new equation

The most important thing when developing a new equation for gas expansibility factor is to define the structure of the equation. On the basis of the research carried out by us, we defined that the most accurate equation to fit the corrected values of air expansibility factor is

$$\epsilon_N = 1 - a_N - b_N \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right]. \tag{15}$$

Based on the experimental values of gas expansibility factor the values of a_S and b_S coefficients (they correspond to a and b coefficients in equation (5)) were derived by Seidl and the values of these coefficients are presented in Table 2. Using the least-squares method we have obtained the values of a_N and b_N coefficients to fit the corrected values of gas expansibility factor (see Table 1) and the values of these coefficients are also presented in Table 2.

As we can see from Table 2, application of discharge coefficient C_{∞} calculated according to Stolz equation when defining the gas expansibility factor according to the experimental data [14] leads to the value of a_S coefficient approaching zero. That is why a_S coefficient can be neglected at development of equation for gas expansibility factor.

Table 2. Values of a_S and b_S coefficients according to the experimental data of Seidl [14] and values of a_N and b_N coefficients according to the corrected experimental data

#	β	Experimental data ε_S		Corrected experimental data ε_N	
		a_S	b_S	a_N	b_N
1	0.2420	$-1.5610 \cdot 10^{-8}$	0.3791	0.0085552	0.362105
2	0.3630	$-2.1536 \cdot 10^{-3}$	0.3577	0.0048254	0.338649
3	0.4840	$1.3816 \cdot 10^{-6}$	0.3834	0.0060568	0.367367
4	0.5445	$5.9339 \cdot 10^{-6}$	0.4025	0.0062141	0.383636
5	0.6655	$-1.1408 \cdot 10^{-4}$	0.4407	0.0087519	0.422299
6	0.7260	$2.5120 \cdot 10^{-6}$	0.5309	0.0074610	0.509042

If we apply discharge coefficient C_{RH} calculated according to Reader-Harris/Gallagher equation when defining the gas expansibility factor according to the corrected experimental data, the value of a_N coefficient in equation (15) does not approach zero (see Table 2). That is why a_N coefficient cannot be neglected at development of equation for gas expansibility factor.

Let's obtain the formulae for calculation of a_N and b_N coefficients defined for the corrected experimental values of gas expansibility factor.

Since a_N coefficient is constant and it does not depend on the diameter ratio of orifice plate, it can be defined as mean value of the values given in Table 2 for the corrected experimental data of expansibility factor ε_{Ne} of air and its value $a_N = 0.006977$.

Coefficient b_N with its values given in Table 2 is a function of diameter ratio β of orifice plate.

Using the least-squares method and the new value of $a_N = 0.006977$ the values of b_N coefficient shall be corrected. The corrected values of b_N coefficient are given in Table 3.

Based on the research we defined that the most accurate equation for b_N coefficient is the following equation [11]

$$b_N = a_b + b_b \beta^4 + c_b \beta^8. \quad (16)$$

Table 3. Corrected values of b_N coefficient

#	β	b_N
1	0.2420	0.374214
2	0.3630	0.324496
3	0.4840	0.360038
4	0.5445	0.378002
5	0.6655	0.438676
6	0.7260	0.513676

Using the least-squares method the values of a_b , b_b , c_b coefficients shall be as follows: $a_b = 0.3507$; $b_b = 0.0849$; $c_b = 1.8195$.

After substituting the values of a_b , b_b , c_b coefficients in equation (16) we obtain the equation for b_N coefficient

$$b_N = 0.3507 + 0.0849 \cdot \beta^4 + 1.8195 \cdot \beta^8. \quad (17)$$

The absolute standard deviation σ_b of values of b_N coefficient calculated according to equation (17) from the values of b_N coefficient given in Table 2 (reassigned as b_{NTi}) for the corrected experimental data shall be calculated as follows

$$\sigma_b = \sqrt{\frac{\sum_{i=1}^n (b_{Ni} - b_{NTi})^2}{n-1}} = 0.0123. \quad (18)$$

where n is the number of values of b_N coefficient ($n=6$).

Table 4. Relative deviations $\delta\epsilon_{RH}$ and $\delta\epsilon_N$ between the corrected experimental values and the values of expansibility factor calculated according to equations (9) and (19) correspondingly.

$\Delta p/p$	ϵ_{Ne}	ϵ_{RH}	$\delta\epsilon_{RH}$ (%)	ϵ_N	$\delta\epsilon_N$ (%)	$\Delta p/p$	ϵ_{Ne}	ϵ_{RH}	$\delta\epsilon_{RH}$ (%)	ϵ_N	$\delta\epsilon_N$ (%)
$\beta=0.2420$						$\beta=0.3630$					
0.00336	0.99065	0.99917	0.86	0.99220	0.16	0.00298	0.98857	0.99926	1.08	0.99229	0.38
0.00471	0.99004	0.99884	0.89	0.99186	0.18	0.00459	0.99051	0.99885	0.84	0.99188	0.14
0.00730	0.98924	0.99819	0.90	0.99122	0.20	0.00791	0.99226	0.99801	0.58	0.99105	-0.12
0.00473	0.98985	0.99883	0.91	0.99186	0.20	0.00460	0.99432	0.99885	0.46	0.99188	-0.25
0.01265	0.98793	0.99685	0.90	0.98988	0.20	0.01665	0.99127	0.99579	0.46	0.98885	-0.24
0.02662	0.98471	0.99333	0.88	0.98637	0.17	0.02800	0.98904	0.99290	0.39	0.98598	-0.31
0.04484	0.98001	0.98872	0.89	0.98177	0.18	0.05567	0.98412	0.98580	0.17	0.97894	-0.53
0.09087	0.96774	0.97694	0.95	0.97002	0.24	0.08013	0.97789	0.97947	0.16	0.97267	-0.53
0.04484	0.98036	0.98872	0.85	0.98177	0.14	0.05574	0.98477	0.98578	0.10	0.97892	-0.59
0.13072	0.95792	0.96660	0.91	0.95971	0.19	0.12559	0.96636	0.96757	0.13	0.96087	-0.57
0.21125	0.93535	0.94528	1.06	0.93844	0.33	0.16510	0.95590	0.95708	0.12	0.95047	-0.57
0.25412	0.92255	0.93367	1.21	0.92685	0.47	0.21325	0.94247	0.94411	0.17	0.93760	-0.52
0.21195	0.93485	0.94509	1.10	0.93825	0.36	0.34600	0.90282	0.90708	0.47	0.90088	-0.21
-	-	-	-	-	-	0.21323	0.94336	0.94411	0.08	0.93761	-0.61
$\beta=0.4840$						$\beta=0.5445$					
0.00290	0.99209	0.99925	0.72	0.99229	0.02	0.00269	0.99320	0.99928	0.61	0.99232	-0.09
0.00445	0.99204	0.99885	0.69	0.99189	-0.02	0.00416	0.99210	0.99889	0.68	0.99193	-0.02
0.00762	0.99192	0.99802	0.61	0.99108	-0.08	0.00717	0.99084	0.99807	0.73	0.99113	0.03
0.00442	0.99152	0.99885	0.74	0.99190	0.04	0.00416	0.99250	0.99888	0.64	0.99193	-0.06
0.01593	0.99024	0.99584	0.57	0.98894	-0.13	0.01511	0.98898	0.99591	0.70	0.98903	0.01
0.02646	0.98722	0.99306	0.59	0.98622	-0.10	0.02516	0.98642	0.99317	0.68	0.98635	-0.01
0.05252	0.98081	0.98615	0.54	0.97944	-0.14	0.05002	0.98032	0.98636	0.62	0.97968	-0.07
0.07516	0.97529	0.98010	0.49	0.97350	-0.18	0.07174	0.97490	0.98035	0.56	0.97381	-0.11
0.05224	0.98081	0.98623	0.55	0.97951	-0.13	0.05006	0.98045	0.98634	0.60	0.97967	-0.08
0.11703	0.96339	0.96879	0.56	0.96241	-0.10	0.11213	0.96400	0.96908	0.53	0.96279	-0.13
0.15339	0.95369	0.95885	0.54	0.95266	-0.11	0.14651	0.95410	0.95937	0.55	0.95329	-0.08
0.19803	0.94043	0.94647	0.64	0.94051	0.01	0.20188	0.93637	0.94348	0.76	0.93776	0.15
0.26719	0.92005	0.92688	0.74	0.92130	0.14	0.30080	0.90646	0.91428	0.86	0.90921	0.30
0.19847	0.93981	0.94634	0.69	0.94039	0.06	0.20172	0.93677	0.94353	0.72	0.93781	0.11
$\beta=0.6655$						$\beta=0.7260$					
0.00136	0.99046	0.99958	0.92	0.99260	0.22	0.00176	0.99050	0.99939	0.90	0.99239	0.19
0.00235	0.98992	0.99927	0.94	0.99230	0.24	0.00267	0.99545	0.99907	0.36	0.99206	-0.34
0.00491	0.99190	0.99848	0.66	0.99150	-0.04	0.00460	0.99254	0.99839	0.59	0.99135	-0.12
0.00236	0.98931	0.99927	1.01	0.99229	0.30	0.00266	0.99511	0.99908	0.40	0.99206	-0.31
0.00818	0.98910	0.99746	0.85	0.99048	0.14	0.00964	0.99061	0.99662	0.61	0.98950	-0.11
0.01616	0.98634	0.99496	0.87	0.98798	0.17	0.01600	0.98823	0.99438	0.62	0.98716	-0.11
0.02301	0.98429	0.99282	0.87	0.98584	0.16	0.03201	0.97872	0.98870	1.02	0.98125	0.26
0.03548	0.97992	0.98890	0.92	0.98191	0.20	0.04593	0.97300	0.98375	1.10	0.97608	0.32
0.06175	0.97233	0.98059	0.85	0.97360	0.13	0.07155	0.96321	0.97457	1.18	0.96652	0.34
0.03555	0.98019	0.98888	0.89	0.98189	0.17	0.04593	0.97284	0.98374	1.12	0.97608	0.33
0.08779	0.96511	0.97229	0.74	0.96529	0.02	0.09319	0.95642	0.96675	1.08	0.95837	0.20
0.11261	0.95708	0.96431	0.76	0.95731	0.02	0.14652	0.93777	0.94726	1.01	0.93806	0.03
0.16720	0.93979	0.94654	0.72	0.93952	-0.03	0.24465	0.90350	0.91045	0.77	0.89970	-0.42
0.24252	0.91465	0.92145	0.74	0.91441	-0.03	0.14652	0.93755	0.94726	1.04	0.93806	0.05
0.16715	0.94007	0.94655	0.69	0.93953	-0.06	-	-	-	-	-	-

The values of $\delta\epsilon_{RH}$ and $\delta\epsilon_N$ were calculated as follows $\delta\epsilon_{RH} = 100 \cdot (\epsilon_{RH} - \epsilon_{Ne}) / \epsilon_{Ne}$ and $\delta\epsilon_N = 100 \cdot (\epsilon_N - \epsilon_{Ne}) / \epsilon_{Ne}$.

By substituting the equation (17) and the new value of a_N coefficient in equation (15) we obtain a new equation for calculation of gas expansibility factor for orifice plate with flange pressure tappings

$$\varepsilon_N = 0.993023 - (0.3507 + 0.0849\beta^4 + 1.8195\beta^8) \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right]. \quad (19)$$

The relative deviation $\delta\varepsilon_N$ of the corrected experimental values and the values of expansibility factor calculated according to equation (19) are given in Table 4. As we can see from Table 4, maximum relative deviation $\delta\varepsilon_N$ is 0.61 % which is twice as little as maximum relative deviation $\delta\varepsilon_{RH}$ of values of expansibility factor calculated according to the known equation (9) which is equal 1.21 %. By the way the average of distribution of the relative deviation in the presented set of data is equal to -0.004 % for the new equation instead of 0.71 % for the known equation.

When β , $\Delta p/p$ and κ are assumed to be known without error, the expanded uncertainty of expansibility factor ε_N calculated according to equation (19) relative to the corrected experimental values of expansibility factor ε_{Ne} shall be defined as follows

$$\begin{aligned} \varepsilon_N - \varepsilon_{Ne} &= \\ &= -(0.3507 + 0.0849\beta^4 + 1.8195\beta^8 - b_{NT}) \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right] = \\ &= -2\sigma_b \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right] = -0.0246 \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right]. \end{aligned} \quad (20)$$

In percentage terms the relative expanded uncertainty of calculation of expansibility factor is defined as follows

$$\frac{2.46 \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right]}{0.993023 - (0.3507 + 0.0849\beta^4 + 1.8195\beta^8) \left[1 - \left(1 - \frac{\Delta p}{p} \right)^{\frac{1}{\kappa}} \right]}. \quad (21)$$

After decomposing the term $[1 - (1 - \Delta p/p)^{1/\kappa}]$ in the numerator of equation (21) into Maclaurin series for the value of $\Delta p/p$ and after taking its first term $\Delta p/(\kappa \cdot p)$, for $\beta=0.75$, $\Delta p/p=0.25$ and $\kappa=1$ in the denominator of equation (21) when the value of the uncertainty is maximal, we obtain a new formula for the relative expanded uncertainty of expansibility factor

$$2.88 \cdot \frac{\Delta p}{\kappa \cdot p}. \quad (22)$$

As it was expected, formula (22) in comparison to the known analogous formula in [15] gives smaller values of the relative expanded uncertainty of expansibility factor for equal input values.

5. Conclusions

It is shown that during experimental research works on gas expansibility factor a number of coefficients of flowrate equation, and discharge coefficient in particular, are used to define the values of expansibility factor and inaccuracy of these coefficients makes influence on the uncertainty of expansibility factor.

It is defined that the formulae in force at present for gas expansibility factor include a systematic component error caused by the following factors:

- the known formulae for expansibility factor are derived with application of Stolz equation for calculation of orifice plate discharge coefficient and a larger value of uncertainty is assigned to this equation in comparison to Reader-Harris/Gallagher equation;
- the experimental values of expansibility factor were defined according to the values of orifice plate discharge coefficient calculated not for the actual Reynolds numbers but for Reynolds numbers equal to infinity.

By taking into account the actual values of orifice plate discharge coefficient, the experimental data for gas expansibility factor are defined more accurately for orifice plates with flange pressure tapings.

New equation for gas expansibility factor for orifice plates with flange pressure tapings is developed and it provides higher accuracy according to the existing experimental data. The average distribution of the relative deviation and the maximal relative deviation for the existing set of experimental data are -0.004 % and 0.61 % correspondingly for the new developed equation instead of 0.71 % and 1.21 % correspondingly for the known formula.

New equation for relative expanded uncertainty of expansibility factor is developed with taking into account the influencing parameters of fluid and flow. The new equation provides decrease of relative expanded uncertainty of expansibility factor.

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Розрахунок коефіцієнта розширення газу під час його протікання через діафрагму з фланцевим відбором тиску

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Анотація

Наведено уточнені значення коефіцієнта розширення газу на основі значень, що їх отримав Давид Зейдль у Колорадському інженерно-експериментальному центрі (CEESI) із застосуванням рівняння масової витрати газу для діафрагми з фланцевим способом відбору тиску, і значень відносного діаметра отвору діафрагми від 0,242 до 0,728 для значення внутрішнього діаметра трубопроводу 52,48 мм (2,066 дюйма). Під час отримання значень коефіцієнта розширення Зейдль застосував рівняння коефіцієнта витікання Штольца для значення числа Рейнольдса рівного нескінченності. Автори уточнили значення коефіцієнта розширення газу, застосовуючи нове рівняння коефіцієнта витікання Рідера-Харіса/Галахера для реальних значень числа Рейнольдса. На базі уточнених значень коефіцієнта розширення газу автори розробили нове рівняння для його розрахунку, що зменшило максимальне відхилення значення коефіцієнта розширення газу відносно рівняння, яке застосовується в ISO 5167-2:2003. Автори також розробили нове рівняння для розрахунку відносної розширеної невизначеності коефіцієнта розширення повітря, яке також наведено у статті.

Ключові слова: коефіцієнт розширення; вимірювання витрати; діафрагма; фланцевий спосіб відбору тиску; невизначеність коефіцієнта розширення.