Structure and morphology peculiarities of $Bi_{24}(Si,M)_2O_{40}$ (*M* = Mn, V) with sillenite structure

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Single crystals in the form of cubes, tetrahedra or combinations of cubes and tetrahedra with sillenite structure in the Bi_2O_3 -SiO₂-MnO₂ system, as well as bulk crystals ($Bi_{24}Ge_2O_{40}$ used as a seed crystal) in the Bi_2O_3 -SiO_2-V_2O_5 system, have been grown by the hydrothermal method. The results of the crystal chemical analysis by X-ray diffraction, together with the formal charges of the cations calculated by the bond-valence method, allowed establishing the formation of phases of the general compositions Bi₂₄(Si,Mn)₂O₄₀ and Bi³⁺, Mn^{4+} Si⁴⁺, Bi₂₄(Si,Bi,Mn)₂O₄₀ with and ions, and Bi24(Si,Bi,V)2O40 with and V⁵⁺ $Bi_{24}(Si^{4+}_{0.58}Bi^{3+}_{0.02}Mn^{4+}_{1.4})(O_{39,99}\square_{0.01})$, which adopt space group *I*23. The lower symmetry can be explained by a kinetic phase transition of order-disorder type associated with peculiarities of the structure (different atoms in the same crystallographic site) and growth conditions. The crystals with a combination of cubes and tetrahedra (initial charge Na₂SiO₃·9H₂O : $Mn(NO_3)_2$ ·6H₂O = 1:1) have space group I23, whereas the crystals with cube $(Na_2SiO_3 \cdot 9H_2O : Mn(NO_3)_2 \cdot 6H_2O > 1)$ or tetrahedron $(Na_2SiO_3 \cdot 9H_2O : Mn(NO_3)_2 \cdot 6H_2O < 1)$ habit crystallize in space groups I23 and P23.

Sillenites / Composition / Crystal structure

Introduction

The members of the sillenite family, nowadays known as the phases $Bi_{24}M_2O_{40\pm\delta}$ and solid solutions $Bi_{24}(M'_{x}M''_{1-x})_{2}O_{40\pm\delta}$ (where M,M',M'' are cations with different formal charges in tetrahedral coordination), crystallize in space group I23 (Z = 1) [1,2] (Fig. 1a). materials are of interest These due to photoconductivity, piezo- and electrooptical effects and photorefractive properties. The physical properties depend on the cations in the tetrahedral site and their formal charge (FC).

The presence in tetrahedral sites of cations with different crystal chemical properties (dimension, electronegativity, cation FC) can lead to a kinetic phase transition of order-disorder type [3]. The ordering depends on structure peculiarities, properties of the components, and the method and conditions of preparation of the samples. There exists according to

our knowledge no information about similar phenomena for sillenites.

The aim of this paper was to determine the composition and structure of sillenites in the Bi_2O_3 -SiO_2-MnO_2 and Bi_2O_3 -SiO_2-V₂O₅ systems. Structure refinements have been reported for some compositions in these systems: $Bi_{24}Si_{1.99}Mn_{0.01}O_{40}$ (*a* = 10.109(1) Å) [4], $Bi_{24}Si_2O_{40}$ (*a* = 10.10433(5) Å) [5], $Bi_{24}Mn_2O_{40}$ (*a* = 10.206(1) Å) [6], $Bi_{24}(V^{5+}_{1.78}Bi^{3+}_{0.06}\square_{0.16})O_{40.54}$ (*a* = 10.247(8) Å) [2], and $Bi^{3+}_{24}[(V^{5+}O_4)(Bi^{3+}O_4)]O_{32}$ (*a* = 10.222(4) Å) [7].

Experimental

All the crystals the Bi₂O₃-SiO₂-MnO₂ in and Bi₂O₃-SiO₂-V₂O₅ were systems grown hydrothermal synthesis by with initial charge compositions NaBiO₃ + Na₂SiO₃·9H₂O +

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Fig. 1 Arrangement of polyhedra in sillenites: space group I23 (a), space group P23 (b).

$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
1 $BI_{24}(SI^{-1}, (1)BI^{-1}, (1)MI^{-1}, (2), (0.39, 95(2), (20, 0.05)))$ $I2S^{-1}$	(3)
$\begin{array}{c c c c c c c c c } \hline & & & & & & & & & & & & & & & & & & $	(3)
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	5(1)
$\begin{array}{c c c c c c c c c } \hline D = 3.5; \ FC_{calc}/FC_{exp.} = 3.5(3)/3.95 & dark green \\ \hline 3 & Bi_{24}(Si^{4+}_{0.9(1)}Mn^{4+}_{1.1})O_{40} & P23 & cube/ & 10.128 \\ \hline R_1 = 4.13, \ wR_2 = 4.52; & dark green \\ \hline D = 3.6; \ FC_{calc}/FC_{exp.} = 4.2(1)/4 & dark green \\ \hline \end{array}$	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
$R_1 = 4.13, wR_2 = 4.52;$ $D = 3.6; FC_{calc}/FC_{exp} = 4.2(1)/4$ dark green	7(1)
D = 3.6; FC _{calc} /FC _{exp} = $4.2(1)/4$	~ /
4 $Bi_{24}(Si^{4+}_{0.04}Bi^{3+}_{0.60}Mn^{4+}_{1.36})(O_{39,70}\square_{0.30})$ P23 tetrahedron/ 10.186	5(2)
$R_1 = 4.00, wR_2 = 4.55;$ dark green	
D = 4.5; FC _{calc} /FC _{exp} = $3.7(2)/3.7$	
5 $Bi_{24}(Si_{0.58}^{4+}Bi_{0.02}^{3+}Mn_{1.4}^{4+})(O_{39,99}\square_{0.01})$ <i>I</i> 23 cube + 10.151)(1)
$R_1 = 5.75, wR_2 = 5.27;$ tetrahedron/	
D = 4.7; FC _{calc.} /FC _{exp.} = 4.0(4)/3.99 dark green	
$6 \qquad Bi_{24}(Si^{4+}_{0.17(1)}Bi^{3+}_{0.01}Mn^{4+}_{1.82})(O_{39.93(5)}\square_{0.07}) \qquad P23 \qquad cube/ \qquad 10.150$	4(1)
$R_1 = 3.84, wR_2 = 4.13;$ dark green	
D = 3.6; FC _{calc} /FC _{exp.} = 4.2(2)/3.995	
7 $Bi_{24}(Si^{4+}_{1.150(6)}Bi^{3+}_{0.452}V^{5+}_{0.398})(O_{39.930(20)}\square_{0.070})$ P23 -/ 10.150	4(2)
$R_1 = 7.73, wR_2 = 23.35;$ orange	
D = 5.2; FC _{calc} /FC _{exp.} = 5.18/4.55	
8 $\operatorname{Bi}_{24}(\operatorname{Si}^{4+}_{1.160(6)}\operatorname{Bi}^{3+}_{0.430}(\operatorname{V}^{4+},\operatorname{V}^{5+})_{0.410})(\operatorname{O}_{39,970(20)}\square_{0.030})$ P23 -/ 10.142) (2)
$R_1 = 7.65, wR_2 = 21.98;$ green	
$D = 5.1; FC_{calc}/FC_{exp.} = 5.12/4.57$	

Fable 1 Characterization of investigated	crystals in the Bi ₂ O ₃ -	$-SiO_2 - M_xO_y$ (M	= Mn, V) systems.
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^a The structure refinements were performed in space group *I*23.

^b Space group not analyzed, space group *I*23 was used.

Mn(NO₃)₂·6H₂O, and NaBiO₃ + Na₂SiO₃·9H₂O + V₂O₅, respectively (alkaline solvent NaOH, $T = 310^{\circ}$ C, $\Delta T = 40^{\circ}$ C, $p = 500 \text{ kg/cm}^2$).

The crystals in the Bi_2O_3 -SiO_2-MnO_2 system were grown as spontaneous single crystals (dark green color, cubes, tetrahedra and combinations of cube and tetrahedron crystal habits, dimensions $\leq 1 \text{ mm}^3$) (samples 1-6 in Table 1). The crystals in the Bi_2O_3 -SiO_2-V₂O₅ system were grown as bulk crystals (green and orange color, $Bi_{24}Ge_2O_{40}$ seed crystal, dimensions $\sim 3 \times 3 \times 3$ mm) (samples 7, 8 in Table 1).

The morphology of the spontaneous single crystals in the Bi₂O₃–SiO₂–MnO₂ system depends on the initial charge composition: cubes for Na₂SiO₃·9H₂O : Mn(NO₃)₂·6H₂O > 1, tetrahedra for Na₂SiO₃·9H₂O : Mn(NO₃)₂·6H₂O < 1 and a combination of cube and tetrahedron habit for Na₂SiO₃·9H₂O : Mn(NO₃)₂·6H₂O = 1:1.

Structural analyses of the spontaneous single crystals (samples 1-6, Table 2) were carried out on Xcalibur and CAD-4 diffractometers at room temperature (Mo K_{α} radiation, graphite monochromator, ω scan mode). For preliminary data processing, we used the CrysAlis RED and WinGX packages, respectively. A neutron diffraction study of the samples prepared in the Bi₂O₃-SiO₂-V₂O₅ system (samples 7, 8, Table 2) was carried out on the Orphee 5C2 reactor (LLB, France; $\lambda = 0.828$ Å). Fullmatrix least squares refinements, using the atomic coordinates of $Bi_{24}Si_2O_{40}$ [5] (space group I23) as starting parameters, were carried out with the SHELXL97 [8] and JANA2000 [9] program packages and included anisotropic displacement parameters for all the atoms. The individual occupancies of three different elements (Si, Mn, Bi and Si, V, Bi) on the tetrahedral site were assessed by the SHELXL97 program. The conditions for the data collection and refinement procedure were the same for all of the samples.

X-ray spectral microanalysis was carried out using an Oxford INCA Penta Fetx 3 instrument.

The formal charge (FC) of the tetrahedral site was controlled by the bond-valence method [10]. The electrostatic bond strength

 $S_{ij} = \exp[(R_{ij} - d_{ij}) / 0.37]$ (1)

where R_{ij} is the bond-valence parameter for a particular ion pair (tabulated data), and d_{ij} experimental values of the interatomic *M*-O or (M',M'')-O distances; FC_{calc} = 4×S_{ij} (Table 1).

The value of the parameter D [11] was employed to test the validity of the crystal structures:

$$D = \frac{\sum |\Delta|}{\sum v_a}, \quad |\Delta| = \left|\sum v_{ij} - v_a\right| \tag{2}$$

where $v_{ij} = k_j / r_i^n$ is the electrostatic bond strength from cations *j* to anions *i*, and

$$k_j = v_c / \left\lfloor \sum_i 1 / r_i^n \right\rfloor$$
(3)



Fig. 2 Unit cell parameter *a vs. x* in the systems $(1-x)Bi_{24}^{3+}Si_{24}^{4+}O_{40}-x"Bi_{24}^{3+}Mn_{2}^{4+}O_{40}"$ (*I*) and $(1-x)Bi_{24}^{3+}Bi_{2}^{3+}(O_{39}\Box_1)-x"Bi_{24}^{3+}Mn_{2}^{4+}O_{40}"$ (*II*).

is the constant of the cation polyhedra, v_c is the cation valency, r_i is the cation-anion distance, v_a is the anion valency. According to [11], the value of D must be less than 5 % (Table 1).

Results and discussion

On the basis of the cell parameters of $\text{Bi}^{3+}_{24}\text{Si}^{4+}_{2}\text{O}_{40}$ (a = 10.104(1) Å) and $\text{Bi}^{3+}_{24}\text{Ge}^{4+}_{2}\text{O}_{40}$ (a = 10.153(4) Å [2]) and the corresponding ionic radii $r(\text{Si}^{4+}) = 0.26$ Å and $r(\text{Ge}^{4+}) = 0.39$ Å [12] we derived an expression for the cell parameters of all $\text{Bi}^{3+}_{24}M^{4+}_{2}\text{O}_{40}$ phases ($a = 0.3769r(M^{4+}) + 10.006$ Å) assuming the fulfillment of Vegard's law. Fig. 2 shows the dependence of the cell parameters of the sillenites in the $(1-x)\text{Bi}^{3+}_{24}\text{Si}^{4+}_{2}\text{O}_{40} - x^{"}\text{Bi}^{3+}_{24}\text{Mn}^{4+}_{2}\text{O}_{40}"$ (line I) and $(1-x)\text{Bi}^{3+}_{24}\text{Bi}^{3+}_{2}(\text{O}_{39}\square_{1}) - x^{"}\text{Bi}^{3+}_{24}\text{Mn}^{4+}_{2}\text{O}_{40}$ " (line II) systems on the composition (x value) using literature data for the $\text{Bi}^{3+}_{24}\text{Si}^{4+}_{2}\text{O}_{40}$ [5] and $\text{Bi}^{3+}_{24}\text{Bi}^{3+}_{2}(\text{O}_{39}\square_{1})$ [13] phases and the calculated value $a \sim 10.15$ Å for the "Bi}^{3+}_{24}\text{Mn}^{4+}_{2}\text{O}_{40}" phase ($r(\text{Mn}^{4+}) = r(\text{Ge}^{4+}) = 0.39$ Å). These dependencies have been outlined by straight lines obeying Vegard's law.

 $\begin{array}{c} The \ experimental \ points \ corresponding \ to \\ Bi_{24}(Si^{4+}_{0.9(1)}Mn^{4+}_{1.1})O_{40} \quad (sample \ 3) \ and \\ Bi_{24}(Si^{4+}_{0.04}Bi^{3+}_{0.60}Mn^{4+}_{1.36})(O_{39.70}\square_{0.30}) \ (sample \ 4) \ (\square -1)^{1/2} \ (\square$ vacancy) fit well on the straight lines I and II, respectively. There is good agreement between the values of FC of the tetrahedral sites calculated by the bond-valence method and the experimental ones for samples 3 and 4 (Table 1). The positive deviation from the linear dependence I is ascribed to Bi³⁺ ions. The composition of sample 2 obtained using quantitative X-ray spectral microanalysis $(Bi_{24,2(1)}(Si_{0,7(1)}Mn_{1,1})O_{40})$ does not contradict the composition calculated from X-ray data (Table 1). This fact supports the presence of additional Bi³⁺ ions in samples 1, 5 and 6.

The crystal structures were refined in the I-centered space group I23; atomic coordinates, equivalent displacement parameters and occupancies of the tetrahedral cationic positions are listed in Table 2. The relatively low *R* discrepancy factors and the positive displacement parameters for all the atoms confirm the main features of the structure. However, the presence of a certain number of hkl reflections with $F > 3\sigma(F)$ (*F* is the structure factor) that are systematically absent in space group I23 (hkl with $h+k+l \neq 2n$, 0kl with $k+l \neq 2n$, hhl with $l \neq 2n$, h00with $h \neq 2n$) for samples 3, 4, 6, 7 and 8 was a clear indication for lower symmetry. Data for sample 1 were collected for space group I23. The opportunity of changing to P23 symmetry was noticed in a later experiment for sample 3 and for samples 2-8 the space group was analyzed. All the crystallographic sites in the structure are split by the transition from space group I23 to space group P23 (Fig. 1). For example, the structure of sample 6 $(Bi_{24}(Si^{4+}_{0.17(1)}Bi^{3+}_{0.01}Mn^{4+}_{1.82})(O_{39,93(5)}\square_{0.07}))$ refined in

Table 2 Atomic coordinates, equivalent isotropic thermal parameters $U_{eq} \times 10^2$ (Å²), site occupancies μ , and selected interatomic distances d (Å) determined on single crystals. Space group *I*23, Bi2,Si,*M* in Wyckoff position 2*a* (0 0 0), O2 and O3 in 8*c* (*x x x*).

Parameter		Sample							
		1	2	3	4	5	6	7	8
Bi1	x	0.82321(8)	$0.17683(3)^{a}$	$0.17664(4)^{a}$	$0.17719(5)^{a}$	$0.17729(5)^{a}$	0.31919(1)	$0.17592(2)^{a}$	$0.18167(3)^{a}$
	у	0.98153(8)	0.31960(4)	0.31919(5)	0.32060(6)	0.32027(6)	-0.01883(1)	0.31830(2)	0.32392(2)
	z	0.68064(8)	0.01915(4)	0.01872(5)	0.01774(5)	0.01964(6)	-0.17671(1)	0.01629(2)	0.48422(3)
	μ	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
$U_{\rm eq} \times 10^2$		1.037(15)	1.364(7)	0.724(8)	1.47(14)	1.3(1)	0.830(2)	1.753(4)	1.888(5)
Bi2	μ	0.05(7)	0.05(5)	-	0.30(4)	0.01(6)	0.006(2)	0.226(3)	0.215(3)
Si	μ	0.83(7)	0.55(5)	0.47(7)	0.02(4)	0.29(6)	0.084(2)	0.711(11)	0.750(12)
М	μ	0.1(7)	0.40(5)	0.53(7)	0.68(4)	0.70(6)	0.910(2)	0.575(3)	0.580(3)
$U_{\rm eq} \times 10^2$		0.9(3)	0.64(4)	0.7(2)	0.49(1)	0.90(6)	0.99(19)	0.199(3)	0.205(3)
01	x	0.365(2)	0.1336(9)	0.135(1)	0.1352(12)	0.1379(11)	0.2553(3)	0.13488(3)	0.24922(4)
	у	0.009(2)	0.2492(8)	0.2511(9)	0.2493(11)	0.2520(10)	0.0102(3)	0.25113(3)	0.36543(4)
	z	0.247(2)	0.4890(9)	0.487(1)	0.4895(12)	0.4854(13)	-0.3694(3)	0.48620(3)	0.01439(4)
	μ	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
$U_{\rm eq} \times 10^2$		0.9(2)	1.7(2)	1.1(1)	1.8(3)	1.4(2)	2.13(7)	1.881(6)	2.024(8)
O2	x	0.803(2)	0.1975(9)	0.1988(9)	0.1898(13)	0.195(4)	0.1977(3)	0.19492(4)	0.30583(4)
	μ	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
$U_{\rm eq} \times 10^2$		1.0(4)	1.6(1)	0.8(2)	2.2(2)	1.6(2)	2.05(9)	1.859(8)	1.882(9)
03	x	0.098(3)	0.9036(10)	0.905(1)	0.894(2)	0.902(4)	0.0915(3)	0.89984(3)	0.10011(4)
	μ	0.987(5)	0.75^{b}	1.0	0.963 ^b	0.998^{b}	0.98(1)	0.983(5)	0.993(5)
$U_{\rm eq} \times 10^2$		2.3(9)	1.9(1)	1.6(3)	2.3(2)	2.2(2)	1.1(1)	2.208(10)	2.388(12)
Bi1 $-1 \times$	01	2.07(2)	2.069(9)	2.06(1)	2.060(12)	2.044(11)	2.0805(28)	2.0684(4)	2.0673(4)
$-1 \times$	01	2.24(2)	2.200(9)	2.20(1)	2.220(12)	2.197(12)	2.1808(30)	2.2218(4)	2.2146(5)
$-1 \times$	01	2.59(2)	2.591(9)	2.61(1)	2.590(12)	2.650(12)	2.5545(30)	2.6221(4)	2.6181(5)
$-1 \times$:02	2.205(7)	2.203(9)	2.21(1)	2.205(13)	2.19(4)	2.2036(11)	2.2120(3)	2.2121(3)
$-1 \times$:03	2.66(2)	2.677(10)	2.67(1)	2.62(2)	2.68(4)	2.7081(24)	2.6251(3)	2.6220(4)
d(Bi1-O);	av	2.35(2)	2.348(9)	2.35(1)	2.34(1)	2.35(2)	2.3455(25)	2.3499(4)	2.3468(4)
Bi2,Si, \overline{M} - 4×	:03	1.73(5)	1.694(10)	1.67(1)	1.88(2)	1.72(4)	1.6071(53)	1.7609(6)	1.7587(7)

^a Left form of the crystal

^b Occupancy of the position was calculated on the base of neutrality of the system.

*I*23 symmetry contains a single lattice site 2a that is filled with ~14 % Si, ~8% Bi and ~78% Mn in random distribution, while for *P*23 symmetry two different crystallographic sites, 1a and 1b, exist (sites M'' and M' in Fig. 1b). Each of them can accommodate Si, Bi and Mn, but in general with different occupancy factors.

In this case we may deal with a kinetic phase transition of order-disorder type [3], *i.e.* a partially ordered phase with a P cubic unit cell forms in the stability area of the disordered phase with an I cubic unit cell under the influence of kinetic factors. The ordering will depend on the composition, structure peculiarities, and chemical properties of the components, as well as on the preparation conditions, in particular on the initial composition [14]. Based on preliminary results, the single crystals of cube and tetrahedron habits (different amounts of the starting materials Na₂SiO₃·9H₂O and Mn(NO₃)₂·6H₂O) have space group P23, whereas the single crystals with a combination of cube and tetrahedron habit (equal

amounts of the starting materials) crystallize in space group *I*23.

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