de Haas–van Alphen effect and Fermi surface properties in rare earth and actinide compounds (Review Article)

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Fermi surface properties in rare earth (R) and actinide (An) compounds of RX₃ (X: Al, Ga, In, Si, Ge, Sn, Pb), AnX₃, RTIn₅ (T: transition metal), and AnTGa₅ are clarified as a function of the number of valence electrons. The electronic state can be changed by applying pressure and magnetic field. A change of Fermi surface properties associated with the metamagnetic behavior and the quantum critical point is also clarified precisely, together with the split Fermi surfaces in the non-centrosymmetric crystal structure, and the de Haas–van Alphen oscillations in the superconducting mixed state. In the quantum critical point region, the conduction electrons, or quasi-particles, are of an *f*-electron character, with heavy effective masses of $10-100 m_0 (m_0)$ is the rest mass of an electron) and condense into the unconventional (anisotropic) superconducting state.

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71.20.-b Electron density of states and band structure of crystalline solids;

81.05.U- Carbon/carbon-based materials.

Keywords: de Haas-van Alphen effect, rare earth, actinide compounds, Fermi surface.

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Dedicated to the memory of Prof. David Shoenberg

1. Introduction

The f-electron compounds of lanthanide and actinide compounds, especially lanthanide compounds, are usually treated in magnetism by an *f*-localized model, whereas they indicate various interesting phenomena such as heavy fermions and anisotropic superconductivity. These originate from the f electrons in the lanthanide and actinide compounds. Here, the 4f(5f) electrons in the lanthanide (actinide) atoms are pushed deep into the interior of the closed $5s^25p^6$ ($6s^26p^6$) shells because of the strong centrifugal potential $\ell(\ell+1)/r^2$, where $\ell = 3$ holds for the *f* electrons. This is the reason why the f electrons possess an atomiclike character even in a compound. The localized *f*-electron picture is thus a good starting point in magnetism, especially in the lanthanide compounds. On the other hand, the tail of their wave function in the f-electron compounds spreads to the outside of the closed $5s^25p^6$ ($6s^26p^6$) shells because it is highly influenced by the potential energy, the relativistic effect, the distance between the lanthanide (actinide) atoms, and hybridization of the f electrons with the conduction electrons.

The *f* electrons of cerium and uranium compounds are typical in exhibiting a variety of characteristic features including spin and charge orderings, spin and valence fluctuations, heavy fermions and anisotropic superconductivity [1-3]. In these compounds, the Ruderman–Kittel–Kasuya–Yosida (RKKY) interaction and the Kondo effect compete with each other. The RKKY interaction enhances the long-range magnetic order, where the *f* electrons with magnetic moments are treated as localized electrons, and the indirect

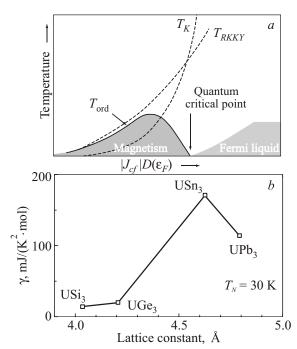


Fig. 1. Doniach phase diagram (*a*) and the γ vs lattice constant in UX₃, cited from Ref. 3 (*b*).

f-f interaction is mediated by the spin polarization of the conduction electrons. The intensity of the RKKY interaction is proportional to the square of the magnetic exchange interaction J_{cf} between the f electrons and conduction electrons, and the corresponding characteristic temperature T_{RKKY} is expressed by

$$T_{RKKY} \propto D(\varepsilon_F) |J_{cf}|^2, \qquad (1)$$

where $D(\varepsilon_F)$ is the electronic density of states at the Fermi energy ε_F .

On the other hand, the Kondo effect quenches the magnetic moments of the localized f electrons by the spin polarization of the conduction electrons, producing a spin singlet state with a binding energy $k_B T_K$ at the cerium and uranium sites, which leads to a heavy fermion state with an extremely large effective mass at temperatures lower than the Kondo temperature T_K . The Kondo effect is characterized by the Kondo temperature T_K , which depends exponentially on $|J_{cf}|$ as follows:

$$T_K \propto \exp\left\{-1/(D(\varepsilon_F)|J_{cf}|)\right\}.$$
 (2)

The competition between the RKKY interaction and the Kondo effect was discussed by Doniach [4] as a function of $|J_{cf}|D(\varepsilon_F)$, as shown schematically in Fig. 1,*a*. The Doniach phase diagram is a good guiding principle to reach the quantum critical point, which is defined as the magnetic ordering temperature $T_{\text{ord}} \rightarrow 0$. This is expressed experimentally by the chemical pressure as in UX₃ (X: Si, Ge, Sn, Pb) shown in Fig. 1,*b* and by applying external pressure, as shown later.

The magnetic susceptibility of $CeCu_6$ and $CeRu_2Si_2$ as well as that of UPt₃ and UPd₂Al₃, shown in Fig. 2, increases with decreasing temperature, following the Curie–

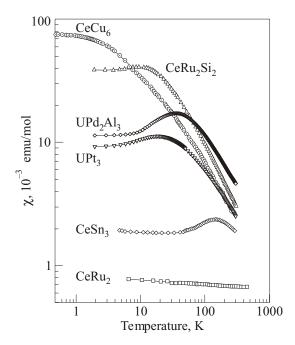


Fig. 2. Temperature dependence of the magnetic susceptibility in the typical cerium and uranium compounds, cited from Ref. 3.

Weiss law at high temperatures, and has a maximum at a characteristic temperature $T_{\chi max}$ [3]. Below $T_{\chi max}$, the susceptibility becomes almost temperature-independent, and the *f*-electron system is changed into a new electronic state, called the heavy fermion state. Here $T_{\chi max}$ approximately corresponds to the Kondo temperature T_K .

The heavy fermion state in the cerium compounds is roughly understood as follows [5]. The 4f levels of the cerium ions are split into J-multiplets (J = 7/2 and 5/2) due to the spin-orbit interaction, where the 4f electrons in the cerium compounds are almost localized in nature, as mentioned above. The corresponding sixfold J = 5/2 multiplet is furthermore split into three doublets in the non-cubic crystalline electric field (CEF) scheme. The magnetic susceptibility at high temperatures follows the Curie-Weiss law with the effective magnetic moment of Ce³⁺, namely, 2.5 μ_B /Ce. The electronic state is, however, changed with decreasing temperature. At low temperatures, the magnetic entropy of the ground-state doublet in the 4*f* levels, $R \log 2$, is obtained by integrating the magnetic specific heat C_m in the form of C_m/T over the temperature. When C_m is changed into the electronic specific heat γT via the many-body Kondo effect, the following relations are obtained:

$$R \log 2 = \int_{0}^{T_K} \frac{C_m}{T} dT,$$
(3)

$$C_m = \gamma T . \tag{4}$$

The γ value can be obtained as

$$\gamma = \frac{R \log 2}{T_K} \approx \frac{10^4}{T_K} \text{ (mJ/K}^2 \cdot \text{mol}).$$
 (5)

For example, the γ value and the Kondo temperature are 1600 mJ/(K²·mol) and 5 K in CeCu₆, and 350 mJ/(K²·mol) and 20 K in CeRu₂Si₂, respectively. The 4*f*-localized electronic state is thus changed into a 4*f*-derived band with a flat energy vs momentum dispersion, possessing an extremely large effective mass. The 4*f*-itinerant band model is highly applicable to the Fermi surfaces in CeRu₂, CeSn₃ and CeRu₂Si₂, which are determined from the de Haas–van Alphen (dHvA) experiment, although the detected cyclotron mass m_c^* is larger than the corresponding band mass m_b . This is because the many-body Kondo effect is not included in the conventional band calculation. A similar feature is found in uranium compounds such as UPt₃ and UPd₂Al₃.

These strongly correlated electrons follow the Fermi liquid nature at low temperatures. The electrical resistivity ρ varies as $\rho = \rho_0 + AT^2$, where ρ_0 is the residual resistivity. The coefficient \sqrt{A} is two to three orders of magnitude larger than that in the usual *s* and *p* electron systems. \sqrt{A} correlates with an enhanced Pauli susceptibility $\chi(T \rightarrow 0) \simeq \chi_0$ and with a large electronic specific heat coefficient $C/T(T \rightarrow 0) \simeq \gamma$.

Interestingly, some heavy fermion systems show unconventional (anisotropic) superconductivity [6]. The most

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important observation for the well-known heavy fermion superconductors such as CeCu₂Si₂, UPt₃, and UPd₂Al₃ is that superconductivity is realized in the magnetically ordered state or the antiferromagnetic (ferromagnetic) fluctuations. The physical quantities such as the specific heat and the spin-lattice relaxation rate do not follow the exponential dependence of exp $(-\Delta/k_BT)$ in the superconducting state, which is expected from Bardeen-Cooper-Schrieffer (BCS) theory, but obey a power law of T^n . Here, Δ is the superconducting energy gap, and n is an integer. This means that the superconducting gap is not completely opened in k space but possesses line and/or point nodes. For example, n = 2 corresponds to the line node. These results are based on the fact that quasi-particles with heavy masses of $10-100 m_0$ (m_0 is the rest mass of an electron) are of an *f*-electron character, which originates from the strong Coulomb repulsion between the f electrons. These quasi-particles condense into Cooper pairs.

When the phonon-mediated attractive interaction is compared with the strong repulsive interaction among the felectrons, it is theoretically difficult for the former interaction to overcome the latter. To avoid a large overlap of the wave functions of the paired particles, the heavy fermion system preferentially chooses an anisotropic channel, such as a *p*-wave spin triplet state or a *d*-wave spin singlet state to form Cooper pairs [6]. The neutron-scattering experiments clearly indicated evidence of a close relationship between superconductivity and magnetic excitation in UPd₂Al₃ [7–9]. The magnetic excitation gap of UPd₂Al₃, which appears in the inelastic neutron profile below the superconducting transition temperature T_{sc} , corresponds to the superconducting order parameter.

Figure 3 shows a schematic view of the superconducting order parameter with *s*-, *d*-, and *p*-wave pairing. The order parameter $\Psi(r)$ with even parity (*s*- and *d*-waves) is symmetric with respect to *r*, where one electron with the up-spin state, \uparrow of the Cooper pair is simply considered to be located at the center of $\Psi(r)$, where r = 0, and the other electron with the down-spin state, \downarrow is located at *r*. The width of $\Psi(r)$ with respect to *r* is called the coherence length ξ , as shown in Fig. 3,*a*.

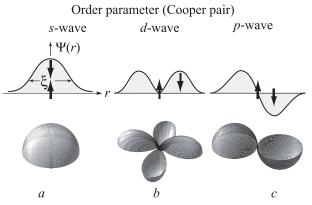


Fig. 3. Schematic view of the superconducting order parameter with *s*-wave, *d*-wave and *p*-wave pairing, cited from Ref. 3.

The technique of nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) has proved to be a useful tool for determining the symmetry of the superconducting condensate. UPd₂Al₃ is considered to be a *d*-wave superconductor from NMR experiments [10], which corresponds to the case in Fig. 3,*b*. The origin of pairing has also been clarified by neutron-scattering experiments on UPd₂Al₃ [7–9], as mentioned above. On the other hand, $\Psi(r)$ with odd parity (*p*-wave) is not symmetric with respect to *r*, where the parallel spin state is shown in Fig. 3,*c*. From NMR and magnetization experiments [11,12], UPt₃ is considered to possess odd parity in symmetry.

Recently, a new aspect of cerium and uranium compounds with magnetic ordering has been discovered. When pressure P is applied to compounds with antiferromagnetic ordering such as CeCu₂Ge₂ [13], CeIn₃, CePd₂Si₂ [14] and CeRhIn₅ [15], the Néel temperature T_N reaches zero at the quantum critical pressure P_c : $T_N \rightarrow 0$ for $P \rightarrow P_c$, and superconductivity is observed at around P_c . Superconductivity is surprisingly found even in the ferromagnetic states of UGe₂ [16], URhGe [17], UIr [18] and UCoGe [19]. The crossover from the magnetically ordered state to the nonmagnetic state under pressure, crossing the quantum critical point, is the most interesting issue in strongly correlated *f*-electron systems. The electronic states can be tuned by pressure. Experimentally, the quantity $|J_{cf}|D(\varepsilon_F)$ in Fig. 1,*a* corresponds to pressure *P*.

It is also noted that the wave function of f electrons in the lanthanide and actinide metals shrinks with increasing the number of f electrons. In the lanthanide metals, this is well known as the lanthanide contraction. There exists the similar trend for the actinide metals such as Am, Cm, Bk, and Cf, revealing the localized nature of 5f electrons. On the other hand, the Wigner–Seitz radius R_{WS} , which is related to the atomic volume V_{WS} (= (4 π /3) R_{WS}^3), steeply decreases from Th to Np, as in transition metals, but increases as a function of the number of 5f electrons, as shown in Fig. 4 [20]. The Wigner–Seitz radius of Am is close to the localized 4f-electron radius of lanthanide metals, and thus

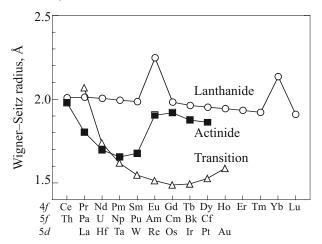


Fig. 4. Wigner–Seitz radius of the actinide, lanthanide and transition metals, cited from Ref. 20.

the radius of Pu has an intermediate value between Np and Am. This is an important feature to understand the electronic states of actinide compounds, which is also related to the crystal structure. The 5f-itinerant band model is applicable to the electronic state of a heavy fermion superconductor UPt₃, as shown later. On the other hand, the 5f-localized electronic state is also well established experimentally in UPd₃. Our attention is similarly concentrated on the electronic states in transuranium compounds including Np and Pu [21].

In this paper, we discuss the Fermi surface properties of lanthanide and actinide compounds including the corresponding Sc and Y compounds, and here after the rare earth is used instead of the lanthanide.

In the next chapter, we present several kinds of techniques for growing high-quality single crystals of rare earth and actinide compounds, and describe the dHvA effect. We present in Chaps. 3–9 the Fermi surface properties based on the results of dHvA experiment and energy band calculation in RX₃ (AnX₃), RTIn₅ (R: rare earth, T: transition metal) and AnTGa₅ (An: actinide), a change of Fermi surface properties in metamagnetism and quantum critical point, split Fermi surfaces in the non-centrosymmetric crystal structure, and dHvA oscillations in the superconducting mixed states. In the final chapter, the characteristic features in these compounds are summarized.

2. Single crystal growth and dHvA experiment

In the dHvA experiment, we need high-quality single crystals as well as low temperatures down to 30 mK and strong magnetic fields up to 170 kOe, for example. Various techniques for the single crystal growth were applied to rare earth and actinide compounds, depending on the melting point and the degree of the vapor pressure of the melt, as shown in Tables 1–4, for cerium, thorium, uranium and transuranium compounds, respectively [22]. These compounds were used for the dHvA experiment.

Table 1. Single crystal growth and Fermi surface studies in cerium compounds, which indicate a wide variety of electronic states such as paramagnetism including Pauli paramagnetism, denoted as (P), quadrupolar ordering (Q) including multipolar ordering, ferromagnetism (F), antiferromagnetism (AF), and superconductivity (S)

Cz	CeRu ₂ (P,S)	$\operatorname{CeRh}_{2}(P)$	$CeSn_3(P)$	CeNi (P)
	$CeRu_2Si_2(P)$	CeAg (Q, F)	$CeGa_2(F)$	$CeRh_{3}B_{2}(F)$
	$CeRu_2Ge_2(F)$		CeIn ₃ (AF)	Ce ₃ Sn ₇ (AF)
	CeRh ₂ Si ₂ (AF)			
Flux	CeIrIn ₅ (P,S)	CeCoIn ₅ (P,	S)	$CeAgSb_2(F)$
	CeRhIn ₅ (AF)	CeCoGe ₃ (A	F)	
	Ce ₂ RhIn ₈ (AF)			
Br	CeSb (AF) CeI	Pt ₃ Si (AF, S)	CePtP (AF)	CePtAs (AF)
	CePd ₅ Al ₂ (AF)			
FΖ	$CeB_6(Q, AF)$			

Table 2.	Single	crystal	growth	and	Fermi	surface	studies	in
thorium com	pounds							

Flu	IX		ThIn ₃	(P)	$ThRhIn_{5}(P)$			P)	
Tab	le 3.	Single	crystal	growth	and	Fermi	surface	studies	in
uraniun	n con	npounds	5						

	-
Cz	UC (P) USi_3 (P) UB_2 (P) UB_4 (P) UPt_3 (P, S)
	URu ₂ Si ₂ (S) UGe ₂ (F) UIr (F) UPd ₂ Al ₃ (AF, S)
Flux	UAl ₃ (P) UFeGa ₅ (P) UCoGa ₅ (P) URhGa ₅ (P)
	UGa2 (F) UGa3 (AF) UIn3 (AF) USb2 (AF) UBi2 (AF)
	UNiGa5 (AF) UPdGa5 (AF) UPtGa5 (AF)
СТ	$U_{3}P_{4}(F) U_{3}As_{4}(F) UP_{2}(AF) UAs_{2}(AF)$

Table 4. Single crystal growth and Fermi surface studies in transuranium compounds

Flux	NpGe ₃ (P)	NpNiGa5 (AF)	NpCoGa5 (AF)
	NpRhGa5 (Q, AF)	NpPtGa5 (AF)	PuIn ₃ (P)

If the vapor pressure is low, the Czochralski pulling method denoted as Cz is a powerful method to obtain a large size of a single crystal ingot. The rf furnace was used for the Cz method when the melting point is less than 1500 °C and the tungsten crucible is available for CeCu₆, for example, as shown in Fig. 5,a. In this case, the tungsten crucible, which is surrounded by an rf-working coil, becomes a heater for the CeCu₆ melt. A large ingot with 10 mm in diameter and 80 mm in length is obtained in CeCu₆, where a necking procedure with a small size less than 1 mm in diameter in the pulling process is available in this temperature-stable rf furnace. In the next chapter, we discuss the Fermi surface properties of RIn₃. Single crystals of light rare earth RIn3 (R: La-Gd) compounds, except SmIn₃, were grown by the Cz method in the rf furnace. The heavy rare earth RIn₃ (R: Tb-Lu) single crystals, including SmIn₃, were grown by the In-self flux method because of high vapor pressure of heavy rare earth metals.

The Cz method was also applied to the compounds with high-melting points, for example about 2500 °C, in the tetra-arc furnace. In this case, as shown in Fig. 5,*b*, the crucible is unnecessary. The starting materials are set on the Cu-heath plate, and grown by the Czochralski method in a tetra-arc furnace. The typical compounds with highmelting points are CeRh₃B₂, UB₂ and UC. Figure 5,*c* shows single crystal ingots of UPt₃, CeRu₂ and CeIrSi₃ grown by the Cz method in the tetra-arc furnace. CeIrSi₃ is known to be a pressure-induced superconductor without inversion symmetry in the tetragonal crystal structure [23].

The Cz method was also applied to the incongruent compounds such as CeRu₂ and USi₃. Figure 6 is the binary phase diagram of CeRu₂ and USi₃. For these compounds, we prepared the off-stoichiometric starting materials of CeRu_{1.8} and USi_{4.6}, respectively in the tetra-arc furnace. Large single crystal ingots with 3–4 mm in diameter and 60 mm in length for CeRu₂ and USi₃ were grown, as shown in Fig. 5,*c*. Annealing of the electrotransport me-

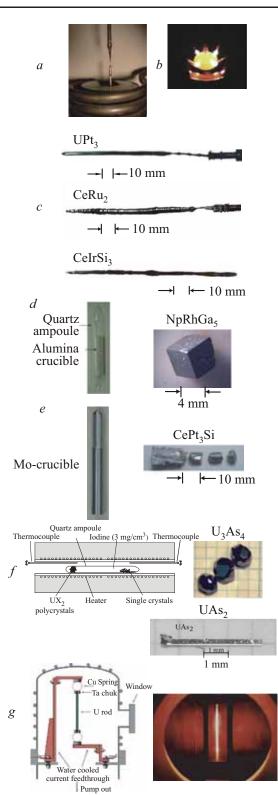


Fig. 5. Photograph of CeCu₆ ingot grown by the Czochralski method in the rf furnace with a working coil (*a*), CeRu₂ ingot grown in a tetra-arc furnace (*b*), single crystal ingots of UPt₃, CeRu₂ and CeIrSi₃ obtained by the Czochralski method (*c*), NpRhGa₅ grown by the flux method in the alumina crucible (*d*), CePt₃Si grown by the Bridgman method in the Mo-crucible (*e*), U₃As₄ and UAs₂ grown by the chemical transport method (*f*), and a UPt₃ ingot which was annealed under high vacuum of 10⁻¹⁰ Torr via the solid state electrotransport method (*g*).

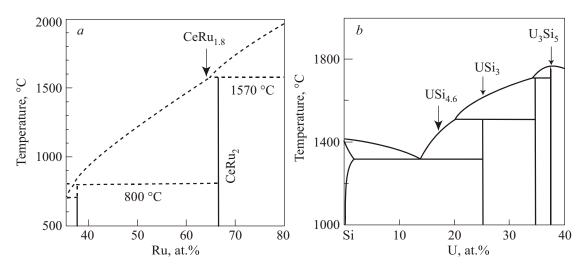


Fig. 6. Binary phase diagrams of CeRu₂ (a) and USi₃ (b), cited from Ref. 22.

thod, which is described below, was also applied to the ingot, reaching the residual resistivity $\rho_0 = 0.6 \ \mu\Omega$ ·cm and the residual resistivity ratio 270 in CeRu₂.

On the other hand, the flux method (Flux), the chemical transport method (CT) and the Bridgman method (Br) are useful for the compounds with the high vapor pressure, and also for the incongruent compounds. The floating zone method (FZ) was also applied to CeB₆. Figure 5,d indicates a single crystal of NpRhGa5 grown by the Ga-flux method, where the starting materials and flux were inserted in an alumina crucible, sealed in a quartz tube, heated up to 900-1000 °C in an electric furnace, and cooled down to lower temperatures, taking about 20 days. Usually, metals with low-temperature melting points such as Al, Ga, In, Sn, Pb, Sb and Bi are available. In the case of NpRhGa5, excess Ga itself becomes flux. A single crystal of CePt₃Si was grown by the Br method in a Mo crucible, as shown in Fig. 5,e. Single crystals of U₃P₄ and UAs₂ were grown by the chemical transport method with iodine in an electric furnace with a distinct temperature gradient, as shown in Fig. 5,f.

It is noted that the starting material of a uranium ingot was annealed under high vacuum of 10^{-10} Torr via the solid state electrotransport method, as shown in Fig. 5,g. For example, an Fe impurity of 40 ppm in the uranium ingot was reduced to less than 2 ppm, and the Cu impurity was completely removed [24]. Subsequent annealing under high vacuum using the electrotransport method drastically improved the quality of the single crystal, which was applied to CeRu₂, UPt₃ and URu₂Si₂, as shown in Fig. 5,g for UPt₃. For example, we recently obtained an extremely high-quality single crystal sample of URu₂Si₂, where the residual resistivity ratio (RRR) reaches more than 500 [21].

The dHvA experiment was performed by the standard field-modulation method with a modulation frequency of 7 Hz and a modulation field of 100 Oe [1,2]. Pressure was applied up to 3 GPa using an MP35N piston-cylinder cell with a 1:2 mixture of commercial Daphne oil (7373) and petroleum ether as a pressure-transmitting medium. The

pressure was calibrated by the superconducting transition temperature T_{sc} of Sn, which is accurate within 0.05 GPa of the absolute value. It is also noted that the cantilever type dHvA method is applicable and useful to an extremely small sample with 0.1×0.1×0.05 mm, for example [25–27].

The detected dHvA signal $V_{\rm osc}$ in the 2 ω technique is written as follows [28]:

$$V_{\rm osc} = \sum_{p} A_{p} \sin\left(\frac{2\pi pF}{H} + \phi_{p}\right),\tag{6}$$

$$A_p \propto J_2 \left(\frac{2\pi Fh}{H^2}\right) H^{1/2} p^{-3/2} \left|\frac{\partial^2 S_F(k_z)}{\partial k_z^2}\right|^{-1/2} R_T R_D R_S, \quad (7)$$

$$R_T = \frac{2\alpha m_c^* T/H}{\sinh\left(2\alpha m_c^* T/H\right)},\tag{8}$$

$$R_D = \exp \left(-\alpha m_c^* T_D / H\right), \qquad (9)$$

$$R_{S} = \cos\left(p\pi m_{c}^{*}g/2m_{0}\right), \qquad (10)$$

$$\alpha = 2\pi^2 pck_B/e\hbar.$$
 (11)

Index p = 1, 2, 3, ... represents the fundamental (p = 1) and the higher-harmonic (p = 2, 3, ...) dHvA frequencies, and J_2 is the Bessel function. The dHvA amplitude A_p is related to the so-called curvature factor $\partial^2 S_F(k_z)/\partial k_z^2$, the thermal reduction factor $R_T (R_T \rightarrow 1 \text{ for } T \rightarrow 0)$, the Dingle reduction factor $R_D (R_D \rightarrow 1$ for the Dingle temperature $T_D \rightarrow 0$, which is caused by the finite scattering lifetime of the conduction electrons, and the spin reduction factor R_S ($R_S = 1$ for the cyclotron mass $m_c^* = m_0$ and g = 2), which is the interference between the oscillations of spin-up and spin-down electrons. Here m_0 is the rest mass of an electron. The dHvA frequency $F = c\hbar S_F/2\pi e$, which obtained in the fast Fourier transformation (FFT) spectrum of the oscillation, is proportional to the extremal (maximum or minimum) cross-sectional area S_F of the Fermi surface. From the temperature and field dependences of the dHvA amplitude, we can determine the cyclotron effective mass m_c^* and the Dingle temperature T_D , respectively.

(13)

 $T_D = \hbar/2\pi k_B \tau$ is inversely proportional to the scattering lifetime τ of an conduction electron. We also estimate the mean free path ℓ from the simple relations: $S_F = \pi k_F^2$, $\hbar k_F = m_c^* v_F$, and $\ell = v_F \tau$, where k_F is half of the caliper dimension of a circular S_F and v_F is the Fermi velocity.

The dHvA experiments were also performed using the micro-cantilever (MouldLessCantilever, SSI-SS-ML-PRC120, Seiko Instruments Inc.) with the same modulation field of $h \simeq 100$ Oe (a modulation frequency of $\omega/2\pi = 11$ Hz), and without the modulation field. The DC-current ($I_{DC} \sim 0.05$ mA) was used with the modulation field, and the AC-current ($I_{AC} \sim 0.05$ mA) was used without the modulation field. The amplitude A for the torque method using the cantilever is written as

$$A \propto I_{AC} \frac{1}{F} \frac{dF}{d\theta}$$
 (without the modulation field) (12)

 $A \propto I_{DC} \omega J_1(x) \frac{1}{F} \frac{dF}{d\theta}$

(with the modulation field and ω detecting technique), where I_{AC} and I_{DC} are the AC and DC excitation current for the cantilever. $J_1(x)$ is the first Bessel function due to the modulation field.

and

The experimentally obtained dHvA results of cerium, thorium, uranium and transuranium compounds, which are shown in Tables 1–4, respectively, were compared with the results of energy band calculation [1–3,5,21–23,29–31]. These compounds include a wide variety of electronic states such as paramagnetism including Pauli paramagnetism, denoted as (P) in Tables 1–4, quadrupolar ordering (Q) including the multi-polar ordering, ferromagnetism (F), antiferromagnetism (AF), and superconductivity (S).

3. Fermi surface properties in RIn₃ (R: La-Lu)

The RIn₃ and RGa₃ (R: Sc, Y, and La-Lu) compounds crystallize in the AuCu₃-type cubic crystal structure, as shown in Fig. 7, a, where the corner-sites are occupied by the R atoms and the face-centered sites are occupied by the In and Ga atoms. The characteristic properties of RIn3 is summarized in Table 5 and in Fig. 7. Most of RIn₃ compounds order antiferromagnetically, except a paramagnet of PrIn₃ with the singlet ground state in the CEF scheme and a divalent Pauli paramagnet of YbIn3. The divalent property of YbIn₃ is clear from the lattice constant of RIn₃, as shown in Fig. 7,b, because the lattice constant of YbIn₃ deviates from the lanthanide contraction [32]. The Néel temperature T_N of RIn₃ is shown in Fig. 7,c, which approximately follows the de Gennes scaling: $T_N \sim (g_J - 1)^2 J(J+1)$, where g_J is the Landé g-factor and J is the total angular momentum [33,34]. Among RIn3 antiferromagnets, CeIn3 is a well known Kondo-lattice compound showing antiferromagnetic ordering at a Néel temperature $T_N = 10$ K [35–38]. The ordered moment 0.65 μ_B /Ce is comparable to the value 0.71 μ_B /Ce expected from the Γ_7 ground state in the CEF scheme. Nevertheless,

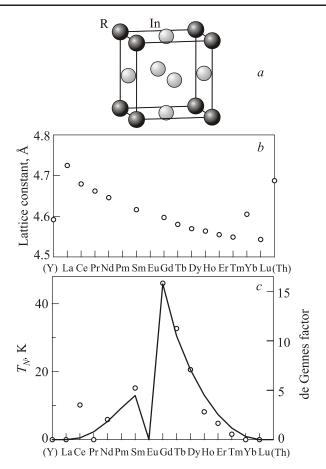


Fig. 7. Cubic crystal structure (*a*), lattice constant (*b*), cited from Ref. 32, and the Néel temperature T_N in RIn₃, where a solid line indicates the de Gennes scaling (*c*).

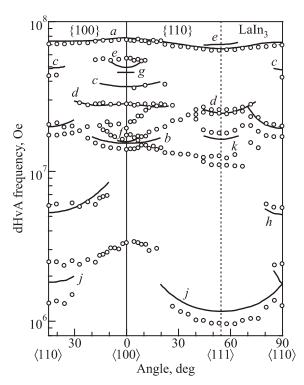


Fig. 8. Angular dependence of the dHvA frequency in $LaIn_3$, cited from Ref. 39. The solid lines are the results of band calculations [40].

RIn ₃	T_N , K	$\mu_s, \mu_B/R$	Electronic states at dHvA experiments	$a, 10^7 \text{ Oe}$ (m_c^*, m_0)	$d, 10^7 \text{ Oe}$ (m_c^*, m_0)	$b, 10^7 \text{ Oe}$ (m_c^*, m_0)	$j, 10^7 \text{ Oe}$ (m_c^*, m_0)
YIn ₃	0	0	Pauli Para	8.13	3.34	1.05	
				(0.64)		(0.27)	
LaIn ₃	0	0	Pauli Para	7.47	2.78	1.38	0.096
-			$\gamma = 7.7 \text{ mJ/(K}^2 \cdot \text{mol})$	(0.57)	(0.40)	(0.26)	(0.17)
CeIn ₃	10	0.65	AF		3.0		
-			$[H_c = 610 \text{ kOe}]$		(2.0)		
PrIn ₃	0	singlet CEF	Para	7.57	3.02	1.28	0.128
-		0	$\gamma = 11.4 \text{ mJ/(K}^2 \cdot \text{mol})$	(0.99)	(0.60)	(0.36)	(0.28)
NdIn ₃	5.9	2.3 (at 2 K)	AF $(H < H_{c3})$	8.09	3.17		0.12
-			Para $(H > H_{c3})$	(1.05)	(0.80)		(0.31)
			$[H_{c1} = 78, H_{c2} = 89, H_{c3} = 111 \text{ kOe}]$	7.75	3.0		0.12
				(1.14)			
SmIn ₃	$T_{N1} = 15.9$		AF (<i>H</i> < 130 kOe)	$H \parallel 0$	(110)		
	$T_{N2} = 15.2$			7.81	3.08		
	$T_{N3} = 14.7$			(1.30)	(0.80)		
GdIn ₃	46		AF ($H < 150$ kOe)		3.07		0.096
					(0.49)		(0.29)
TbIn ₃	$T_{N1} = 32$	8.9 (at 3 K)	AF ($H < 130 \text{ kOe}$)	7.83	3.13	0.93	
	$T_{N2} = 25$		$[H_{c1} = 102, H_{c2} = 102, H_{c3} = 157, H_{c4} = 311,$	(1.60)	(0.34)	(0.19)	
			$H_{c5} = 235, H_{c6} = 398 \text{ kOe}$]				
DyIn ₃	20	8.8 (at 3 K)	AF ($H < 130$ kOe)	8.16	3.43	1.41	0.065
			$[H_{c1} = 50, H_{c2} = 115 \text{ kOe}]$	(0.88)	(0.57)	(0.57)	(0.20)
HoIn ₃	$T_{n1} = 8.2$	9.2	Para $(H > H_{c4})$	8.26	3.46	1.02	
	$T_{N2} = 7.7$	(at 1.5 K)	$[H_{c1} = 17, H_{c2} = 87, H_{c3} = 40, H_{c4} = 101 \text{ kOe}]$	(0.92)	(0.85)	(0.22)	
ErIn ₃	4.6	8.2 (at 3 K)		8.15	3.49	0.92	
			$[H_{c1} = 27, H_{c2} = 53, H_{c3} = 58 \text{ kOe}]$	(0.80)	(0.88)	(0.38)	
TmIn ₃	1.5	3.5	Para $(H > H_c)$	7.23	3.05	0.82	
		(at 1.3 K)	$[H_c = 9 \text{ kOe}]$	(0.93)	(1.12)	(0.24)	
LuIn ₃	0	0	Pauli Para	8.18	3.57	0.89	
			$\gamma = 7.5 \text{ mJ/(K}^2 \cdot \text{mol})$	(0.61)	(0.77)	(0.24)	
ScGa ₃	0	0	Pauli Para	10.55	4.41	0.94	
-				(0.75)	(0.67)	(0.31)	
LuGa ₃	0	0	Pauli Para	9.81	4.13	1.19	
-				(0.74)	(0.63)	(0.30)	

Table 5. Magnetic properties, dHvA frequency and the corresponding cyclotron mass for $H \parallel (100)$ (only branch *j* for $H \parallel (111)$) in RIn₃ [39–42,45–50], ScGa₃ and LuGa₃ [55]

CeIn₃ possesses a large electronic specific heat coefficient $\gamma = 130 \text{ mJ/(K}^2 \cdot \text{mol})$ at low temperatures, which is twenty times larger than $\gamma = 7.7 \text{ mJ/(K}^2 \cdot \text{mol})$ in LaIn₃.

We will start to explain the Fermi surface properties in RIn₃. Figure 8 shows the angular dependence of the dHvA frequency in LaIn₃ [39]. The solid lines represent the results of energy band calculation [40]. Branch a originates from the band 7-electron Fermi surface with the nearly spherical topology, while the others originate from the band 6-hole Fermi surface, as shown in Fig. 9. Here, the electronic configuration of the La atom is $[Xe]4f^05d^16s^2$, while the valence electrons of the In atom are $5s^25p^1$. The total number of valence electrons are 12 in LaIn₃. LaIn₃ is, therefore, a compensated metal with equal number of electrons and holes, or equal volume of the band 7-electron Fermi surface and the band 6-hole Fermi surface. The latter Fermi surface consists of three kinds of major parts. Among them, a Fermi surface centered at Γ , denoted by d, is electron in dispersion and is spherical in topology, bulges slightly along the (100) direction and connects with

another part of the Fermi surface centered at R by a slender arm elongated along the $\langle 111 \rangle$ direction. The arm is denoted by *j*. The topology of the Fermi surface for branch *d* is similar to that of Cu, although the volume is small compared to that of Cu. Here we note that the Γ point is a central position in the cubic Brillouin zone, and the nearly spherical band 7-electron Fermi surface is centered at the corner R point.

Conduction electrons are mainly due to La 5*d* and In 5*p* electrons. The cyclotron masses for branches *a* and *d* for $H \parallel \langle 100 \rangle$ are 0.57 m_0 and 0.40 m_0 , respectively, which are almost the same as the corresponding band masses of 0.58 m_0 and 0.53 m_0 , respectively.

Next we consider a change of the Fermi surface in the antiferromagnetic state of NdIn₃ with a Néel temperature $T_N = 5.9$ K [41,42]. The magnetic structure in the antiferromagnetic state with a magnetic wave vector q = (1/2, 0, 1/2), determined by the neutron scattering experiment, is tetragonal, as shown in Fig. 10 [43].

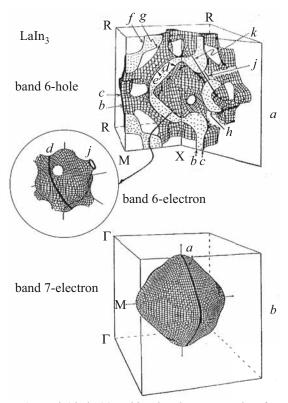


Fig. 9. Band 6-hole (*a*) and band 7-electron Fermi surfaces (*b*) in LaIn₃, cited from Refs. 39, 40.

Figure 11 shows the magnetization curve with three metamagnetic transitions at $H_{c1} = 78$, $H_{c2} = 89$ and $H_{c3} = 111$ kOe, which are indicated by the vertical broken lines [44], and the dHvA oscillation for $H \parallel (100)$. With increasing magnetic field, the compound changes from the antiferromagnetic state to a field-induced ferromagnetic (or paramagnetic) state at $H_c (= H_{c3}) = 111$ kOe, passing through the intermediate-magnetic state. The FFT spectrum in NdIn₃ is roughly the same as the one in LaIn₃ because the 4*f* electrons in NdIn₃ are localized and therefore do not contribute

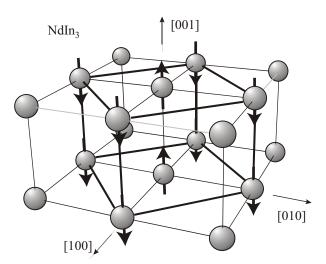


Fig. 10. Antiferromagnetic structure in NdIn₃, cited from Ref. 43. Four chemical unit cells are shown, where one magnetic unit cell is represented by thick solid lines with arrows indicating the directions of the magnetic moments.

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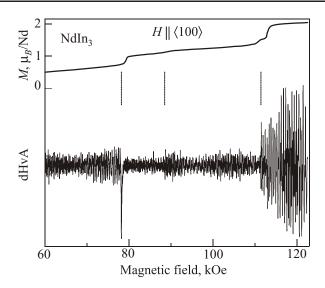


Fig. 11. Magnetization curve and the dHvA oscillation for $H \parallel \langle 100 \rangle$ in NdIn₃, cited from Refs. 41, 42, 44.

to the Fermi surface. Among the dHvA branches in the antiferromagnetic state of NdIn₃, we remark branch *a* due to the band 7-electron Fermi surface. Figure 12,*a* shows the field dependence of the dHvA frequency of branch *a*. The dHvA frequency corresponding to the up-and downspin states of the conduction electrons is degenerated in the antiferromagnetic state, and also in the intermediated-magnetic state, but is split into the up-and down-spin states in the field-induced ferromagnetic (paramagnetic) state, as shown schematically in Fig. 12,*b*.

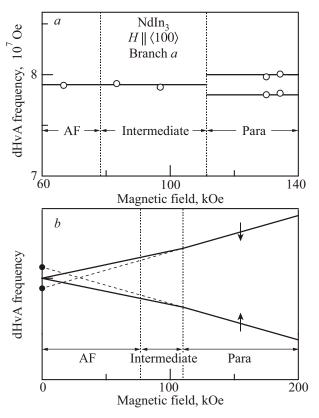


Fig. 12. Field dependence of the dHvA frequency in NdIn₃, cited from Refs. 41, 42.

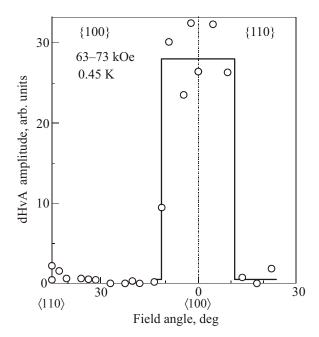


Fig. 13. Angular dependence of the dHvA amplitude for branch *a* in NdIn₃, cited from Refs. 41, 42.

It is noticed that the dHvA amplitude of branch a in the antiferromagnetic state strongly depends on the field direction, as shown in Fig. 13. It is usual in the field angle from 0° (H ||(100)) to about 10°, but is strongly reduced at angles larger than 10°. This is due to the small magnetic Brillouin zone based on the large tetragonal magnetic structure shown in Fig. 10. From the angular dependence of the dHvA amplitude for branch a, the nearly spherical electron-Fermi surface in the paramagnetic state of NdIn₃, as shown in Fig. 9,b or Fig. 14,a, which corresponds to branch a in LaIn₃, is changed into a multiply-connected Fermi surface with necks along the [110] and [110] directions in the antiferromagnetic state, as shown in Fig. 14,b. Note that no necks exist along the [100] and [010] directions. A thick solid line in Fig. 14,b corresponds to a circulating orbit a for $H \parallel [100]$. Therefore, the cubic symmetry is broken in the antiferromagnetic state. If we follow the Fermi surface in Fig. 14,b, branch a is not detectable for $H \parallel (110)$, but is experimentally detected even in the antiferromagnetic state, although its amplitude is extremely small, as shown in Fig. 13. This is because an electron can circulate along a closed orbit by breaking through the necks of the Fermi surface. The antiferromagnetic Fermi surface in the 4f-localized antiferromagnet NdIn₃ is thus reconstructed on the basis of the magnetic Brillouin zone. The angular dependence of the dHvA frequency in the antiferromagnetic state and the paramagnetic state is shown later in Figs. 21,d and 21,e, respectively, where the other Fermi surface properties in RIn3 are also shown in Fig. 21 [39-42,45-50].

The dHvA experiments of RIn₃ (R: Sm to Tm) were done in the antiferromagnetic state, while some RIn₃ (R: Ho, Er, Tm) compounds were done in the paramagnetic (field-

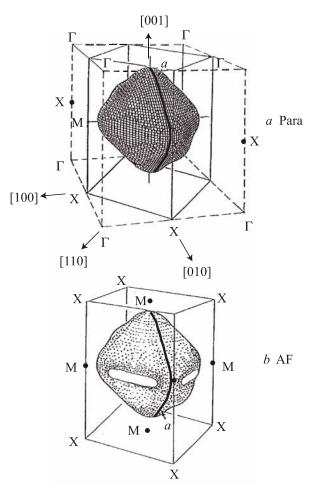


Fig. 14. Fermi surfaces in the paramagnetic state (a) and the antiferromagnetic state (b) in NdIn₃, cited from Refs. 41, 42.

induced ferromagnetic) states, where the corresponding critical field H_c was about 100 kOe or less than 100 kOe, as in NdIn₃. PrIn₃ was in the paramagnetic state with the singlet state in the 4*f*-CEF scheme [46]. These are summarized in Table 5 [39–42,45–50].

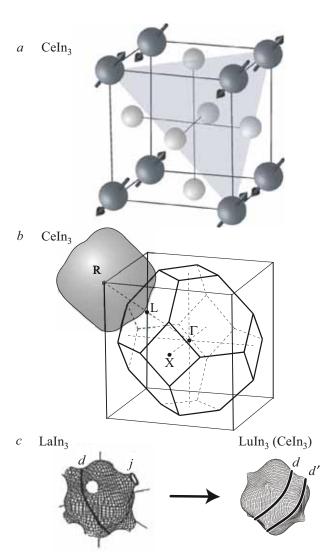
The similar change of the electronic state based on the magnetic structure is also realized in a Kondo-lattice compound CeIn₃ with antiferromagnetic ordering at $T_N = 10$ K, where ordered moments of 0.65 μ_B /Ce with the propagation vector q = (1/2, 1/2, 1/2) are aligned along the (111) direction as shown in Fig. 15,*a* [35–37]. The angular dependence of the dHvA frequency in CeIn₃ is later shown in Fig. 21,*b* [45,51].

The detected dHvA named d in CeIn₃ is very close to the one in LaIn₃. Branch d in CeIn₃ is, however, observed in the whole angle region, possessing no arms, indicating that the Fermi surface is a nearly spherical Fermi surface with humps. It is noted that there exist no necks in another non-4f (4 f^{14}) reference compound LuIn₃ [49]. The neck in LaIn₃ is changed into a hump in LuIn₃ and CeIn₃, as shown in Fig. 15,c.

The cyclotron mass of branch d in CeIn₃ is strongly field-dependent, ranging from 2.3 to $16m_0$, as shown in Fig. 16,*a*, which brings about a drastic change of the dHvA

amplitude for the magnetic field direction from $\langle 100 \rangle$ to $\langle 110 \rangle$, as shown in Fig. 16,*b*. This is due to the spin factor in Eq. (10). From the large cyclotron mass of the branch *d* for *H* || $\langle 110 \rangle$, it is suggested that the electronic state on the hump corresponds to the heavy fermion state. Namely, the heavy electronic state exists locally in the Fermi surface. The orbit for the magnetic field along $\langle 110 \rangle$ passes four times on the hump for one cycle of an orbit. On the other hand, the orbit for the magnetic field along $\langle 100 \rangle$ does not pass on the hump. The hump is nowadays called "hot spot" [52].

Next we consider the meaning of a heavy fermion state. The conduction electron with a large cyclotron mass is believed to move slowly in the crystal [53]. We confirmed experimentally that the product of the cyclotron mass and the inverse scattering lifetime or the Dingle temperature $m_c^* \tau^{-1}$ or $m_c^* T_D$ is constant by using two orbits of the Fermi surface named *d* in CeIn₃. As mentioned in Chap. 2, the following equation is obtained:



 $\frac{m_c^*}{\tau} = \frac{\hbar k_F}{\ell} \,. \tag{14}$

Thus, m_c^*/τ is expected to be the same for two similar orbits with the same mean free path. When the effective mass m_c^* is enhanced by a factor of $(1 + \lambda)$ by the many-body Kondo effect, τ should also be enhanced by a factor $(1 + \lambda)$. This occurs because a large cyclotron mass is translated into a small velocity from the equation of $\hbar k_F = m_c^* v_F$ so that the scattering lifetime is enhanced by $(1 + \lambda)$ from the equation of $\ell = v_F \tau$ if the mean free path ℓ is the same between two orbits. In terms of the Dingle temperature, Eq. (12) becomes

$$m_c^* T_D = \frac{\hbar^2 k_F}{2\pi k_B \ell}.$$
 (15)

The above relation between the cyclotron mass and the Dingle temperature was applied to the nearly spherical Fermi surface *d*. The dHvA frequency *F*, the cyclotron mass m_c^*

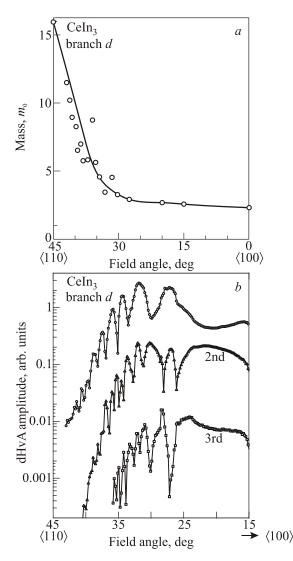


Fig. 15. Crystal and magnetic structure in CeIn₃ (*a*), the corresponding magnetic Brillouin zone of CeIn₃ and a band 7-electron Fermi surface (*b*), and Fermi surfaces named *d* in LaIn₃ and LuIn₃ (CeIn₃) (*c*), cited from Refs. 38, 49.

Fig. 16. Angular dependence of the cyclotron mass of the branch d(a) and the corresponding dHvA amplitude for the fundamental, 2nd and 3rd harmonics in the field range of 70 to 90 kOe at 0.45 K in CeIn₃, cited from Ref. 51 (*b*).

and the Dingle temperature T_D are $3.15 \cdot 10^7$ Oe, $2.44 m_0$ and $T_D = 0.19$ K for $H \parallel \langle 111 \rangle$, and $3.29 \cdot 10^7$ Oe, $12 m_0$ and $T_D = 0.04$ K for the field direction close the $\langle 110 \rangle$ direction, indicating that the product of $m_c^* T_D$ is constant for the two orbits. We can thus concluded that the larger the cyclotron mass becomes the larger the scattering lifetime is, so that the value of $m_c^* \tau^{-1}$ or $m_c^* T_D$ is constant.

Branch a of band 7-electron Fermi surface in Fig. 15,b was, however, not detected in CeIn3, which is ascribed to the reconstruction of the Fermi surface on the basis of the antiferromagnetic Brillouin zone. This Brillouin zone is the same as that for the face-centered cubic structure, as shown in Fig. 15,b. Most of the band 7-electron Fermi surface centered at the R point is changed into a fully occupied band in this new Brillouin zone, where the original R point is reduced to the Γ point in this Brillouin zone. The antiferromagnetic ordering of CeIn3 is very robust against the magnetic field. The antiferromagnetic phase diagram of T_N vs H_c is obtained as follows: $T_N \sim [1 - (H/H_c)^2]$ and the metamagnetic field from the antiferromagnetic state to the paramagnetic state $H_c \simeq 610$ kOe for $T_N \rightarrow 0$ [52]. At high magnetic fields larger than H_c , namely in the paramagnetic state, branch *a* was observed: $F = 7.9 \cdot 10^7$ Oe and $m^* =$ = $6 m_0$ for $H \parallel \langle 110 \rangle$ [54]. The present dHvA frequency is slightly larger than $7.47 \cdot 10^7$ Oe in LaIn₃ [39] and is close to 8.13.10⁷ Oe in YIn₃ [55] or 8.18.10⁷ Oe in LuIn₃ [49].

A drastic change of the Fermi surface in an antiferromagnetic Kondo compound $CeIn_3$ is realized under pressure [38], which will be shown later in Chap. 6.

YbIn₃ in Fig. 7,*b* is a Pauli paramagnet with the divalent property of Yb²⁺ [32]. The electronic configuration of the Yb atom is $[Xe]4f^{14}6s^2$, and thus the valence electrons are $6s^2$. Considering the valence electrons of $5s^25p^1$ in the In atom, the total number of valence electrons are 11 in YbIn₃, revealing an uncompensated metal. Figure 17 shows the angular dependence of the dHvA frequency in YbIn₃ [49].

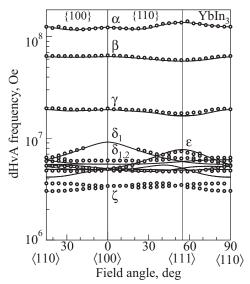


Fig. 17. Angular dependence of the dHvA frequency in a Pauli paramagnet YbIn₃. The solid lines are the results of energy band calculation, cited from Ref. 49.

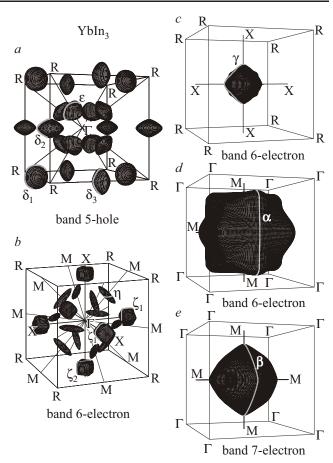


Fig. 18. Theoretical Fermi surfaces in a Pauli paramagnet YbIn₃, cited from Ref. 49.

The solid lines in Fig. 17 indicate the results of energy band calculation. The experimental results of dHvA branches named α , β , γ , δ_i and ε are in good agreement with the theoretical ones, as shown in Fig. 18, which are the band 6-electron Fermi surface centered at R, the band 7-electron Fermi surface centered at R, the band 6-electron Fermi surface centered at Γ , the band 5-hole Fermi surface centered at M and band 5-hole located along Λ , respectively.

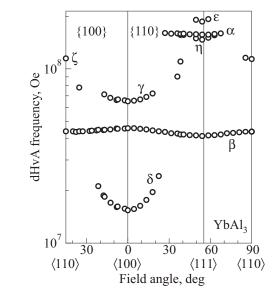


Fig. 19. Angular dependence of the dHvA frequency in YbAl₃ [56].

Branch ζ_i also corresponds to the band 6-electron Fermi surface. The cyclotron mass is light and is close to the corresponding band mass m_b , ranging from $1.1 m_0$ in branch α to $0.22 m_0$ in branch ζ_i .

Here we note the 4*f*-electron character in Yb compounds. The 4*f* electrons of YbAl₃ and YbCu₂Si₂, for example, possess the localized moment at high temperatures, with Yb³⁺ with an electron configuration of $[Xe]4f^{13}5d^{1}6s^{2}$, where the $5d^{1}6s^{2}$ electrons become the valence electrons. The Fermi surface is thus similar to that of a non-4*f* reference La compound or the corresponding Lu compound with an electron configuration of $[Xe]4f^{14}5d^{1}6s^{2}$ (Lu³⁺). The 4*f* electrons, however, become itinerant at low temperatures, via the many-body Kondo effect. The corresponding temperatures are $T_{\chi max} = 120$ K in YbAl₃ and $T_{\chi max} = 40$ K in YbCu₂Si₂, below which the magnetic susceptibility becomes approximately constant. The 4*f* electrons at temperatures lower than $T_{\chi max}$ contribute to the Fermi surface, and therefore the corresponding topology of the Fermi surface is highly different from the Fermi surface with the Yb³⁺ configuration. The 4*f*itinerant Fermi surfaces of YbAl₃ and YbCu₂Si₂ are, however, very similar to the corresponding Yb²⁺ compounds, namely YbIn₃ and YbCu₂Ge₂, respectively. A careful comparison of the dHvA result with the result of energy band calculations is therefore necessary for a better understanding of the Fermi surface in YbAl₃ [56] and YbCu₂Si₂ [57].

Figure 19 shows the angular dependence of the dHvA frequency in YbAl₃ [56]. One of the six dHvA branches, named β with a dHvA frequency of $4.5 \cdot 10^7$ Oe, is nearly spherical in topology and has a large cyclotron mass of $24m_0$. The other branches are in the range $14-17m_0$. The topology of the Fermi surface cannot be explained by the conventional band calculations, as shown in Figs. 20,a,b, because the fully occupied 4f-levels in YbAl₃ are below the Fermi surface of YbAl₃ in Fig. 20,b is similar to that of YbIn₃ in Fig. 18.

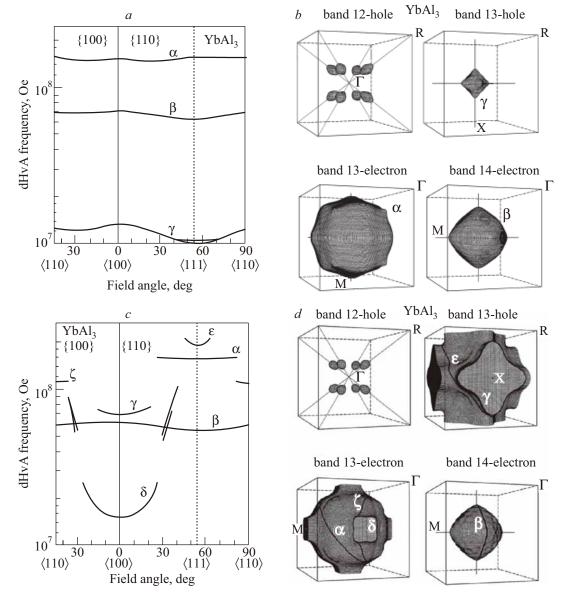


Fig. 20. Angular dependence of the dHvA frequency (*a*) and the corresponding Fermi surfaces based on the conventional band model (*b*); the angular dependence of the dHvA frequency (*c*) and the corresponding modified Fermi surfaces in YbAl₃ (*d*), cited from Ref. 56.

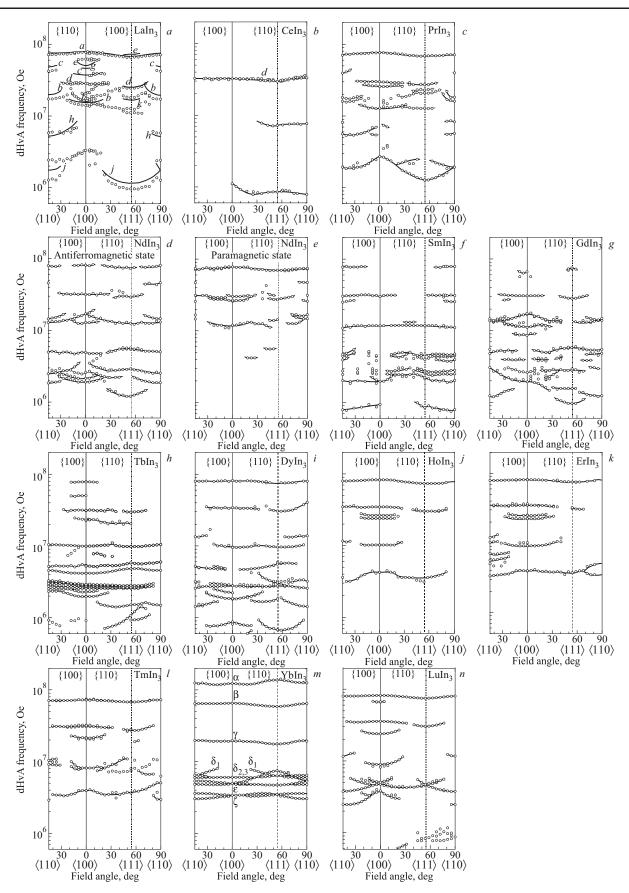


Fig. 21. Angular dependence of the dHvA frequency in RIn₃ (R = La [39], Ce [45], Pr [46], Nd [41], Sm [47], Gd [48], Tb, Dy, Ho, Er, Tm, Yb [49], and Lu [49]). Solid lines in LaIn₃ are the results of energy band calculations [40], while the other solid lines connecting the data are guide lines.

A small alteration so as to shift upward the 4f-levels by 200 mRy is therefore necessary to fit the experimental dHvA data. Thus obtained angular dependence of the dHvA frequency and Fermi surfaces are shown in Figs. 20, c and 20, d, respectively. A nearly spherical Fermi surface of branch α is changed into a multiply-connected Fermi surface whose arms are directed along the (100) direction, which is brought about by disappearance of the Fermi surface named γ in Fig. 20, b. Branches α , γ , δ , ε and ζ in Fig. 19 are well explained by this modified Fermi surface. Such shifting of the 4f-levels affects the Fermi surface because the 4f electrons directly contribute to the conduction electrons. This effect also plays an important role in the mass enhancement, which is caused by the manybody Kondo effect. The similar modification is necessary for YbCu₂Si₂ [57], as well as YbT₂Zn₂₀ (T: Co, Rh, Ir) shown in Chap. 6.

We summarize in Fig. 21 and Table 5 the Fermi surface properties of RIn₃ (R: Y, La-Lu), ScGa₃ and LuGa₃. Main branches a, d, and b are observed in almost all of RIn₃. Almost the same Fermi surface properties are also observed in YIn₃, ScGa₃ and LuGa₃ [55] in Table 5.

The present results are summarized as follows. The magnetic energy gaps associated with the antiferromagnetic ordering are small enough and thus the electrons undergoing cyclotron motions can break through these energy gaps and circulate on orbits of the paramagnetic Fermi surface. The occurrence of this effect, however, becomes more difficult as the number of f electrons increases. In that case, the electrons follow the orbits on the antiferromagnetic Fermi surface, which was constructed in a small Brillouin zone based on the magnetic unit cell larger than the chemical unit cell in volume. The typical example is NdIn₃. The paramagnetic (or field-induced ferromagnetic) Fermi surface of NdIn₃ is almost the same as that of LaIn₃. A nearly spherical Fermi surface in the paramagnetic state, which corresponds to branch a of the band 7-electron Fermi surface of LaIn₃, is changed into a multiply-connected one with necks in the antiferromagnetic state.

On the other hand, if a Fermi surface is small and is located in the center of the Brillouin zone, it remains in the antiferromagnetic state because it is contained in the magnetic Brillouin zone. Branch d in LaIn₃ is observed in the magnetic RIn₃ compounds. Moreover, mass enhancement due to the electron–magnon interaction in magnetically ordered compounds is large compared with the one due to the electron–phone interaction. The mass enhancement factor in RIn₃ is in the range of 1–2. An exceptional case is CeIn₃. The mass enhancement is extremely large and anisotropic for the field direction in CeIn₃.

4. Fermi surface properties in RX3 and AnX3

The cubic RX_3 (X: Al, Ga, In, Si, Ge, Sn, Pb) and AnX_3 (An: actinide) compounds are classified in Table 6 according to the

number of valence electrons, *n*, from n = 11 in a divalent Yb²⁺ compound YbIn₃ to n = 19 in a 5*f* relevant paramagnet NpGe₃, passing through a non-4*f* reference compound LaIn₃ (LuIn₃), a Kondo-lattice compound with antiferromagnetic ordering CeIn₃, CeIn₃ under pressure, a non-5*f* reference compound ThIn₃, a divalent Yb²⁺ compounds YbSn₃ and YbPb₃, non-4*f* reference compounds LaSn₃ and LaPb₃, an antiferroquadrupolar compound PrPb₃, a heavy fermion compound UAl₃, antiferromagnets UGa₃ and UIn₃, a 4*f*-itinerant compound CeSn₃, an antiferromagnet NpIn₃ which is close to LaIn₃ in topology of the Fermi surface and is classified in the compounds with n = 12, a paramagnet PuIn₃, Pauli paramagnets USi₃ and UGe₃, a spin-fluctuation compound USn₃, and a paramagnet NpGe₃ [58–71].

Table 6. Numbers of valence electrons and Fermi surface studies in the RX_3 and AnX_3 compounds with the AuCu₃-type cubic crystal structure

Number of va-	Compounds	Refs.
lence electrons	_	
11	YbIn ₃ (P)	[49]
	YbAl ₃ (P)	[56]
12	LaIn ₃ (P)	[39]
	$LuIn_3(P)$	[49]
	NdIn ₃ (AF)	[41,42]
	CeIn ₃ (AF)	[45]
	NpIn ₃ (AF)	[58]
13	CeIn ₃ under pressure (P, S)	[38]
	$ThIn_{3}(P)$	[59]
14	YbSn ₃ (P)	[60]
	YbPb ₃ (P)	[61]
15	LaSn ₃ (P)	[62]
	$LaPb_{3}(P)$	[63]
	$PrPb_3(Q)$	[63]
	$UAl_3(P)$	[64]
	UGa ₃ (AF)	[65]
	UIn ₃ (AF)	[66]
16	$CeSn_3(P)$	[67]
17	$PuIn_3(P)$	[68]
18	$USi_3(P)$	[69]
	$UGe_3(P)$	[70]
	$USn_3(P)$	
19	$NpGe_3(P)$	[71]

The compounds with the number of valence electrons, n = 11 and 12 are explained in Chap. 3. The Fermi surface properties of CeIn₃ under pressure and ThIn₃ will be explained in Chap. 7. We will start from the compounds with the number of valence electrons, n = 14, namely Pauli paramagnets YbSn₃ and YbPb₃ because Yb is divalent and the valence electrons in Sn and Yb are $5s^25p^2$ and $6s^2$, respectively [60,61]. Figure 22 indicates the angular dependence of the dHvA frequency in YbPb₃. The detected three branches named α , ε and φ are explained by the result of energy band calculation of which the Fermi surface is shown in Fig. 23. Here, the Fermi surface consists of a band 7-hole Fermi surface named α and band 8-electron Fermi surfaces named ε and φ , indicating a compensated metal as in LaIn₃ (n = 12) [39]. The similar dHvA data and

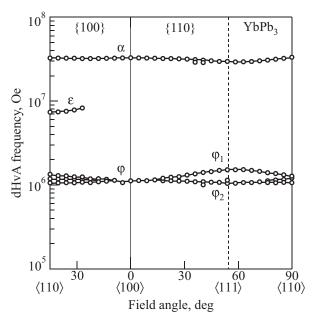


Fig. 22. Angular dependence of the dHvA frequency in a Pauli paramagnet YbPb₃, cited from Ref. 61.

the corresponding Fermi surfaces are obtained in YbSn₃ [60].

Next we show in Fig. 24,*a* the angular dependence of the dHvA frequency in LaSn₃ [62]. Main characteristic dHvA branches are as follows. Two branches named α and β exist in the whole range of angles, revealing two nearly spherical Fermi surfaces, three branches named γ_1 , γ_2 and γ_3 are centered at (111), and branch δ is centered at (110).

Compared with LaIn₃, LaSn₃ has three electrons more per primitive cell, and hence the electronic structure of LaSn₃ is that of an uncompensated metal. All the sheets of the Fermi surface in LaIn₃ disappear in LaSn₃. In LaSn₃,

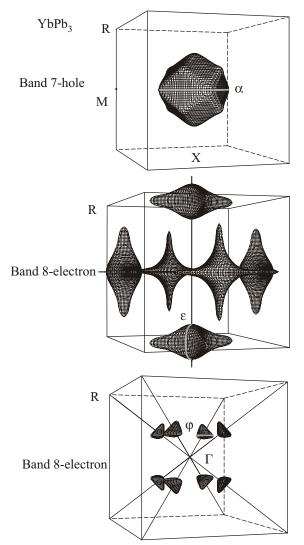


Fig. 23. Fermi surfaces in a Pauli paramagnet YbPb₃, cited from Ref. 61.

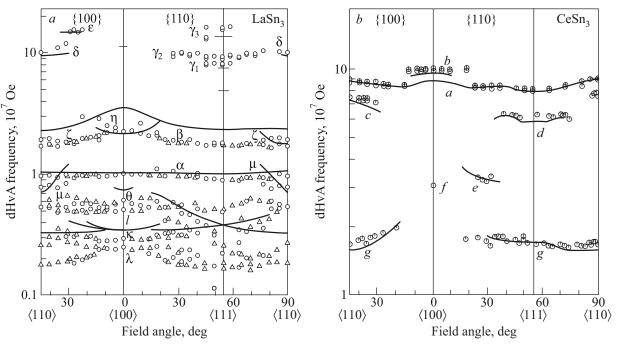


Fig. 24. Angular dependence of the dHvA frequency in a non-4*f* reference compound LaSn₃ (*a*) and a 4*f*-itinerant CeSn₃ (*b*), cited from Refs. 62, 67, 72, 73. Solid lines are the results of energy band calculation.
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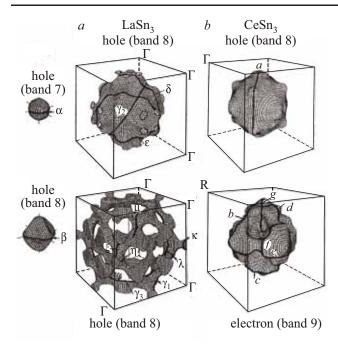


Fig. 25. Fermi surface of $LaSn_3$ (*a*) and $CeSn_3$ (*b*), cited from Refs. 72, 73.

band 8 yields a main Fermi surface centered at R, and two small hole closed Fermi surfaces exist at Γ in bands 7 and 8, as shown in Fig. 25,*a*. The solid lines in Fig. 24,*a* are the result of energy band calculation [72]. The detected dHvA branches are well explained on the basis of the Fermi surface in Fig. 25,*a*.

CeSn₃ at low temperatures is a so-called valence-fluctuation compound with a Kondo temperature of about 150 K where the magnetic susceptibility possesses a maximum at about 150 K, as shown in Fig. 2. It is interesting to understand the 4*f*-electron character in comparison with the antiferromagnetic Kondo compound CeIn₃. Figure 24,*b* shows the angular dependence of the dHvA frequency in CeSn₃ [67]. Some dHvA branches are similar to those of LaSn₃ but the other branches are considerably different from those of LaSn₃. The detected cyclotron masses are roughly five times larger than those of LaSn₃: $4.2 m_0$ for branch *a* in CeSn₃ and $0.91 m_0$ for branch γ_2 in LaSn₃, in agreement with γ values: 53 mJ/(K²·mol) in CeSn₃ and 11 mJ/(K²·mol)in LaSn₃.

The energy band calculation was carried out under the assumption that the 4f electron is itinerant [73]. The calculated Fermi surfaces mainly consist of a large band 8-hole Fermi surface centered at R and a large band 9-electron Fermi surface centered at Γ . The origin of the analogy in Fermi surfaces between CeSn₃ and LaSn₃ is as follows. Namely, the large distorted spherical band 8-hole Fermi surface in LaSn₃ is similar to the band 8-hole Fermi surface in CeSn₃. Small nearly spherical hole Fermi surfaces in bands 7 and 8, denoted by α and β in LaSn₃, are also present in CeSn₃, not shown in Fig. 24,b and Fig. 25,b, although their volumes of the Fermi surfaces in CeSn₃ are smaller than those of LaSn₃. The marked difference between LaSn₃ and CeSn₃ is ascribed to a large band 9electron Fermi surface in CeSn₃. Note that this Fermi surface has no occupied states along $\langle 111 \rangle$.

The solid lines in Fig. 24,*b* indicate the result of the 4*f*itinerant energy band calculation [73]. Branch *a* corresponds to the large hole-Fermi surface, while the other main branches are due to the electron Fermi surface, indicating a compensated metal. Both in the magnitude of the crosssectional area and in the observed range of field angle, the 4*f*-itinerant band model agrees reasonably well with the experimental results. The reason for the disappearance of branch *a* at angles in the vicinity of the $\langle 100 \rangle$ direction is due to the combined effect of a curvature factor and a relatively large cyclotron mass.

We will go on to the next compound n = 15, LaPb₃ [63]. LaPb₃ should be very similar to LaSn₃, with n = 15,

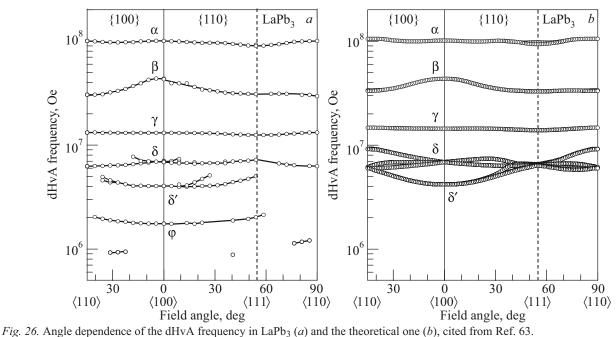


Fig. 20. Angle dependence of the drive nequency in Ear 03(a) and the theoretical one (b), ched in

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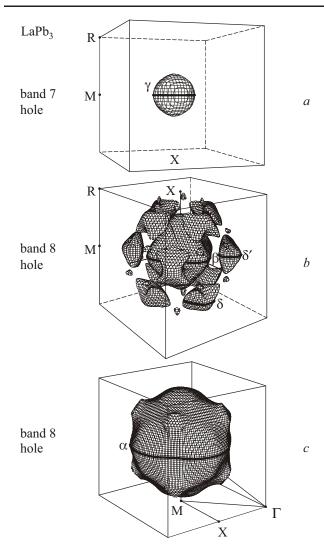


Fig. 27. Fermi surfaces in LaPb₃, cited from Ref. 63.

although the Fermi surface of LaPb₃ is slightly different and simple compared with that of LaSn₃. It is, however, noted that branches γ_2 , δ , β , and α in LaSn₃, shown in Fig. 24,*a*, correspond to branches α , β , and γ in LaPb₃, respectively, as shown in Fig. 26,*a*. Figures 26,*a* and 26,*b* show the angular dependence of the dHvA frequency and the result of energy band calculations, respectively, in LaPb₃. Main three branches named α , β , and γ are closed Fermi surfaces, which are well explained by the energy band calculations of which the Fermi surfaces are shown in Fig. 27.

The angular dependence of the dHvA frequency in an antiferroquadrupolar compound PrPb₃ with $T_Q = 0.4$ K is approximately the same as that in LaPb₃ [63]. It is interesting that the cyclotron mass of PrPb₃ is strongly enhanced below 0.7 K, as shown in Fig. 28: $1.6m_0$ at 1.3 K and $4.0m_0$ at 0.18 K for branch γ . The corresponding cyclotron mass is 0.38 m_0 in LaPb₃ and 0.94 m_0 in an antiferromagnet NdPb₃. The mass enhancement in PrPb₃ might be ascribed to the quadrupolar ordering.

We will go on to another compounds with the number of valence electrons, n = 15, namely UAl₃, where the va-

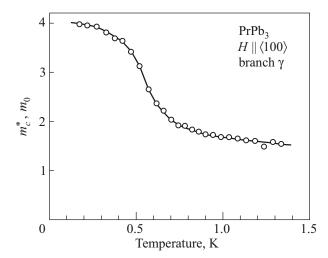


Fig. 28. Temperature dependence of the cyclotron mass in PrPb₃, cited from Ref. 63.

lence electrons are [Rn] $5f^{3}6d^{1}7s^{2}$ in the U atom and $3s^{2}3p^{1}$ in the Al atom. The topology of the Fermi surface in UAl₃ should be similar to that in LaPb₃, although the 5*f* contribution to the Fermi surface in UAl₃ might change the topology of the Fermi surface and also the mass enhancement. UAl₃ does not order magnetically, and the magnetic susceptibility possesses a broad maximum around $T_{Xmax} \approx$ ≈ 140 K, as shown in Fig. 29. At higher temperatures up to 800 K, not shown in Fig. 29, the susceptibility follows the Curie–Weiss law [74]. The obtained effective magnetic moment $\mu_{eff} = 3.6 \ \mu_{B}/U$ is close to $3.62 \ (3.58) \ \mu_{B}/U$ in the 5*f*-localized $5f^{3} \ (5f^{2})$ configuration. This is a reason why UAl₃ is characterized as a spin-fluctuating compound. The crossover from 5*f*-localized to 5*f*-itinerant is supposed to

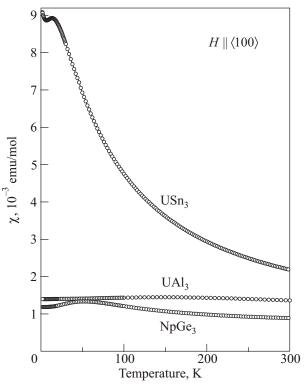


Fig. 29. Temperature dependence of the magnetic susceptibility in USn₃, UAl₃ and NpGe₃, cited from Ref. 74.

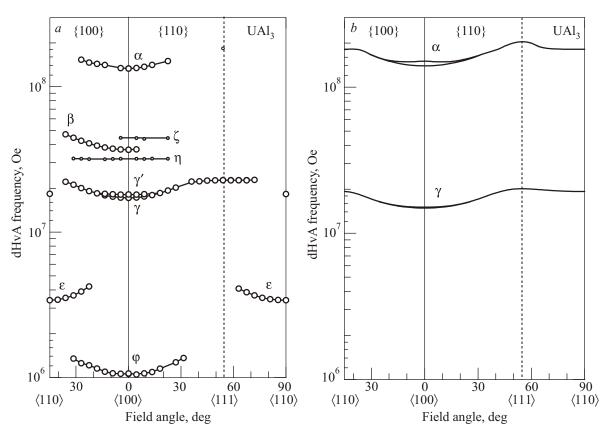


Fig. 30. Angular dependence of the dHvA frequency in a heavy fermion compound UAl₃ (a) and the theoretical one (b), cited from Ref. 64.

occur below $T_{\chi max} \simeq 140$ K. It is thus important to clarify the 5*f*-electron character from the dHvA experiment and energy band calculation. Here it is noted that the valencefluctuating compound mentioned for CeSn₃ corresponds to the spin-fluctuating compound. The former was named for Ce and Yb compounds with a relatively large T_K value, say, $T_K = 50-150$ K, while the latter for the similar U compounds. Both compounds become the enhanced Pauli paramagnets at low temperatures.

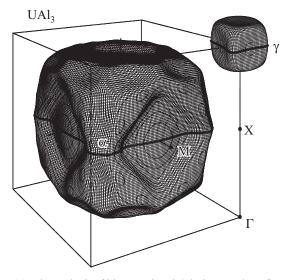


Fig. 31. Theoretical 5*f*-itinerant band 8-hole Fermi surfaces in UAl₃, cited from Ref. 64.

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Figures 30,*a* and 30,*b* show the angular dependence of the dHvA frequency and the theoretical one based on the 5*f*-itinerant band model, respectively for UAl₃ [64]. Among the detected several branches, two main branches named α and γ are well explained by the theoretical closed band 8-hole Fermi surfaces, as shown in Fig. 31.

One large Fermi surface is nearly cubic, centered at Γ , and the other small Fermi surface is also nearly cubic, centered at R. The detected cyclotron mass is relatively large, ranging from 3 to $17m_0$, which is twice to three times larger than the corresponding band mass: $m_c^* = 17m_0$ and $m_b = 6m_0$ for branch α for $H \parallel \langle 100 \rangle$, and $\gamma = 47 \text{ mJ/(K}^2 \cdot \text{mol})$ and the theoretical value $\gamma_b = 14.8 \text{ mJ/(K}^2 \cdot \text{mol})$.

UGa₃ and UIn₃ are the compounds with n = 15, similar to UAl₃. Both compounds, however, order antiferromagnetically below $T_N = 67$ and 90 K, respectively. UGa₃ was studied on the basis of the 5*f*-itinerant antiferromagnet [75], but the detected dHvA branches in UGa₃ are not explained by the spin-polarized 5*f*-itinerant band model, which is most likely due to the magnetic structure, not definitely determined yet in experiments. Here we show in Figs. 32 and 33 the angular dependence of the dHvA frequency in UGa₃ [65] and UIn₃ [66], respectively.

The compound with the number of electrons, n = 17, corresponds to PuIn₃, as shown in Table 6. It is, however, better to present the corresponding Fermi surface property as a final compound in RX₃ and AnX₃. We will go on to USi₃ with n = 18. USi₃ is a Pauli paramagnet with a small

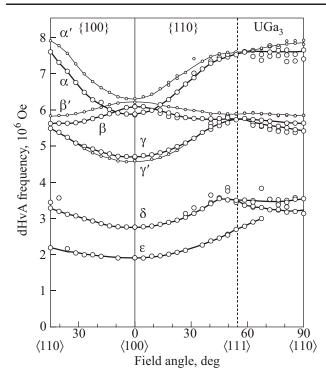


Fig. 32. Angular dependence of the dHvA frequency in an antiferromagnet UGa₃, cited from Ref. 65.

 γ value of 11.9 mJ/(K²·mol). Figures 34,*a* and 34,*b* show the angular dependence of the dHvA frequency and the corresponding theoretical one based on the 5*f*-itinerant band model, respectively [69]. Fifteen dHvA branches are observed, ranging from 7.37·10⁶ to 2.33·10⁸ Oe, which are

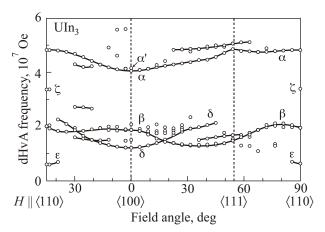


Fig. 33. Angular dependence of the dHvA frequency in an antiferromagnet UIn₃, cited from Ref. 66.

in good agreement with the theoretical ones based on the 5*f*-itinerant Fermi surfaces shown in Fig. 35. Theoretically, the 5*f* electrons form wide bands across the Fermi energy, which hybridize considerably with Si-3*p* electrons. The *p*–*f* hybridization makes the dispersion of the 5*f*-bands very large. Cyclotron masses, which are in the range from 0.39 to 4.17 *m*₀, are thus approximately the same as the corresponding band masses, being in good agreement with a relation between the γ value of 11.9 mJ/(K²·mol) and $\gamma_b = 11.7$ mJ/(K²·mol). The mass enhancement is thus extremely small in USi₃.

A small mass enhancement is observed in UGe₃ with $\gamma = 20 \text{ mJ/(K}^2 \cdot \text{mol})$, with the same topology of the Fermi surface as in USi₃, from the dHvA experiment and energy

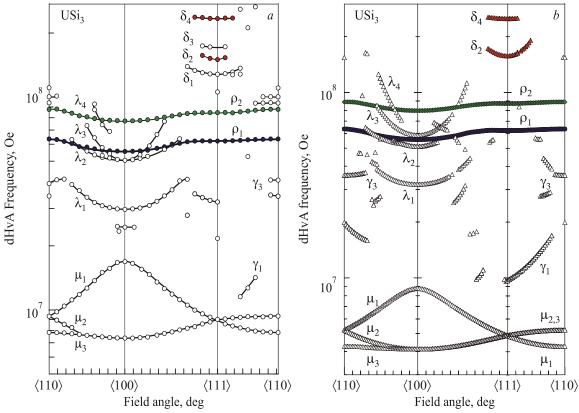


Fig. 34. Angular dependence of the dHvA frequency in a Pauli paramagnet USi3 (a) and the theoretical one (b), cited from Ref. 69.

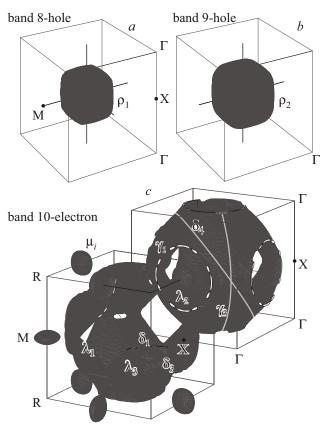


Fig. 35. Theoretical 5*f*-itinerant Fermi surfaces in USi₃, cited from Ref. 69.

band calculation [70], while a relatively large mass enhancement is expected in a spin-fluctuating compound USn₃ with $\gamma = 170 \text{ mJ/(K}^2 \cdot \text{mol})$, as shown in Fig. 1,*b*. Here, the Doniach phase diagram in Fig. 1,*a* is expressed by a relation of the distance between the U atoms, a vs the γ value. Correspondingly, the low-temperature magnetic susceptibility is large, as shown in Fig. 29.

Figure 36 shows the angular dependence of the dHvA frequency in USn₃. Only branches μ_i are observed. The cyclotron mass of branches $\mu_{2,3}$ for $H \parallel \langle 100 \rangle$ is $1.5 m_0$ in USn₃, which is large compared with $0.40 m_0$ in USi₃ and $0.42 m_0$ in UGe₃.

The next compound is NpGe₃ with n = 19 [71]. This is an enhanced Pauli paramagnet, similar to UAl₃. The mag-

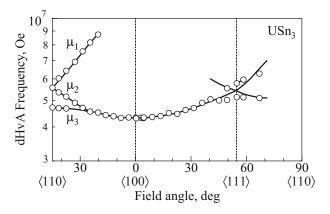


Fig. 36. Angular dependence of the dHvA frequency in a spin-fluctuation compound USn₃.

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netic susceptibility has a maximum around 50 K, as shown in Fig. 29. From the susceptibility data above 250 K, the estimated effective magnetic moment is $\mu_{eff} = 2.78 \ \mu_B/\text{Np}$, which is close to $\mu_{eff} = 2.68 \ \mu_B/\text{Np}$ in Np^{3+} (5 f^4), but is smaller than $\mu_{eff} = 3.62 \ \mu_B/\text{Np}$ in Np^{4+} (5 f^3). The present result of the magnetic susceptibility suggests that the Np ion possesses a local moment at high temperatures, but the electronic state is changed into the enhanced Pauli paramagnet at temperatures lower than 50 K.

Figures 37,*a* and 37,*b* show the angular dependence of the dHvA frequency and the corresponding one based on the 5*f*-itinerant Fermi surfaces shown in Fig. 38, being in good agreement between experiment and theory [71]. The band 10-electron Fermi surface in USi₃ (UGe₃), shown in Fig. 35,*c*, is spherical, but possesses a hollow space at the center and a window for (100), with a flat closed Fermi surface at the M point. One more 5*f* electron becomes a valence electron in NpGe₃. This means that the hole bands (8 and 9) are occupied completely by the electron and also the band 10-electron Fermi surface, centered at R, is partially occupied by the remaining electron, producing a hollow ball with a "belly" orbit and a "neck", as shown in

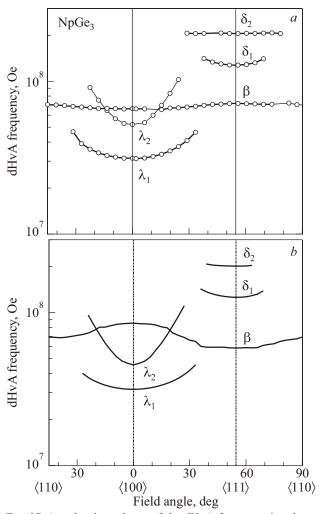


Fig. 37. Angular dependence of the dHvA frequency in a heavy fermion compound NpGe₃ (a) and the theoretical one (b), cited from Ref. 71.

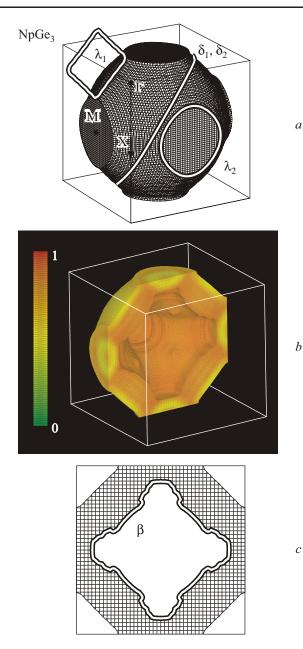


Fig. 38. (Color online) Theoretical 5*f*-itinerant Fermi surfaces and cross-sections in NpGe₃. The color presents the contribution of 5*f*-electrons, cited from Ref. 71.

Fig. 38. The cyclotron mass is in the range of 2.6 to $16 m_0$, which is enhanced approximately 3.5 times from the corresponding band mass. This is in fairly good agreement with the ratio of $\gamma = 34 \text{ mJ/(K}^2 \cdot \text{mol})$ to the theoretical one $\gamma_b = 16.8 \text{ mJ/(K}^2 \cdot \text{mol})$, $\gamma/\gamma_b = 2.0$. It is noted that the cyclotron mass and the corresponding band mass for an outer "belly" orbit δ_2 are $m_c^* = 4.7 m_0$ and $m_b = 1.35 m_0$, respectively, which are compared with $m_c^* = 15 m_0$ and $m_b = 4.03 m_0$ for an inner orbit β . This is because the inner part of the band 10-electron Fermi surface is mainly due to the contribution of 5f electrons in Np, while the outer part is due to the 4p component of Ge.

Next we discuss the electronic state of a complicated magnetic compound NpIn₃ [58]. Ferromagnetic and anti-

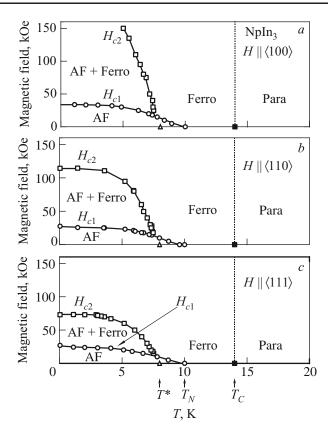


Fig. 39. Magnetic phase diagram in an antiferromagnet NpIn₃, cited from Ref. 58.

ferromagnetic orderings occur at $T_C = 14$ K and $T_N = 10$ K, respectively, together with another transition at $T^* = 8$ K. When the magnetic field is applied to the sample, the antiferromagnetic state is finally changed into a ferromagnetic state with two metamagnetic transitions at H_{c1} and H_{c2} . The antiferromagnetic ordering and two metamagnetic transitions are found to be of the first-order phase transition. We show in Fig. 39 the magnetic phase diagram for three principal directions [58]. All the dHvA signals are detected in the ferromagnetic state, namely above H_{c2} .

Figure 40 shows the angular dependence of the dHvA frequency [58]. Since the ferromagnetic state is not realized at the highest magnetic field of 150 kOe for the magnetic field around the (100) direction, as shown in Fig. 39, no dHvA signals are observed around (100). They should be observed in magnetic fields higher than $H_{c2} \simeq 200$ kOe for $H \parallel$ (100). Three dHvA branches named α , β and γ are observed. Branches α and β correspond to nearly spherical Fermi surfaces. The dHvA frequency of branch γ increases with increasing the field angle from (100) to (110) or (111). At 31° (to (110) and 36° (to (111)), branch γ abruptly disappears, suggesting the open orbit, which is most likely due to a multiply-connected Fermi surface.

From the present dHvA results, we constructed the Fermi surface of NpIn₃ with n = 16. Two cases can be considered. The one is the case based on the 5*f*-itinerant picture. Another is the case based on the 5*f*-localized picture. In the case of 5*f*-itinerant picture, the total number of va-

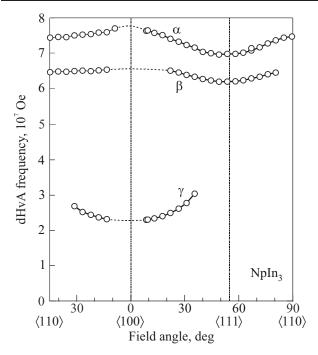


Fig. 40. Angular dependence of the dHvA frequency in an antiferromagnet NpIn₃, cited from Ref. 58.

lence electrons in NpIn₃ is even, namely 16, where the electronic configurations are Np $(5f^4 6d^17s^2)$ and In $(5s^25p^1)$. This means that NpIn₃ is a compensated metal with equal carrier numbers of electrons and holes.

In the case of 5*f*-localized picture, the Np³⁺ (5*f*⁴) configuration might be applicable to NpIn₃, because the magnetic effective moment is close to the value for the Np³⁺ free ion. Moreover, the Mössbauer measurement indicates the Np³⁺ valence state from the isomer shift [76]. In this case, the total number of valence electrons is 12, which is also even in number, meaning that NpIn₃ is a compensated metal.

Both 5*f*-itinerant and localized pictures deduce NpIn₃ as a compensated metal. Thus we restrict ourselves to a compensated metal of NpIn₃ in order to construct the Fermi surface from the present dHvA results on the basis of the 5*f*-localized Np³⁺ (5*f*⁴) configuration. We note that the Brillouin zone in the ferromagnetic state is the same as that in the paramagnetic state. Thus it is possible to treat NpIn₃ as a compensated metal in the same way as in the paramagnetic state.

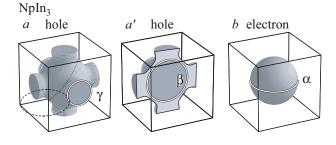


Fig. 41. Proposed Fermi surfaces in the field-induced ferromagnetic state of NpIn₃, cited from Ref. 58.

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On the basis of the 5*f*-localized Np³⁺ (5*f*⁴) configuration and the Fermi surface of LaIn₃, we constructed the Fermi surface in the ferromagnetic state of NpIn₃, as shown in Fig. 41. Characteristic features of the Fermi surface properties in NpIn₃ are as follows. A spherical Fermi surface with a relatively small cyclotron mass of $4m_0$ in NpIn₃ corresponds to a spherical electron Fermi surface in LaIn₃. A complicated hole-Fermi surface in LaIn₃ is simply modified to a multiply-connected Fermi surface with arms along (100) and vacant space at the center in NpIn₃, whose cyclotron masses are large: about $6m_0$ for the arm and $12-14m_0$ for a spherical Fermi surface (vacant space).

Finally we present the dHvA experiment for a paramagnet PuIn₃ with n = 17, where the valence electrons are $5f^5 6d^17s^2$ in the Pu atom and $5s^25p^1$ in the In atom [68]. As noted above, the Wigner–Seitz radius of Pu is an intermediate value between Np with the 5*f*-itinerant and/or 5*f*localized nature and Am with the 5*f*-localized nature. It is thus a challenging study to clarify the electronic state of Pu compounds.

Figure 42 shows the dHvA oscillations and their FFT spectra [68]. It is noted that the dHvA amplitude of branch γ in EX 1 is extremely reduced in EX 2, where the dHvA experiment named EX 2 was done one week later than the first experiment named EX 1. An intensive reduction of the

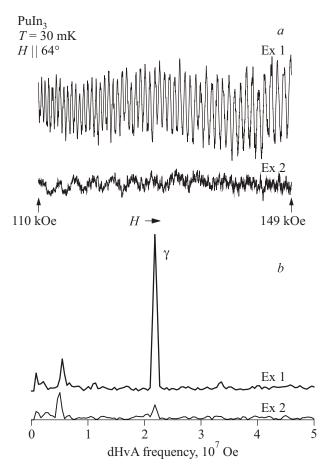


Fig. 42. dHvA oscillations (*a*) and the corresponding FFT spectra in a paramagnet $PuIn_3$ (*b*), cited from Ref. 68.

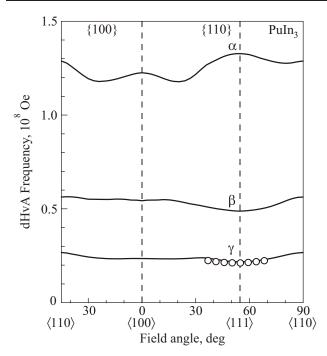


Fig. 43. Angular dependence of the dHvA frequency in a paramagnet PuIn₃. Solid lines are the results of 5*f*-itinerant energy band calculation, cited from Ref. 68.

dHvA amplitude is due to point defects produced by α decay of ²³⁹Pu. On the other hand, the dHvA amplitude of the dHvA frequency $F = 5.5 \cdot 10^6$ Oe is the same between EX 1 and EX 2, as shown in Fig. 42,*b*, which is not due to the dHvA branch in PuIn₃ but due to a dHvA signal of impurities, most likely In, which might be included in subgrain boundaries of the PuIn₃ single crystal sample. This is because the corresponding cyclotron mass is less than $0.5 m_0$.

Figure 43 shows the angular dependence of the dHvA frequency, where branch γ is observed around (111) [68]. Solid lines in Fig. 43 are the result of 5f-itinerant band calculation. Branch y corresponds to a small spherical electron Fermi surface centered at the Γ point, where two kinds of spherical Fermi surface are theoretically obtained on the basis of the 5f-itinerant band model, as shown in Fig. 44. The cyclotron mass of branch γ is $4.8 m_0$, which is three times larger than the corresponding band mass of $1.56 m_0$. A relatively large cyclotron mass of $17 m_0$ might be expected for branch α for $H \parallel \langle 110 \rangle$. On the basis of the results of energy band calculation, the contribution of the 5fcomponent to Fermi surfaces is approximately 50% for branches α and γ , while it is 70% for branch β . It is noticed that these Fermi surfaces in PuIn3 are approximately the same as those of YbIn₃ with n = 11 in topology, as shown in Figs. 17 and 18, although there exists no contribution of 4f electrons to the Fermi surfaces in YbIn₃.

The Fermi surface properties such as 5*f*-itinerant characteristics and the enhanced cyclotron mass in PuIn₃ are very similar to those in the enhanced paramagnet NpGe₃, mentioned above. PuIn₃ is most likely an enhanced paramagnet as in NpGe₃, although the fundamental properties such as the magnetic susceptibility and specific heat are furthermore needed to be clarified in PuIn₃.

We summarize the Fermi surface properties in RX₃ compounds. The Fermi surface of LaSn₃ is slightly different from LaPb₃ in topology. Surprising is that the Fermi surface of LaPb₃ is roughly similar to that of UAl₃. The *f* contribution to the Fermi surface is, however, highly different between two compounds. Therefore, the cyclotron mass is large in UAl₃. The similar Fermi surface is experimentally observed between a 5*f*-localized ferromagnet NpIn₃ and a non-4*f* reference compound LaIn₃, or between an enhanced Pauli paramagnet PuIn₃ and an divalent compound YbIn₃.

It is also interesting that the topology of the Fermi surface in a divalent YbIn₃ is very similar to that of an enhanced Pauli paramagnet YbAl₃, as described in Chap. 3, although the cyclotron mass is highly different between two compounds. The topology of the Fermi surface in ThIn₃ is also almost the same as that of CeIn₃ under pressure, which will be shown later. From the present dHvA experiments and the results of energy band calculations, it is concluded that the *f*-itinerant band model is applicable to the topology of the Fermi surface in enhanced Pauli paramagnets such as YbAl₃, CeSn₃, UAl₃, UX₃ (X: Si, Ge), NpGe₃ and PuIn₃.

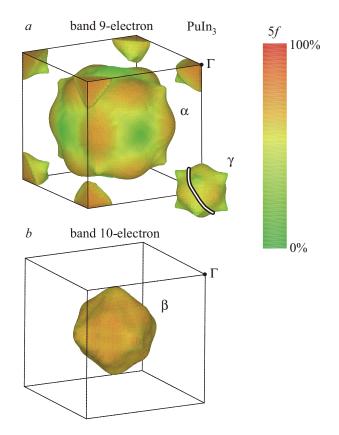


Fig. 44. (Color online) Theoretical 5*f*-itinerant Fermi surfaces in PuIn₃, cited from Ref. 68. The color presents the contribution of 5*f*-electrons.

5. Fermi surface properties in RTIn5 and AnTGa5

Next we present the Fermi surface properties of RTX_5 and $AnTX_5$ with the HoCoGa₅-type tetragonal structure, as shown in Fig. 45. RTX_5 and $AnTX_5$ are classified according to the number of valence electrons, as shown in Table 7 [77–85].

Table 7. Number of valence electrons and Fermi surface studies in RTX_5 and $AnTX_5$ compounds with the HoCoGa₅-type tetragonal structure

Number of valence electrons	Compounds	Refs.
27	LaRhIn ₅ (P)	[77]
	CeRhIn ₅ (AF)	[77]
28	CeRhIn5 under pressure (S)	[78]
	CeCoIn ₅ (P, S)	[79]
	ThRhIn ₅ (P)	[80]
29	UFeGa ₅ (P)	[81]
30	UCoGa ₅ (P)	[82]
31	UPtGa5 (AF)	[83]
	NpRhGa5 (AF)	[84]
32	PuCoGa ₅ (P, S)	[85]
	PuRhGa ₅ (P, S)	

The electronic states in CeTIn₅, ThTIn₅ and AnTGa₅ indicate paramagnetism including Pauli paramagnetism, antiferromagnetism (AF), and superconductivity (S). The crystal structure in Fig. 45 is characteristic, which is closely related to the electronic state. Namely, the uniaxially distorted AuCu₃-type layers of RX₃ (AnX₃) and the TX₂ layers are stacked sequentially along the [001] direction (*c*-

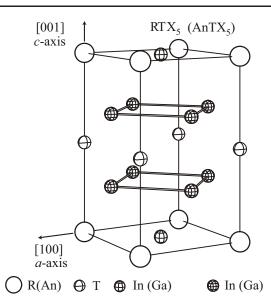


Fig. 45. The tetragonal crystal structure in RTX5 and AnTX5.

axis). For example, the 4*d* electrons of Rh in LaRhIn₅ hybridize with the 5*p* electrons of In, which results in a small density of states around the Fermi energy. This means that there are very few conduction electrons in the RhIn₂ layer and hence the LaIn₃ layer is conductive, producing cylindrical Fermi surfaces. This is also applicable to all the RTX₅ and AnTX₅ compounds, except UTGa₅ (T: Co, Rh and Ir), shown later.

Figures 46,*a* and 46,*b* show the angular dependence of the dHvA frequency and the theoretical one in LaRhIn₅, respectively [77]. Main detected dHvA branches named α_i (*i* = 1, 2 and 3) and β_i (*i* = 1 and 2) are the same as the theoretical ones. These dHvA branches are well identified by

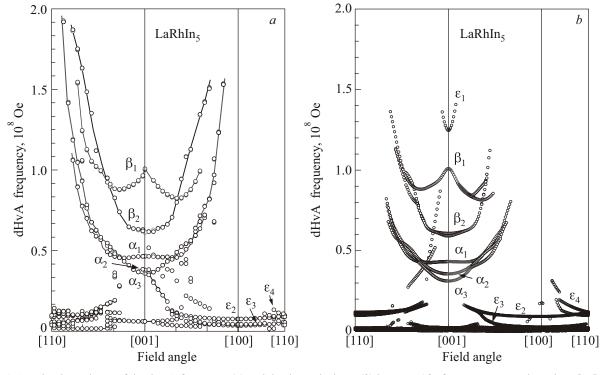


Fig. 46. Angular dependence of the dHvA frequency (a) and the theoretical one (b) in a non-4f reference compound LaRhIn₅ [77].

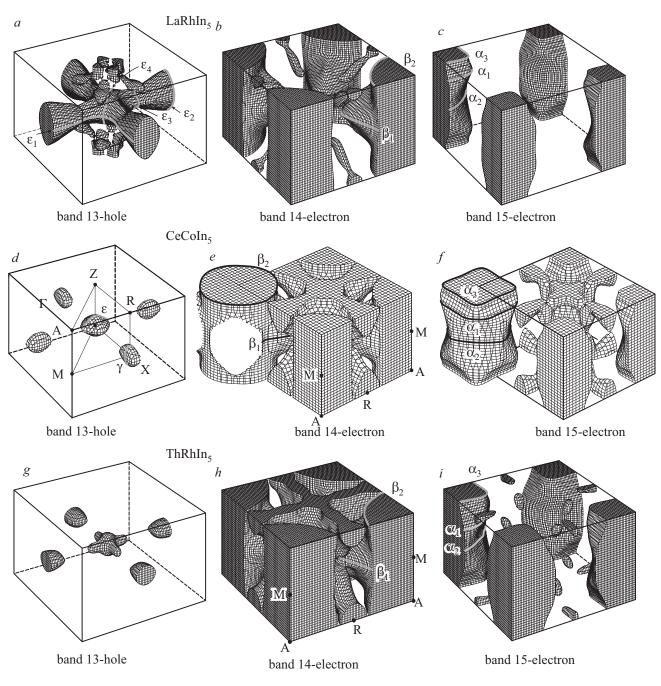


Fig. 47. Theoretical Fermi surfaces of LaRhIn₅ (a)–(c), CeCoIn₅ (d)–(f) and ThRhIn₅ (g)–(i), cited from Refs. 77, 80.

the theoretical Fermi surfaces in Figs. 47,*a*,*c*. The dHvA branches α_i are due to a band 15-electron Fermi surface, which is nearly cylindrical but highly corrugated, having maximum and minimum cross-sections. Branches β_i are also due to a highly-corrugated band 14-electron Fermi surface. This Fermi surface has a convex part stretching along the [110] direction. This is the main reason why the dHvA frequency of branch β_1 has a minimum at about 30°. Here, the electronic configuration in LaRhIn₅ is [Xe] $5d^16s^2$ in the La atom, [Kr] $4d^85s^1$ in the Rh atom and [Kr] $5s^25p^1$ in the In atom. The valence electrons are 27 in number, as shown in Table 7, indicating an uncompensated metal for LaRhIn₅.

In an antiferromagnet CeRhIn₅, the 4*f* electrons are considered to be localized at the Ce sites with magnetic moments of 0.8 μ_B /Ce [86], where the electronic configuration of the Ce atom is [Xe] 4*f*¹ 5*d*¹ 6*s*². The detected main dHvA branches in CeRhIn₅ are thus approximately the same as those of LaRhIn₅ [77].

With increasing pressure *P* for CeRhIn₅, the Néel temperature $T_N = 3.8$ K increases, has a maximum around 1 GPa, and decreases with increasing pressure [87,88]. A smooth extrapolation indicates that $T_N \rightarrow 0$ at $P_c^* = 2.4-2.5$ GPa, as shown in Fig. 48. CeCoIn₅ is a superconductor. The superconducting transition temperature T_{sc} as a function of pressure is also shown in Fig. 48,*b* [89].

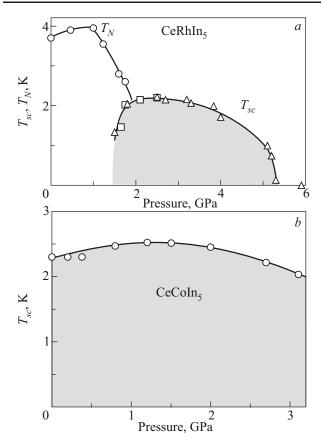


Fig. 48. Pressure phase diagram in CeRhIn₅ (a) and CeCoIn₅ (b), cited from Refs. 87–89.

Figures 49,*a* and 49,*b* show the temperature dependence of the electrical resistivity in CeRhIn₅ under pressure, together with the temperature dependence of electrical resistivity in CeCoIn₅, NpPd₅Al₂ and PuCoGa₅ [90]. At 1.60 and 1.89 GPa, superconductivity as well as antiferromagnetic ordering, shown by arrows in Fig. 49,*b*, are clearly observed in CeRhIn₅. Only superconductivity is observed at 2.08 GPa. Around the critical pressure region, CeRhIn₅ reveals superconductivity with a maximum transition temperature $T_{sc} = 2.2$ K [15]. From the NQR and specific heat experiments, together with the dHvA experiment shown below, the critical pressure is $P_c(H = 0) \approx 2.0$ GPa at zero field [91], whereas $P_c^*(H \neq 0) = 2.4-2.5$ GPa in magnetic fields [78,92,93].

We studied a change of the Fermi surface properties against pressure for CeRhIn₅. A marked change of the dHvA frequencies occurs above $P_c^* \simeq 2.4$ GPa [78]. The detected dHvA frequencies above $P_c^* \simeq 2.4$ GPa are consistent with those of a non-magnetic heavy fermion superconductor CeCoIn₅ of which the dHvA branches are well explained by the 4*f*-itinerant band model [79]. A change of the 4*f*-electron nature from localized to itinerant is realized at $P_c^* \simeq 2.4$ GPa in CeRhIn₅, which will be described in Chap. 7. The upper critical field H_{c2} in superconductivity is also shown later in Fig. 67,*a*, together with the superconducting properties in CeCoIn₅, PuRhGa₅ and NpPd₅Al₂ [79,94–98].

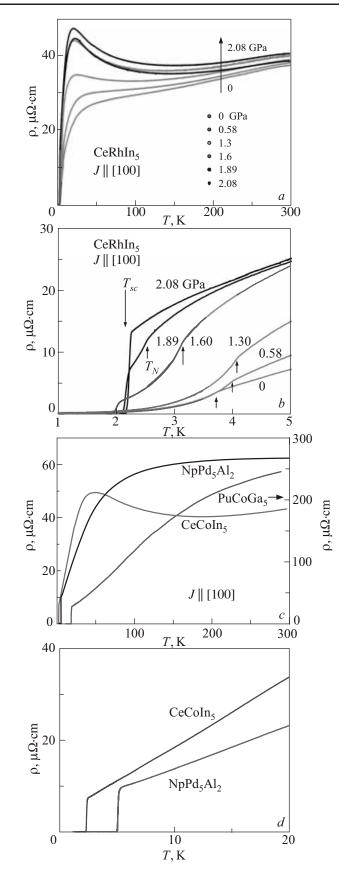


Fig. 49. Temperature dependence of the electrical resistivity in CeRhIn₅ under pressure (*a*), (*b*); in CeCoIn₅, PuCoGa₅, and NpPd₅Al₂ (*c*), (*d*). Only PuCoGa₅ is a polycrystal sample, and the scale is shown by the right hand in (*c*), cited from Ref. 90.

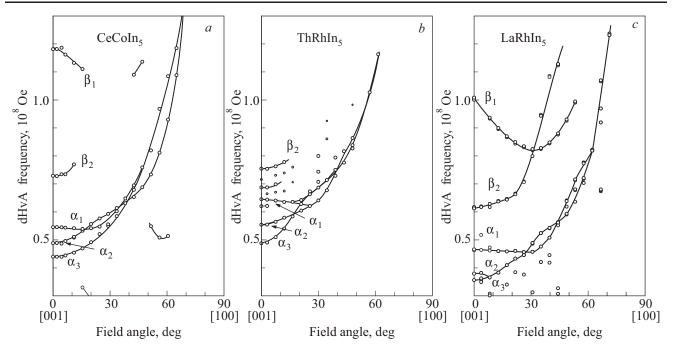


Fig. 50. Angular dependence of the dHvA frequency of a non-magnetic heavy fermion superconductor $CeCoIn_5(a)$, a Pauli paramagnet ThRhIn₅(*b*) and a non-4*f* reference compound LaRhIn₅(*c*), cited from Ref. 80.

Here, the number of valence electrons in CeCoIn₅ is 28, as shown in Table 7, because the 4*f* electron in the Ce atom becomes itinerant at low temperatures, as noted above. CeCoIn₅ thus becomes a compensated metal. Namely, the volume of the electron Fermi surface is equal to that of the hole Fermi surface. The same number of valence electrons is realized in a Pauli paramagnet ThRhIn₅, where the electronic configuration is [Rn] $6d^27s^2$ in the Th atom.

We show in Fig. 50 the angular dependence of the dHvA frequency in CeCoIn₅ and ThRhIn₅, together with LaRhIn₅ for comparison [79,80]. The detected dHvA branches named α_i and β_2 in ThRhIn₅ are approximately the same as those of CeCoIn₅. Note that the dHvA frequencies in both compounds are larger than those of LaRhIn₅ in Fig. 50, c [77]. The theoretical Fermi surface in CeCoIn5 and ThRhIn5 is shown in Figs. 47, d-f and 47, g-i, respectively. The cyclotron mass is, however, highly different between CeCoIn5 and ThRhIn5. The cyclotron mass in CeCoIn5 at low fields is estimated as $100 m_0$ in branch β_2 and $30 m_0$ in branches α_i , as shown in Fig. 51, b. We also show in Fig. 51, a the magnetic field dependence of the electronic specific heat coefficient C_e/T for comparison. The large cyclotron mass in CeCoIn5 is field-dependent, and decreases as a function of the magnetic field. This is characteristic in heavy fermions. These cyclotron masses in CeCoIn5 are large compared with 0.87 m_0 in branch β_2 and 0.89–0.95 m_0 in branches α_i in ThRhIn₅. The large cyclotron mass in CeCoIn₅ is mainly due to the many-body Kondo effect. It is clarified from the energy band calculation that the 4f-electron contribution to the density of states at the Fermi energy in CeCoIn5 is about 70% in magnitude. Note that the 4f electron does not contribute the electronic state in ThRhIn5 because of no existence of 4f electrons, revealing a small cyclotron mass.

The characteristic features of superconductivity in CeCoIn₅ are as follows. Superconductivity is of the $d_{x^2-y^2}$ -type, with line nodes for the [110] direction, elon-gating along the [001] direction on the quasi-two dimensional Fermi surfaces, which was clarified from the angular

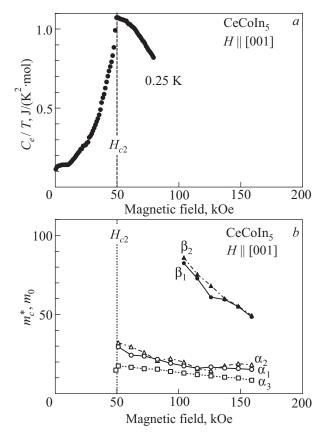


Fig. 51. Field dependence of the electronic specific heat $C_e/T(a)$ and cyclotron mass in CeCoIn₅ (*b*), cited from Ref. 82.

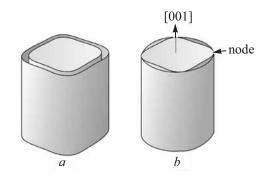


Fig. 52. Schematic pictures of the two dimensional superconducting gap with an isotropic gap (a) and a line node gap (b), cited from Ref. 21.

dependence of the thermal conductivity in magnetic fields [99]. We show schematically the gap with the line nodes in

CeCoIn₅ H || [001 a 2.0 50 mK *M*, emu/g 1.0 H || [100] 0 40 80 Magnetic field, kOe 120 NpPd₅Al₂ b 0.4 1.8 K H_{c2} *H* || [100] 0.2 0 2.3 Magnetization, μ_B/Np 0 0 20 40 $\overline{60}$ Magnetic field, kOe

Fig. 52,*b*. The usual gap is shown in Fig. 52,*a* for comparison. The first-order phase transition from the superconducting mixed state to the normal state occurs at the upper critical field H_{c2} in CeCoIn₅ in the magnetization curve [100], as shown in Fig. 53,*a*, together with the similar step-like magnetization curves of NpPd₅Al₂ in Fig. 53,*b*, which are later discussed [96]. This persists up to about $0.3T_{sc}$ ($T_{sc} = 2.3$ K) for $H \parallel$ [001] and $0.4T_{sc}$ for $H \parallel$ [100] in CeCoIn₅. The H_{c2} value is later shown in Fig. 67,*b* as a function of temperature. The Fulde, Ferrel, Larkin, Ovchinikov (FFLO) state most likely exists in the superconducting mixed state close to H_{c2} at temperatures far lower than $T_{sc} = 2.3$ K [97,98]. These are closely related to the strong Pauli paramagnetic effect in the present superconductivity of CeCoIn₅.

Furthermore we show in Fig. 54,a the temperature dependence of the magnetic susceptibility in CeCoIn₅ [77],

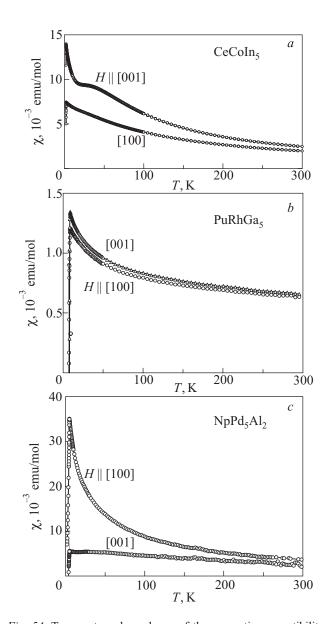


Fig. 53. Magnetization curves of CeCoIn₅ [100] (*a*) and NpPd₅Al₂ (*b*) [96], revealing a step-like increase of the magnetization at H_{c2} .

Fig. 54. Temperature dependence of the magnetic susceptibility in CeCoIn₅ [77] (*a*), PuRhGa₅ [95] (*b*) and NpPd₅Al₂ [96] (*c*).

together with the magnetic susceptibility in PuRhGa5 and NpPd₅Al₂ [95,96]. The susceptibility increases steeply with decreasing temperature, but a sudden drop of the susceptibility occurs below $T_{sc} = 2.3$ K due to the onset of superconductivity. This is not usual. In the case of a typical heavy fermion superconductor UPt3, for example, the magnetic susceptibility has a maximum at $T_{\chi max} \simeq 20$ K, and becomes constant at temperatures lower than $T_{\chi max}$, as shown in Fig. 2. Superconductivity occurs below $T_{sc} = 0.5$ K in UPt₃. This means that superconductivity is realized after the heavy fermion state is completely formed. On the other hand, the heavy fermion state is not completely formed at $T_{sc} = 2.3$ K in CeCoIn₅. Namely, superconductivity of CeCoIn5 is realized in the non-Fermi liquid state. The similar behavior is observed in the other superconductors of PrRhGa₅ and NpPd₅Al₂, as shown in Figs. 54,b and 54, *c*, respectively, which are described later.

Superconductivity in the non-Fermi liquid state of CeCoIn₅ can be also seen in the specific heat data [101,102]. Figure 55 shows the temperature dependence of the specific heat in the form of C_e/T under several magnetic fields. The value of C_e/T increases with decreasing temperature under magnetic fields. The γ value is 380 mJ/(K²·mol) at $T_{sc} = 2.3$ K, but is extremely enhanced to be 1070 mJ/(K²·mol) at 0.2 K. Note that the upper critical field $H_{c2} = 49.5$ kOe for $H \parallel [001]$. The specific heat in the form of C_e/T in the normal state (under H = 60 kOe) does not saturate at low temperatures, but increases with decreasing temperature. The non-Fermi liquid state is thus observed in the specific heat, together with the magnetic susceptibility shown in

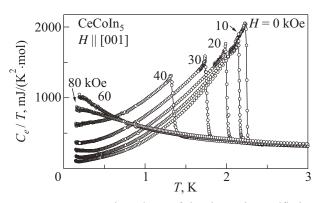


Fig. 55. Temperature dependence of the electronic specific heat in the form of C_e/T in CeCoIn₅, cited from Ref. 102.

Fig. 54,*a*. This is also observed in the electrical resistivity. The electrical resistivity follows a *T*-linear dependence below 10 K, as shown in Fig. 49,*d*. Moreover, the upper critical field $H_{c2}(0)$ and cyclotron mass m_c^* decrease monotonically with increasing pressure [89]. These results indicate that the electronic state of CeCoIn₅ is very close to the quantum critical point at ambient pressure.

We will go on to the next compound of a Pauli paramagnet UFeGa₅ with the number of valence electrons, 29, as shown in Table 7, where the electronic configuration is [Rn] $5f^3 6d^1 7s^2$ in the U atom and [Ar] $3d^6 4s^2$ in the Fe atom. Here we briefly note the electronic states in UTGa₅. Figure 56 shows the temperature dependence of the magnetic susceptibility [21]. UTGa₅ (T: Fe, Ru, Os, Co, Rh, Ir) compounds are Pauli paramagnets, while UTGa₅ (T: Ni, Pd, Pt) order antiferromagnetically.

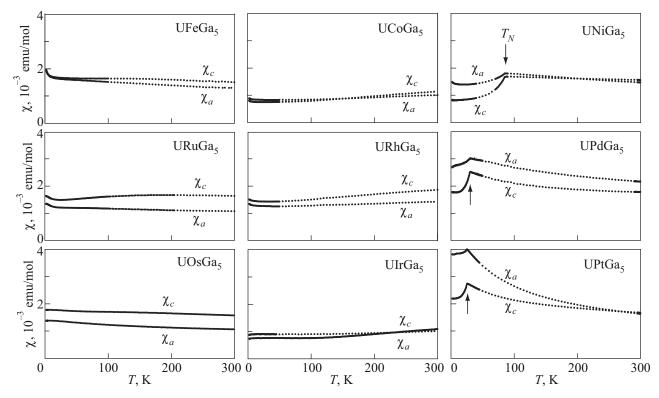


Fig. 56. Temperature dependence of the magnetic susceptibility in UTGa₅ (T: transition metal), cited from Ref. 21.

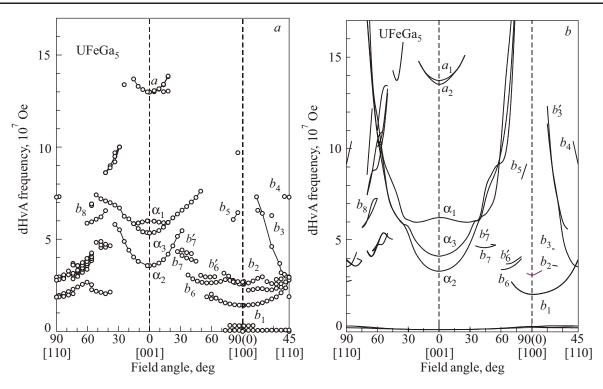


Fig. 57. Experimental angular dependence of the dHvA frequency (a) and the theoretical one (b) in a Pauli paramagnet UFeGa₅, cited from Ref. 81.

We show in Fig. 57 the angular dependence of the dHvA frequency and the corresponding theoretical one for UFeGa₅ [81]. The detected dHvA branches are consistent with the theoretical ones based on the 5*f*-itinerant band 15-electron Fermi surfaces shown in Fig. 58. The Fermi surface consists of a corrugated but cylindrical Fermi surface and a lattice-like Fermi surface. The cyclotron mass is relatively large, ranging from 2.4 to $9.9 m_0$: $9.2 m_0$ for branch α_1 and $9.9 m_0$ for branch *a*. The theoretical band mass is about half of the experimental one, which is consistent with a relation between $\gamma = 40 \text{ mJ/(K}^2 \cdot \text{mol})$ and the theoretical one $\gamma_b = 19.6 \text{ mJ/(K}^2 \cdot \text{mol})$.

In a Pauli paramagnet UCoGa₅ with the number of valence electrons, n = 30, as shown in Table 7, we observed

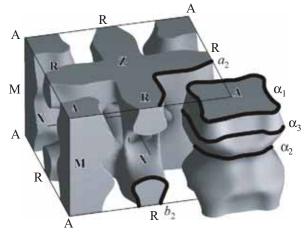


Fig. 58. Theoretical band 15-electron-Fermi surfaces based on a *4f*-itinerant band model in a Pauli paramagnet UFeGa₅, cited from Ref. 81.

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dHvA branches with very small dHvA frequencies, indicating a semimetal [82]. We show in Fig. 59 the angular dependence of the dHvA frequency. Three kinds of dHvA branches named a, b and c correspond to small ellipsoidal Fermi surfaces. We constructed the Fermi surfaces by using the present dHvA data so as to become the semimetal with equal volumes of electron and hole Fermi surfaces, as

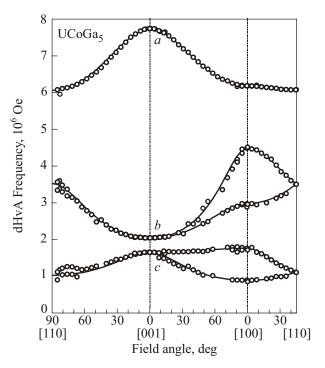


Fig. 59. Angular dependence of the dHvA frequency in a Pauli paramagnet UCoGa₅, cited from Ref. 82.

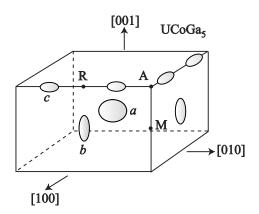


Fig. 60. Proposed Fermi surfaces in a Pauli paramagnet UCoGa₅, cited from Ref. 82.

shown in Fig. 60. The Fermi surface consists of small band 15-hole Fermi surfaces (branches *b* and *c*) and a small band 16-electron Fermi surface (branch *a*) because one more valence electron is added, compared with that in UFeGa₅, and the number of valence electrons is 30 in UCoGa₅, revealing a compensated metal or a semimetal. The γ value of UCoGa₅ is small, $\gamma = 3.3 \text{ mJ/(K}^2 \cdot \text{mol})$, which corresponds to a light cyclotron mass of $m_c^* = 0.82 m_0$ in branch *a* for *H* || [001].

The next compound is UPtGa₅ with the number of valence electrons, n = 31, as shown in Table 7. UPtGa₅ is, however, an antiferromagnet with the Néel temperature $T_N =$ = 26 K and a small ordered moment $\mu_s = 0.32 \ \mu_B/U$ [103]. UPtGa₅ is supposed to be a 5*f*-itinerant antiferromagnet, similar to UGa₃ mentioned in Chap. 4. It is however, noticed that the magnetic susceptibility follows the Curie–Weiss law

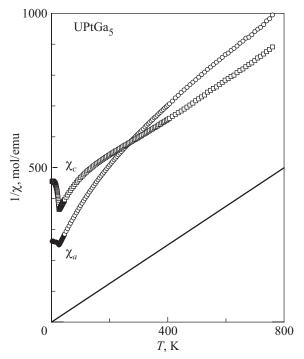


Fig. 61. Temperature dependence of the inverse magnetic susceptibility in UPtGa₅. A solid line corresponds to the free ion value of $5f^2$ and $5f^3$ configurations, cited from Ref. 74.

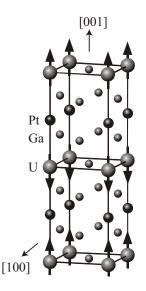


Fig. 62. Antiferromagnetic structure of UPtGa₅, cited from Ref. 103.

above 500 K, with effective magnetic moments of 3.5 and 3.2 μ_B/U for $H \parallel [001]$ and [100], respectively, as shown in Fig. 61 [74]. These effective moments are close to the free ion value of $\mu_{\text{eff}} = 3.58 \ \mu_B/U$ for $5f^2$ (U^{4+}) or $\mu_{\text{eff}} = 3.62 \ \mu_B/U$ for $5f^3$ (U^{3+}), as shown by a solid line in Fig. 61, indicating the localized nature of 5*f* electrons at high temperatures.

A ferromagnetic coupling in the basal (001) plane was observed by the neutron scattering experiment, which is stacked along the [001] direction with an antiferromagnetic $(\uparrow \downarrow)$ sequence, as shown in Fig. 62 [103]. Therefore, the magnetic unit cell becomes doubled, containing the 62 valence electrons. In other words, the magnetic Brillouin zone becomes flat along the [001] direction.

We show in Fig. 63 the angular dependence of the dHvA frequency in the antiferromagnetic state [83]. The detected dHvA branches named α_1 , α_2 , α_3 and γ , and ϵ roughly follow the $1/\cos\theta$ dependence (θ is the tilted angle from [001] to [100] or [110]), revealing cylindrical Fermi surfaces. These branches are well explained by the spin (orbital)-polarized 5f-itinerant band model, as shown in Fig. 63, *b* [83]. The Fermi surface shown in Fig. 64 consists of four kinds of corrugated but cylindrical Fermi surfaces. Branches ε , α_3 , α_1 , α_2 and γ correspond to orbit *a* of the band 31-hole Fermi surface, orbits c_1 and c_2 (band 32electron), orbits d_1 and d_2 (band 33-electron) and orbits e_1 and e_2 (band 30-hole), respectively. The cyclotron effective masses are relatively large: $20 m_0$ (branch ε), $24 m_0$ (branch α_3), 13 and 10 m_0 (branches α_1 , α_2 , respectively) and $10 m_0$ (branch γ). These values are consistent with $\gamma = 57 \text{ mJ/(K}^2 \cdot \text{mol})$. It is stressed here that the almost localized nature of the 5f electrons at high temperatures is changed into the 5*f*-itinerant character, with a small ordered moment of 0.32 μ_B/U .

The similar magnetic structure is realized in an antiferromagnet NpRhGa₅, and the corresponding angular depen-

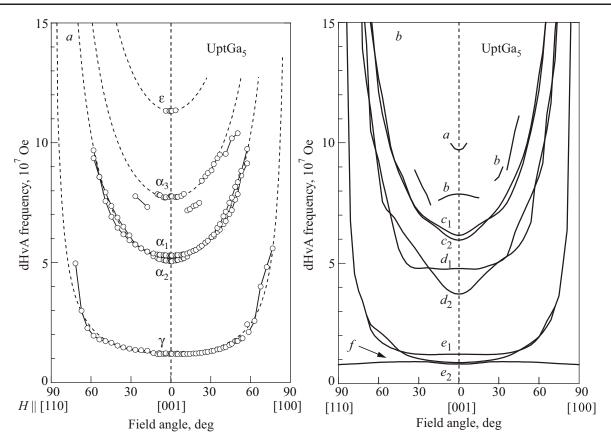


Fig. 63. Angular dependence of the dHvA frequency (*a*) and the theoretical one based on the spin (orbital)-polarized 5*f*-itinerant band model in an antiferromagnet UPtGa₅, cited from Ref. 83 (*b*).

dence of the dHvA frequency is similar to that of UPtGa₅, as shown in Fig. 65 [84]. The magnetic property of NpRhGa₅ is very interesting [104]. There are two successive antiferromagnetic transitions at $T_{N1} = 36$ K and $T_{N2} = 32$ K. The magnetic structure in the temperature range

from T_{N1} to T_{N2} , named AN1, is the same as that in UPtGa₅. We show in Fig. 66 the magnetic phase diagram for $H \parallel [001]$ [105]. Below T_{N2} , the magnetic unit cell (AN2) is the same as AN1 but the direction of the magnetic moment changes abruptly from [001] to [110]. The or-

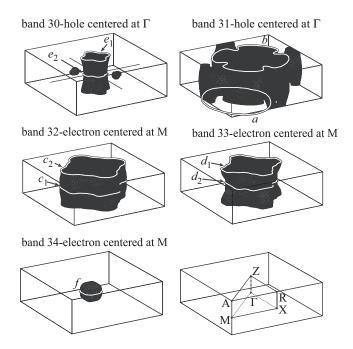


Fig. 64. Theoretical Fermi surfaces based in an antiferromagnet UPtGa₅, cited from Ref. 83.

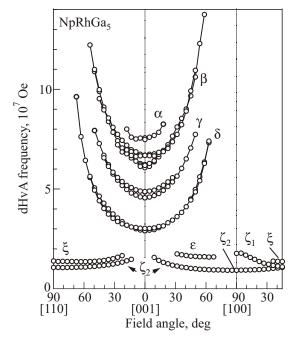


Fig. 65. Angular dependence of the dHvA frequency in an antiferromagnet NpRhGa₅, cited from Ref. 84.

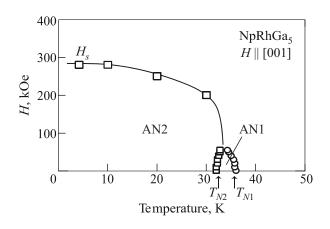


Fig. 66. Magnetic phase diagram for $H \parallel [001]$ in NpRhGa₅, cited from Ref. 105.

dered moment is most likely enhanced from 0.6 μ_B/Np to 0.96 μ_B/Np . The former value is an ordered moment, estimated under the assumption that the AN1 phase persists down to 0 K without the magnetic transition at T_{N2} . The latter value of 0.96 μ_B/Np is determined experimentally at low temperatures far below T_{N2} . It is theoretically pointed out that the quadrupolar interaction plays an important role on this transition at T_{N2} [106].

Here we note that all the NpTGa₅ compounds order antiferromagnetically, indicating no paramagnetism, which are in contrast with the electronic states in UTGa₅. Moreover, the ordered moments in neptunium compounds are roughly twice larger than those in uranium compounds. This is the reason why the magnetic moment at the Np site is of the localized character. The Fermi surface properties of NpRhGa₅ are, however, well explained by the spin (orbital)polarized 5*f*-itinerant band model as in UPtGa₅, as described above. This claims that the 5*f* electrons, as it were, possess the dual nature: the local moment at the Np site and the contribution of the 5*f* electrons to the Fermi surface.

The discovery of non-magnetic heavy fermion superconductors PuCoGa₅ (T_{sc} = 18.5 K) and PuRhGa₅ (T_{sc} = = 9 K) with the number of valence electrons, n = 32, in Table 7 has attracted attention because of its high T_{sc} and unconventional superconducting properties [90,107]. The magnetic susceptibility of PuRhGa5 increases with decreasing temperature, following the Curie-Weiss law with an effective magnetic moment of the $5f^5$ (Pu³⁺) configuration, but indicates a sudden drop of the susceptibility due to onset of superconductivity [95], as shown in Fig. 54,b. From the result of the upper critical field, the topology of the Fermi surface is most likely cylindrical as in CeCoIn₅, as shown in Fig. 67, c [95], although the dHvA experiment was not carried out because of the high H_{c2} value at lower temperatures. Theoretically, three kinds of cylindrical Fermi surfaces are proposed on the basis of the 5f-itinerant band model for PuCoGa₅ [85], as shown in Fig. 68,a, together with the cylindrical Fermi surfaces of CeCoIn5 and NpPd₅Al₂ in Figs. 68,b and 68,c, respectively.

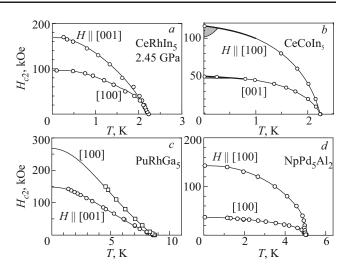


Fig. 67. Temperature dependence of the upper critical field in CeRhIn₅ [94] (*a*), CeCoIn₅ [79] (*b*), PuRhGa₅ [95] (*c*) and NpPd₅Al₂ [96] (*d*). Thick solid lines in CeCoIn₅ indicate the first-order phase transition at H_{c2} , and the dark-gray regions in the mixed state might be the FFLO state, cited from Refs. 97, 98.

Finally we note superconductivity of NpPd₅Al₂ with the tetragonal structure [96]. The crystal structure of NpPd₅Al₂ is similar to the tetragonal structure of CeCoIn₅ and PuCoGa₅, as shown in Fig. 69. The $5s^25p^1$ ($4s^24p^1$) electrons of the In(Ga) atoms in CeCoIn₅ (PuCoGa₅) are, however, replaced by the 4d electrons of the Pd atom in NpPd₅Al₂. The 4*d* electrons are well hybridized with the 5*f* electrons, and produce the strongly correlated conduction electrons. NpPd₅Al₂ does not order magnetically. The corresponding magnetic susceptibility increases steeply with decreasing temperature, but a sudden drop of the susceptibility occurs below $T_{sc} = 4.9$ K due to the onset of superconductivity, as shown in Fig. 54,c. This is very similar to that in CeCoIn5 in Fig. 54,a. The electronic state of NpPd₅Al₂ is found to be located in the vicinity of the antiferromagnetically ordered state from the results of the magnetic susceptibility and the negative value of the paramagnetic Curie temperature. In fact, the γ value is large, $\gamma = 200 \text{ mJ/(K}^2 \cdot \text{mol})$ at $T_{sc} = 4.9 \text{ K}$, and is enhanced to be 390 mJ/(K^2 ·mol) at 0 K from the entropy balance. Furthermore, the low-temperature electrical resistivity does not follow the Fermi liquid relation, but indicates a T-linear dependence, as shown in Fig. 49,d. The large paramagnetic effect is reflected in the strong suppression of the upper critical field, as shown in Fig. 67,d and the step-like increase of the magnetization at H_{c2} , as shown in Fig. 53, b. In the case of a typical d-wave superconductor CeCoIn₅, a large paramagnetic effect induces a first-order phase transition at H_{c2} , namely the step-like increase of the magnetization, below temperatures lower than $0.3T_{sc}$ or $0.4T_{sc}$ $(T_{sc} = 2.3 \text{ K})$, as shown in Fig. 53,*a* [100]. The similar phenomenon is realized in NpPd5Al2. Surprisingly, the step-like increase of magnetization is observed up to a high temperature of 3 K (= $0.6T_{sc}$).

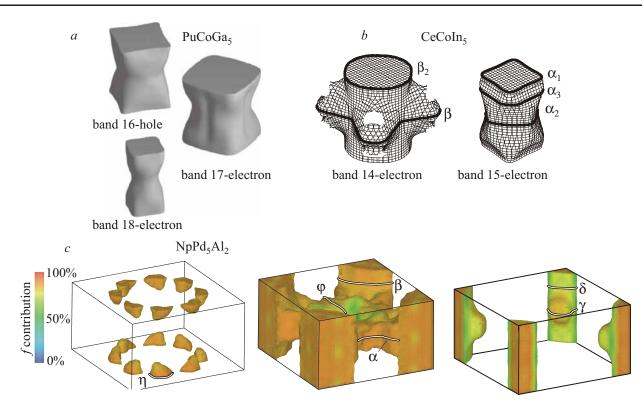


Fig. 68. Theoretical Fermi surfaces based on the f-itinerant band model in PuCoGa₅ [85] (a), CeCoIn₅ [78] (b) and NpPd₅Al₂ [108] (c).

It is noticed that the normal and superconducting properties of NpPd₅Al₂ are very similar to those of CeCoIn₅, but the anisotropy of the magnetic susceptibility and the upper critical field is different from each other. If we simply analyze the anisotropy of the upper critical field from the so-called effective mass model, it is deduced that the

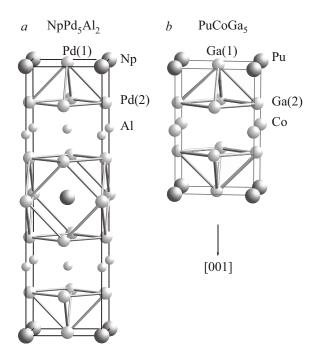


Fig. 69. Crystal structure of actinide superconductors NpPd₅Al₂ (a) and PuCoGa₅ (b), cited from Ref. 21.

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Fermi surface is of a pan-cake shape in NpPd₅Al₂. The corresponding Fermi surface based on the 5*f*-itinerant band model is, however, quasi-two dimensional, as shown in Fig. 68, *c* [108]. It might be necessary to consider the anisotropic spin susceptibility between $H \parallel$ [110] and [001], because the upper critical field is suppressed due to the large paramagnetic effect.

We will summarize the Fermi surface properties in RTIn₅ and AnTGa₅. One of the characteristic properties in RTIn5 and AnTGa5 compounds is quasi-two dimensional in the electronic state, revealing nearly cylindrical Fermi surfaces along the tetragonal [001] direction. Furthermore, the quasi-two dimensional electronic state, together with the heavy fermion state, enhances heavy fermion superconductivity, as in CeCoIn₅, NpPd₅Al₂, PuCoGa₅ and PuRhGa₅. In fact, the superconducting transition temperature T_{sc} = = 0.2 K in CeIn₃ under 2.6 GPa is enhanced to T_{sc} = 2.3 K in CeCoIn₅. Interesting is a relation between the superconducting transition temperature and γ value: 2.3 K in CeCoIn5, 4.9 K in NpPd5Al2, 8.6 K in PuRhGa5 and 18.5 K in PuCoGa₅. Correspondingly, the γ value decreases from 1070 mJ/(K²·mol) in CeCoIn₅ to 100 mJ/(K²·mol) in PuTGa₅ (T: Co, Rh). The γ value in CeIn₃ under 2.6 GPa is roughly estimated as 1000 mJ/($K^2 \cdot mol$) from the cyclotron mass close to $100 m_0$, which is discussed later in Chap. 7. It is also stressed that heavy fermion superconductivity in these superconductors is realized in the non-Fermi liquid state. Superconducting properties of CeRhIn5 at 2.45 GPa, CeCoIn₅, PuRhGa₅ and NpPd₅Al₂ are summarized in Table 8.

	CeRhIn ₅ (2.45 GPa)		CeRhIn ₅ (2.45 GPa) CeCoIn ₅		PuRhGa ₅		NpPd ₅ Al ₂	
	<i>H</i> [100]	[001]	<i>H</i> [100]	[001]	<i>H</i> [100]	[001]	<i>H</i> [100]	[001]
T_{sc} , K	2.22		2.3		8.6		4.9	
$-dH_{c2}/dT$, kOe/K	184	193	240	110	35	20	64	310
$H_{c2}(0)$, kOe	97	169	116	50	270	150	37	143

Table 8. Superconducting properties of CeRhIn5 at 2.45 GPa, CeCoIn5, PuRhGa5 and NpPd5Al2, cited from Refs. 94, 79, 21, 96

6. Metamagnetism

Metamagnetism or the metamagnetic behavior is a phenomenon showing an abrupt nonlinear increase of magnetization at the magnetic field H_c or H_m . The magnetization curve of an antiferromagnet is a typical example, which was shown in Chaps. 3–5, see Fig. 11, for example. In this Chapter we will introduce two different kinds of metamagnetic behavior.

As mentioned in Introduction, some Ce, Yb or U compounds such as CeCu₆, CeRu₂Si₂, YbCu₂Si₂, and UPt₃ exhibit no long-range magnetic ordering. The magnetic susceptibility of these compounds increases with decreasing temperature, following the Curie-Weiss law at high temperatures, and shows a maximum at a characteristic temperature $T_{\chi max}$. Below $T_{\chi max}$, the susceptibility becomes almost temperature-independent, and the f-electron system is changed into a new electronic state, called the heavy fermion state, as shown in Fig. 2. The almost localized felectrons at high temperatures become itinerant at temperatures lower than $T_{\gamma max}$ via the many-body Kondo effect. The crossover from "localized" to "itinerant" occurs at a characteristic temperature $T_{\chi max}$, which approximately corresponds to the Kondo temperature T_K . Below $T_{\chi max}$, the magnetization indicates a metamagnetic behavior or an abrupt nonlinear increase in magnitude at the magnetic field H_m . We will present the Fermi surface properties below and above H_m , together with a relation between $T_{\chi max}$ and H_m , for CeRu₂Si₂, UPt₃ and YbT₂Zn₂₀ (T: Co, Rh, Ir).

Moreover, we will show another metamagnetic behavior based on the field-induced ferroquadrupolar ordering in PrCu₂ in the last section.

6.1. Metamagnetic behavior of a heavy fermion compound CeRu₂Si₂

Here we discuss a metamagnetic behavior in CeRu₂Si₂, which crystallizes in the tetragonal structure with one molecule per primitive cell, as shown in Fig. 70. The metamagnetic behavior occurs at a critical field $H_m = 77$ kOe for the magnetic field along the [001] direction, as shown in Fig. 71. The magnetization curve is reversible at the metamagnetic behavior, showing no hysteresis [109,110].

An important point is as follows. We define a field differential magnetization $\chi = dM/dH$. The magnitude of $\Delta \chi = \chi - \chi_0$ at $H = H_m$, where χ_0 is a field-independent suscep-

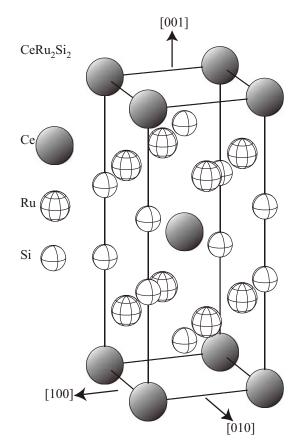


Fig. 70. Crystal structure of CeRu₂Si₂.

tibility, namely, χ at low fields ($H \ll H_m$), is found to become finite at low temperatures. This is shown in inset of Fig. 71, indicating a finite value of $\Delta \chi^{-1}$ as $T \to 0$. This result clearly indicates that the present metamagnetic be-

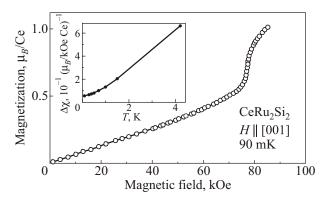


Fig. 71. Magnetization curve of CeRu₂Si₂, cited from Refs. 109, 110. The insert shows the temperature dependence of $\Delta \chi^{-1}$ defined in the text.

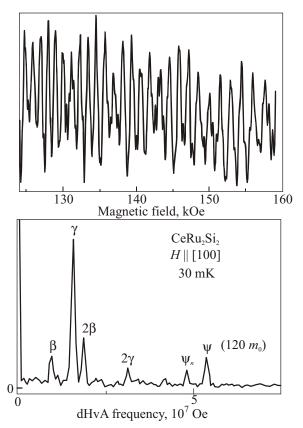


Fig. 72. dHvA oscillation (*a*) and the corresponding FFT spectrum of CeRu₂Si₂ for the field along [100] (*b*).

havior is not of the first-order. We may expect that the heavy fermion state at $H < H_m$ is continuously connected to the high-field spin-polarized state where the magnetic moment at each cerium site is polarized along the field direction of [001]. Note that the magnetic moment of the doublet in the 4*f*-CEF scheme is about 1 μ_B /Ce. When the magnetic moment is tilted from [001], the metamagnetic field increases as a function of 1/ cos θ , where θ is a field-tiled angle. The present metamagnetism is of an Ising-type.

The Fermi surface was observed by the dHvA experiment in magnetic fields up to 190 kOe at low temperatures down to 20 mK [111–113]. Figure 72 shows the dHvA oscillation for $H \parallel$ [100] and the corresponding FFT spectrum. Figure 73 shows the angular dependence of the dHvA frequency, which was obtained below H_m , and the result of the energy band calculations under the assumption that the 4*f*-electrons in the Ce ions are itinerant. All the dHvA branches are identified as follows:

branches ψ and ψ_n : band 14-hole. branches κ , ϵ and α : band 15-electron. branch γ : band 13-hole. branch β : band 12-hole.

The theoretical Fermi surface is shown in Fig. 74 [114]. The experimental dHvA result is in good agreement with the 4*f*-itinerant band model, although the calculated Fermi surfaces have a slightly larger volume than the experimental surfaces. The branches ψ and ψ_n have an extremely large cyclotron mass of $120 m_0$. The cyclotron mass is about 60 times larger than the corresponding band mass because the many-body Kondo effect is not included in the usual band calculations.

The metamagnetic behavior occurs at 77 kOe for $H \parallel [001]$, as mentioned above. Figure 75 shows the magnetic field dependence of dHvA frequency and cyclotron

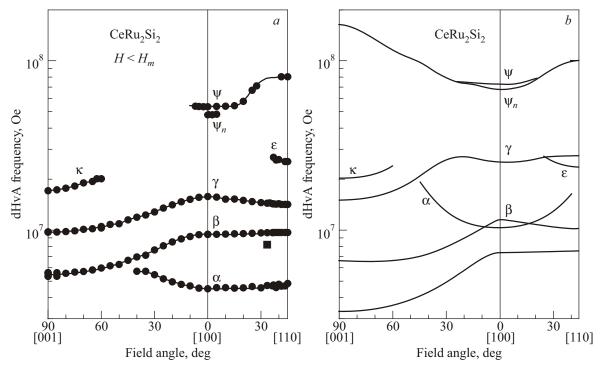
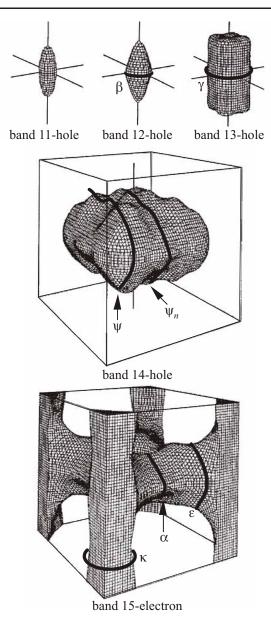


Fig. 73. Angular dependence of the dHvA frequency below $H_c(a)$ and the result of the 4*f*-itinerant band calculations of CeRu₂Si₂ (*b*), cited from Refs. 113, 114.



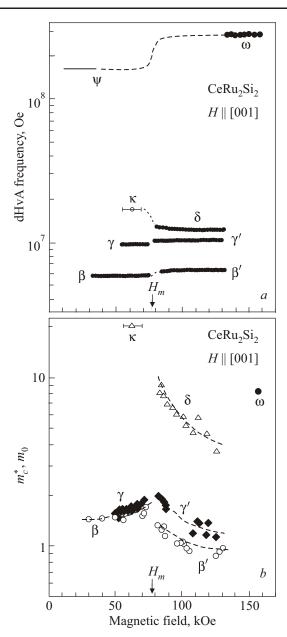


Fig. 74. Theoretical Fermi surface of $CeRu_2Si_2$ below H_c , cited from Ref. 114.

mass for $H \parallel [001] [111-113]$. A step-like change of dHvA frequency, together with a change of the cyclotron mass, is observed at H_m . After the metamagnetic behavior, i.e. at H > 77 kOe, a larger Fermi surface is observed for $H \parallel [001] [111-113]$. This dHvA frequency is the same as that of the main band 14-hole Fermi surface in LaRu₂Si₂, as shown in Fig. 76. Note that the experimental dHvA result of LaRu₂Si₂ is consistent with the theoretical calculation [115]. This result claims that the nature of the 4f-electrons in CeRu₂Si₂ is changed from itinerant to localized. The Fermi surface of LaRu₂Si₂ is shown in Fig. 77.

These results of dHvA experiments are not consistent with those of the magnetization experiments mentioned above. The dHvA results reveal that the spin-polarized state in $H > H_m$ is equal to the localized 4*f*-electron state from the viewpoint of the topology of the Fermi surface,

Fig. 75. Field dependence of the dHvA frequency (*a*) and cyclotron mass (*b*) for $H \parallel [001]$ in CeRu₂Si₂, cited from Ref. 113.

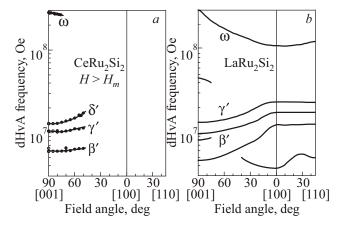


Fig. 76. Angular dependence of experimental dHvA results above H_c for CeRu₂Si₂ (*a*) and the band calculation results of LaRu₂Si₂ (*b*), cited from Refs. 113, 115.

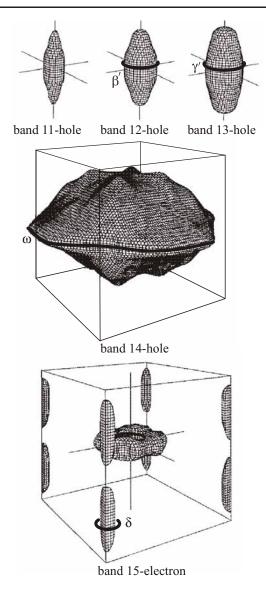


Fig. 77. Theoretical Fermi surface of $LaRu_2Si_2$, cited from Ref. 115.

indicating a change of 4*f*-electron nature from itinerant to localized at H_m , while the magnetization results indicate that the heavy fermion state in $H < H_m$ is continuously connected to the high-field spin-polarized state in $H > H_m$.

The metamagnetic behavior in CeRu₂Si₂ was considered to be an abrupt non-linear increase of the magnetization of which the magnetic field H_m is plotted as a function of temperature, as shown in Fig. 78,*a* [109,110]. Direct and clear evidence was obtained by the specific heat experiment [116]. Two peaks were observed in the field dependence of the specific heat above 0.5 K, as shown in Fig. 78,*b* [116,117]. These results were explained by the Zeeman effect of the conduction electrons with the characteristic density of states.

A change of the 4*f*-electronic state, which occurs below $T_{\chi max}$, is not of the first order because the many-body Kondo effect is not of a first order transition. Therefore, a change of the Fermi surface which occurs at $H > H_m$

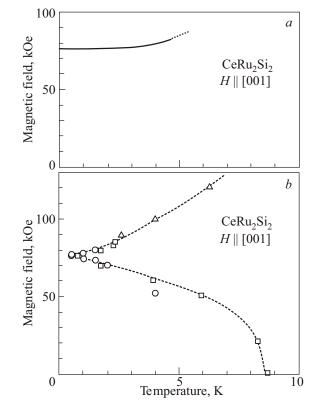


Fig. 78. Temperature dependence of metamagnetic field (*a*) and phase diagram of CeRu₂Si₂, which was determined from the specific heat (shown by circles) and from the thermal expansion coefficient (shown by squares and triangles) (*b*), cited from Refs. 109, 110, 116, 117.

should not be of the first order, although the present change of the Fermi surface at H_m reveals the first-order phase transition. It is not easy to understand the present metamagnetic behavior because it occurs in a small field region around H_m with $T \rightarrow 0$, as shown in Fig. 78,*b*.

Several theories were presented to explain the metamagnetic behavior in $CeRu_2Si_2$, but this is still an open question [118–120].

A similar metamagnetic behavior occurs in CeFe₂Ge₂ [121] and CeCu₆ [122]. The relation between $T_{\chi max}$ and H_m for these compounds is later shown in Fig. 90 [123].

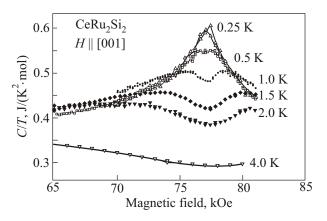


Fig. 79. Magnetic field dependence of the specific heat in CeRu₂Si₂, cited from Ref. 116.

6.2. 5f-itinerant heavy fermion compound: UPt3

UPt₃ with the hexagonal structure is a well-known heavy superconductor in which unconventional pairing state is realized [11]. To understand the 5*f*-electron nature, it is essentially important to clarify the Fermi surface property [124,125].

Figure 80 shows the angular dependence of the dHvA frequency. The origin of the detected dHvA branches is identified on the basis of the 5*f*-itinerant band model. Figure 81 shows the theoretical Fermi surfaces. The branches are as follows:

branch ω : band 37-electron

branch τ , $\sigma, \rho, \lambda, \epsilon$ and α : band 36-hole

branch δ : band 35-hole.

The dHvA frequencies, shown by circles in Fig. 80, are in good agreement with theoretical results (solid lines) based on the 5*f*-itinerant band model. The dHvA branch ω possesses the largest cross-sectional area and cyclotron mass. The mass is determined as 80*m*₀ in the field range of 150 to 175 kOe for the field along [0001], 105*m*₀ in the field range of 182 to 196 kOe for [1010] and 90*m*₀ in the field range of 170 to 196 kOe for [1120]. The corresponding band masses are 5.09, 6.84 and 5.79*m*₀, respectively. The cyclotron masses are about 15 times larger than the corresponding band masses. It should be noted that all the conduction bands contain a 5*f*-electron component of about 70% at the Fermi energy.

UPt₃ exhibits the metamagnetic behavior at about 200 kOe as in CeRu₂Si₂. Figure 82 shows the high-field magnetization curve. This metamagnetic behavior persists up to T_{Xmax} ($\simeq 20$ K) where the magnetic susceptibility has

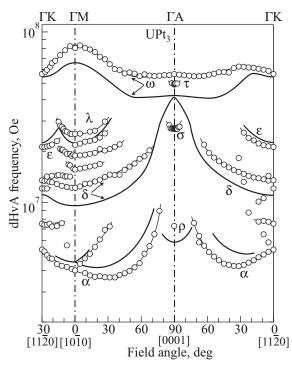


Fig. 80. Angular dependence of the dHvA frequency in UPt₃, cited from Ref. 125. Theoretical results are shown by solid lines.

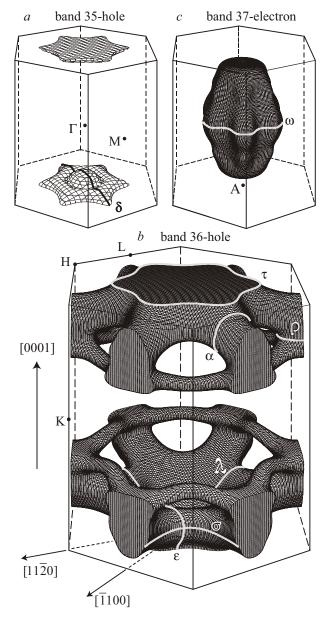


Fig. 81. Fermi surfaces in UPt₃, cited from Ref. 125.

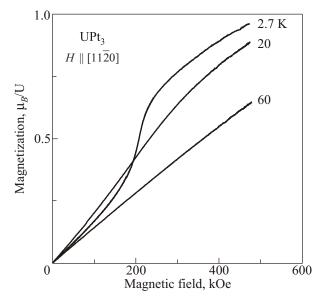


Fig. 82. High-field magnetization in UPt₃, cited from Ref. 126. Low Temperature Physics/Fizika Nizkikh Temperatur, 2012, v. 38, No. 2

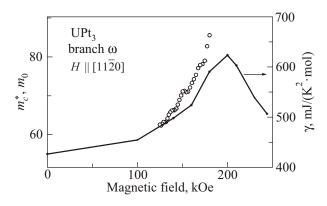


Fig. 83. Field dependence of the cyclotron mass and the γ value in UPt₃ [126]. The result of the γ value was cited from Ref. 127.

a maximum in the temperature dependence, as shown in Fig. 2. Here we note the growth of the cyclotron effective mass at this metamagnetic field $H_m \simeq 200$ kOe, as shown in Fig. 83. The mass in the main band 37-electron Fermi surface, named branch ω , is strongly enhanced with increasing the field from $63 m_0$ at 125 kOe to $86 m_0$ at 180 kOe [126]. This is roughly consistent with the field dependence of the γ value shown in Fig. 83 [127].

It can be thus concluded that the 5*f*-electrons in UPt₃ are of itinerant nature. Namely, the dHvA results are well explained by the 5*f*-itinerant band model. All the branches are heavy, with cyclotron masses of $15-105 m_0$, i.e. ten to twenty times larger than the corresponding band masses. The mass enhancement is caused by magnetic fluctuations, where the freedom of charge transfer of the 5*f* electrons appears in the form of the 5*f*-itinerant band but the freedom of spin fluctuations of the same 5*f* electrons enhances the effective mass as in the many-body Kondo effect. These heavy conduction electrons or quasiparticles condense into Cooper pairs. To avoid a large overlap of the wave functions of the paired particles, the heavy fermion state would rather choose an anisotropic channel, like a *p*-wave spin triplet to form Cooper pairs in UPt₃.

6.3. Heavy fermion state in YbT₂Zn₂₀ (T: Co, Rh, Ir)

In the usual Ce compounds, the magnetic ordering occurs on the basis of the RKKY interaction, as in an antiferro-

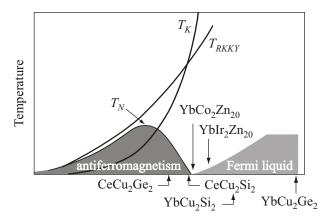


Fig. 84. Doniach phase diagram.

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magnet CeCu₂Ge₂ with $T_N = 4.2$ K [128]. This is because the ground state is the Kramers doublet in the 4*f*-CEF scheme. On the other hand, the Néel temperature is close to zero in a heavy fermion superconductor CeCu₂Si₂, via the many-body Kondo effect [129]. This is because the ionic radius of Ge is larger than that of Si. In fact, the antiferromagnetic state of CeCu₂Ge₂ is changed into a superconducting state by applying pressure: $T_N \rightarrow 0$ for $P \rightarrow P_c = 8$ GPa in CeCu₂Ge₂ [130]. The electronic states of two compounds are schematically presented in the well-known Doniach phase diagram, as shown in Fig. 84 [4].

Yb compounds possess the similar Kramers doublet in the 4*f*-CEF scheme and are expected to order magnetically at low temperatures. YbCu₂Si₂ with the tetragonal crystal structure and YbIr₂Zn₂₀ with the cubic crystal structure compounds, however, do not order magnetically. The temperature dependence of the linear thermal expansion is characteristic [57,131], as shown in Fig. 85. The linear thermal expansion of a Pauli paramagnet YbCu₂Ge₂ shrinks monotonically with decreasing temperature, and becomes approximately zero at low temperatures. This is a usual behavior, indicating an unchange of the electronic state as a function of temperature. On the other hand, there

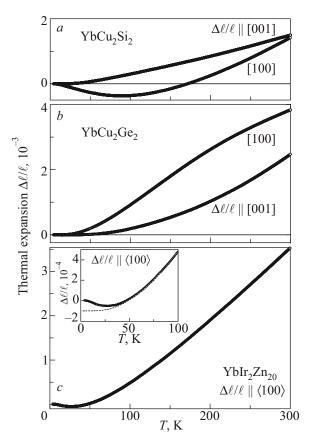


Fig. 85. Linear thermal expansions $\Delta \ell / \ell$ along [001] and [100] in YbCu₂Si₂ (*a*) and YbCu₂Ge₂ (*b*), cited from Ref. 57, and along (100) of YbIr₂Zn₂₀ (*c*), cited from Ref. 131. The inset in shows enlarged scales of the experimental data of YbIr₂Zn₂₀ at low temperatures (*c*). The broken line in the inset is the lattice contribution calculated on the basis of the Grüneisen relation using the specific heat data of YIr₂Zn₂₀.

appears a negative thermal expansion in YbCu₂Si₂ and YbIr₂Zn₂₀ below 90 K and 30 K, respectively, revealing that the electronic state changes from the trivalent state of the Yb ion to the 4f-itinerant state with decreasing temperature. In other words, YbCu₂Si₂ and YbIr₂Zn₂₀ should order antiferromagnetically if the 4f electrons are localized even at low temperatures. Following the Doniach phase diagram, a change of the 4f-localized state to a nonmagnetic 4f-itinerant state corresponds to expansion of the volume in YbCu₂Si₂ and YbIr₂Zn₂₀. These results suggest that the non-magnetic 4f-itinerant state of YbIr₂Zn₂₀ can be tuned to the magnetically ordered state, crossing the quantum critical point, with increasing pressure. It is also noted that the electronic state of YbCo₂Zn₂₀ is very close to the quantum critical point even at ambient pressure, which is also shown below.

Here, YbT₂Zn₂₀ (T: Co, Rh, Ir) crystallizes in the cubic CeCr₂Al₂₀ (*Fd* $\overline{3}m$) crystal structure, as shown in Fig. 86. It is remarkable that the lattice constant a = 14.187 Å in YbIr₂Zn₂₀ is very large, and thus the distance between Yb–Yb atoms is considerably large, 6.14 Å, compared with a = 4.20 Å in YbAl₃ with the AuCu₃-type cubic structure. Note that the Yb atom, which forms the diamond structure, as shown in Fig. 86,*a*, is coordinated by 16 zinc atoms, while the Ir atom has an icosahedral zinc coordination, forming caged structures, as shown in Fig. 86,*b*.

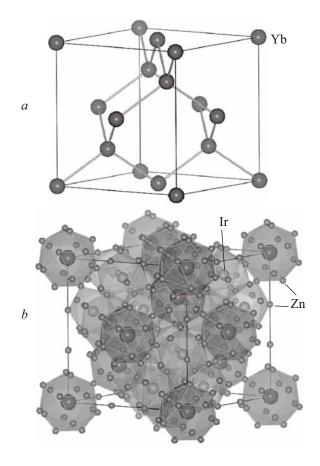


Fig. 86. Crystal structure of YbIr₂Zn₂₀, where Yb atoms form the diamond structure (*a*). Caged structure in YbIr₂Zn₂₀ (*b*).

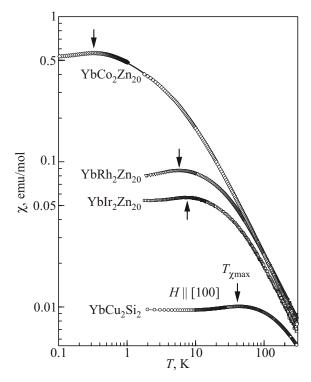


Fig. 87. Temperature dependence of the magnetic susceptibility in YbCo₂Zn₂₀, YbRh₂Zn₂₀, and YbIr₂Zn₂₀ for $H \parallel \langle 100 \rangle$, and in YbCu₂Si₂ for $H \parallel [100]$. The data above 2 K were measured by SQUID magnetometer, and the data below 1 K for YbCo₂Zn₂₀ were obtained by the ac-susceptibility measurement, cited from Ref. 123.

One of the characteristic properties in the heavy fermion compounds is the metamagnetic behavior or an abrupt nonlinear increase of magnetization at the magnetic field H_m below $T_{\chi max}$, as noted above. Figure 87 shows the logarithmic scale of temperature dependence of the magnetic susceptibility in YbCu₂Si₂, YbIr₂Zn₂₀, YbRh₂Zn₂₀ and YbCo₂Zn₂₀ [123,131–135]. The $T_{\chi max}$ values in these compounds, as shown by arrows in Fig. 87, are 40, 7.4, 5.8, and 0.32 K, respectively, where a low-temperature value of $T_{\chi max} = 0.32$ K in YbCo₂Zn₂₀ is remarkable, revealing that the electronic state of YbCo₂Zn₂₀ is very close to the quantum critical point.

We measured the magnetization at 1.3 K for these compounds [123,131,133,134], as shown in Fig. 88. The metamagnetic behavior was observed at $H_m = 97$ kOe in YbIr₂Zn₂₀, 63 kOe in YbRh₂Zn₂₀, and 6 kOe in YbCo₂Zn₂₀, shown by arrows, where the magnetization at 1.3 K does not reveal the metamagnetic behavior, but the ac-susceptibility at 60 mK indicates a peak at $H_m = 6$ kOe in YbCo₂Zn₂₀. Here, it is noted that the metamagnetic field is almost temperature-independent below $T_{\chi max}$: $H_m = 97$ kOe at 1.3 K and 100 kOe at 4 K in YbIr₂Zn₂₀, for example. In YbCo₂Zn₂₀, we also observed the metamagnetic behavior below $T_{\chi max} = 0.32$ K, as shown in Fig. 89,*a*. Interesting is a magnetic phase diagram in Fig. 89,*b*, which is very similar to the phase diagram of CeRu₂Si₂ shown in Fig. 78. Namely, the specific heat coefficient *C/T* of YbCo₂Zn₂₀ has a

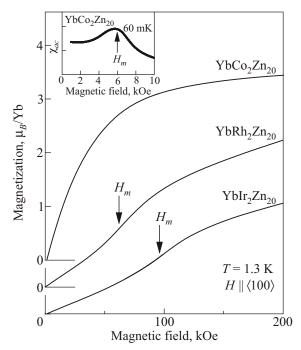


Fig. 88. Magnetization curves at 1.3 K in YbT_2Zn_{20} (T: Co, Rh, Ir). Inset shows the field dependence of the ac-susceptibility at 60 mK in $YbCo_2Zn_{20}$, cited from Ref. 123.

two-peak structure in the field dependence, as shown in Fig. 79 for CeRu₂Si₂. Such two-peak structure in C/T is not observed in YbIr₂Zn₂₀ and YbRh₂Zn₂₀.

The metamagnetic behavior thus appears at H_m below $T_{\chi max}$. The present results are summarized in Fig. 90, representing a relation between $T_{\chi max}$ and H_m in several Ce, Yb, and U compounds: H_m (kOe) = $15T_{\chi max}$ (K). This relation corresponds to $\mu_B H_m = k_B T_{\chi max}$ [123,136].

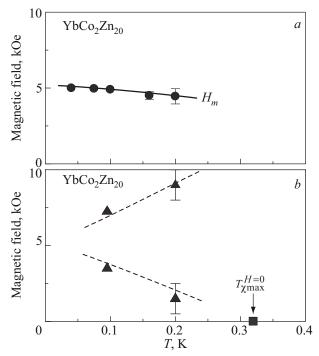


Fig. 89. Temperature dependence of the metamagnetic field (*a*) and phase diagram of $YbCo_2Zn_{20}$ which was determined from the specific heat (shown by triangles) (*b*), cited from Ref. 134.

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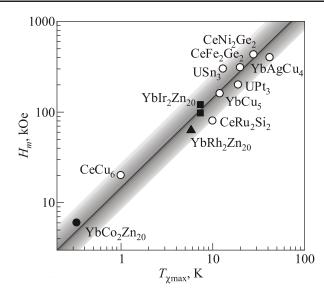


Fig. 90. Relation between $T_{\chi max}$ and H_m in several Ce, Yb, and U compounds. The solid line represent the relation of H_m (kOe) = =15 $T_{\chi max}$ (K), cited from Ref. 123.

We studied the metamagnetic behavior of $YbIr_2Zn_{20}$ via the dHvA experiment. Figure 91 shows the magnetic field dependence of dHvA frequency named branch β and cyclotron mass, together with the \sqrt{A} value in the electrical

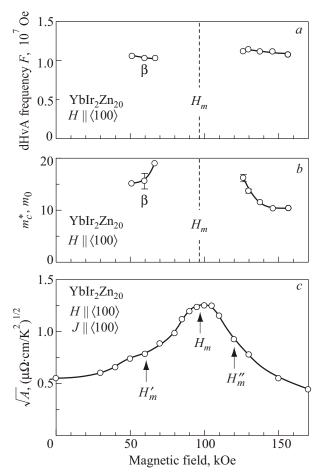


Fig. 91. Magnetic field dependences of the dHvA frequency of branch β (*a*), the corresponding cyclotron mass $m_c^*(b)$, and \sqrt{A} for $H \parallel \langle 100 \rangle$ in YbIr₂Zn₂₀ (*c*), cited from Ref. 131.

resistivity $\rho = \rho_0 + AT^2$ under magnetic field, for $H \parallel \langle 100 \rangle$. The dHvA frequency is approximately unchanged above and below $H_m = 97$ kOe, which is highly different from the result of CeRu₂Si₂ shown in Fig. 75. The cyclotron mass of branch β ($F = 1.1 \cdot 10^7$ Oe), however, has a maximum around H_m , following a field dependence of \sqrt{A} , which is the same result of CeRu₂Si₂ shown in Fig. 75.

We measured the magnetoresistance at 0.1 K under several pressures for YbIr₂Zn₂₀. With increasing pressure, the metamagnetic field $H_m = 97$ kOe at ambient pressure, shown by an arrow, shifts to lower magnetic fields and becomes zero at $P_c \simeq 5.2$, GPa [135], as shown in Fig. 92. It is remarkable that a shoulder-like feature of metamagnetic behavior at 0 and 1.2 GPa is changed into a sharp peak at higher pressures. The present peak, associated with the metamagnetic behavior, is a guiding parameter to reach the quantum critical point: $P \rightarrow P_c$ for $H_m \rightarrow 0$, as shown in Fig. 93,*a*. Here, the *A* value is extremely enhanced with increasing pressure and has a maximum at $P_c \simeq 5.2$ GPa, with $A = 380 \ \mu\Omega \cdot cm/K^2$ at 5.0 GPa, as shown in Fig. 93,*b*.

The relation between A and γ is known as the Kadowaki–Woods plot [137]. The A and γ values in YbT₂Zn₂₀ (T: Co, Rh, Ir) is found to belong to the generalized Kadowaki–Woods relation for N = 4, as shown in Fig. 94 [132, 138,139]. The value of $A = 380 \ \mu\Omega \cdot \text{cm/K}^2$ at 0 kOe under 5.0 GPa exceeds $\gamma = 10 \ \text{J/(K}^2 \cdot \text{mol})$ if we follow this relation. An extremely heavy fermion state is realized in YbIr₂Zn₂₀

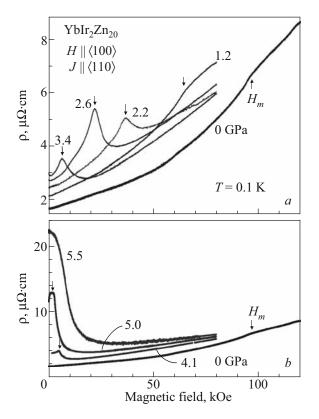


Fig. 92. Transverse magnetoresistance in the pressure region from ambient pressure to 3.4 GPa (*a*) and from 4.1 to 5.5 GPa in $YbIr_2Zn_{20}$ (*b*), cited from Ref. 135. Arrows indicate the metamagnetic transition.

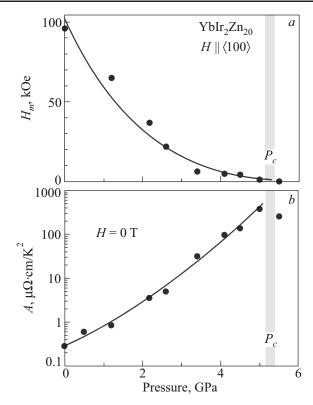


Fig. 93. Pressure dependence of H_m (a) and A values (b) in YbIr₂Zn₂₀, cited from Ref. 135. Solid lines connecting the data are guides for the eyes.

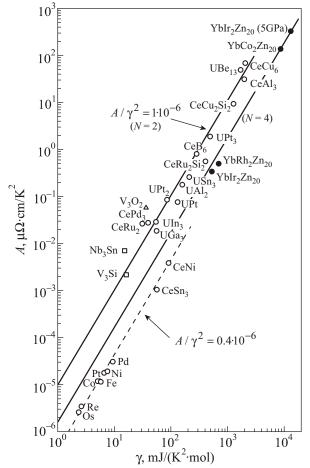


Fig. 94. Generalized Kadowaki–Woods relation in Ce, Yb, U and the other compounds.

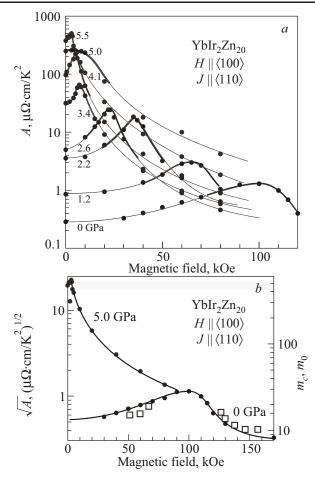


Fig. 95. Field dependence of the *A* value under several pressures (0–5.5 GPa) (*a*), and the \sqrt{A} values under 0 and 5.0 GPa (*b*), shown by circles, and cyclotron effective mass m_c^* at 0 GPa, shown by open squares in YbIr₂Zn₂₀, cited from Ref. 135.

under pressure. Surprisingly YbCo₂Zn₂₀ is very close to this state: $A = 160 \ \mu\Omega \cdot \text{cm/K}^2$ and $\gamma = 8 \cdot 10^3 \ \text{mJ/(K}^2 \cdot \text{mol)}$.

We also measured the temperature dependence of the electrical resistivity below 0.8 K under magnetic fields and pressures. The Fermi liquid relation of $\rho = \rho_0 + AT^2$ is satisfied in these experimental conditions, and the obtained *A* value is shown in Fig. 95,*a* as a function of magnetic field. A broad peak at $H_m = 97$ kOe at ambient pressure in the *A* value is changed into a distinct peak at 2.2 and 3.4 GPa,

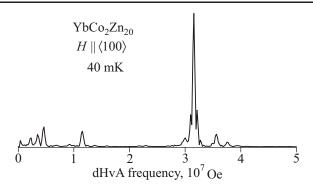


Fig. 96. FFT spectrum for $H \parallel (100)$ in YbCo₂Zn₂₀, cited from Ref. 134.

together with an anomalous enhancement of A value at higher pressures: $A = 380 \ \mu\Omega \cdot \text{cm/K}^2$ at 0 kOe under 5.0 GPa, as mentioned above, which is strongly reduced with increasing magnetic field: $A = 1.45 \ \mu\Omega \cdot \text{cm/K}^2$ at 80 kOe under 5.0 GPa.

We studied the relation between \sqrt{A} and the cyclotron effective mass m_c^* obtained from the dHvA experiment for YbIr₂Zn₂₀ [135]. Figure 95, b shows the field dependence of the cyclotron mass for the dHvA frequency $F = 1.1 \cdot 10^{7}$ Oe in the magnetic field $H \parallel (100)$ at ambient pressure, as shown by open squares, revealing from $10m_0$ to $20m_0$. The cyclotron mass increases slightly with increasing magnetic fields up to H_m , but decreases gradually in much higher fields. The cyclotron mass well correlates with the \sqrt{A} value at 0 GPa against the magnetic field, shown by solid circles. From the experimental results of \sqrt{A} at 0 and 5.0 GPa in Fig. 95, b, we can estimate the cyclotron mass at 0 kOe to be about $450 m_0$ at 5.0 GPa, revealing an extremely large cyclotron mass. In other words, a strong field quenching of the cyclotron mass is expected to occur at high magnetic fields in YbIr₂Zn₂₀ at 5.0 GPa.

The similar results are obtained in YbCo₂Zn₂₀ at ambient pressure. Figure 96 shows the FFT spectrum for $H \parallel \langle 100 \rangle$ in YbCo₂Zn₂₀. The dHvA frequency is in the range $1 \cdot 10^{6} - 4 \cdot 10^{7}$ Oe. From the size of the small Brillouin zone, these dHvA branches correspond to main Fermi surfaces [131]. The cyclotron effective mass is found to be highly field-dependent, decreasing steeply with increasing

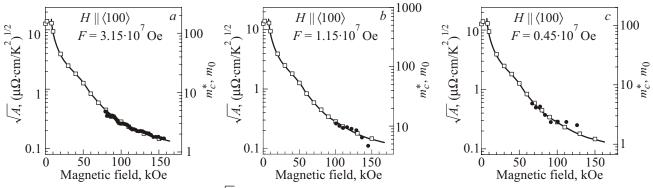


Fig. 97. Magnetic field dependence of the \sqrt{A} value for $J \parallel H \parallel \langle 100 \rangle$, shown by squares, together with the field dependence of the cyclotron effective mass m_c^* , shown by closed circles for $H \parallel \langle 100 \rangle$ in YbCo₂Zn₂₀, for *F*, Oe: 3.15 $\cdot 10^7$ (*a*), 1.15 $\cdot 10^7$ (*b*), and 0.45 $\cdot 10^7$ (*c*), cited from Ref. 123. Solid lines connecting the data are guide lines.

magnetic field. Figures 97,*a*,*b*,*c* show the field dependence of the cyclotron mass for the dHvA frequency $F = 3.15 \cdot 10^7$, $1.15 \cdot 10^7$, and $0.45 \cdot 10^7$ Oe, respectively, together with the \sqrt{A} value obtained from the electrical resistivity under magnetic field.

Following the Fermi liquid relation, the \sqrt{A} value well correlates with the cyclotron effective mass. The cyclotron mass at 0 kOe is thus estimated to be 150, 500, and $110 m_0$, respectively. The present experimental results indicate, however, that the super-heavy effective masses at 0 kOe are quenched, or strongly reduced in high magnetic fields.

6.4. Field-induced ferroquadrupolar ordering in PrCu₂

The quadrupolar interaction is of basic importance in the *f*-electron magnetism as well as the magnetic interactions such as the RKKY interaction and the many-body Kondo effect. The quadrupole moment is obtained from the electrostatic energy:

$$\mathcal{H} = \int \rho(r)V(r) d^{3}r =$$

$$= ZeV(0) + \sum_{j} P_{j} \left(\frac{\partial V}{\partial x_{j}}\right)_{0} + \frac{1}{2} \sum_{j,k} Q_{jk} \left(\frac{\partial^{2} V}{\partial x_{j} \partial x_{k}}\right) + \dots, (16)$$

$$Ze = \int \rho(r) d^3r , \qquad (17)$$

$$P_j = \int \rho(r) x_j \ d^3r \,, \tag{18}$$

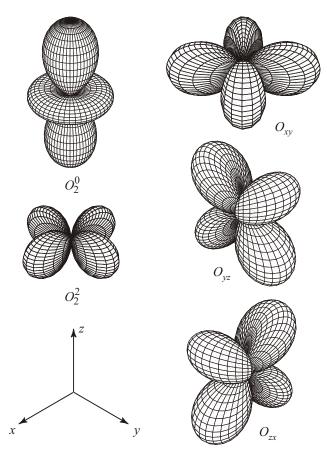


Fig. 98. Schematic view of the quadrupole moments.

where $\rho(r)$ is the charge distribution of the *f*-electrons in the rare earth and uranium compounds, V(r) is the electrostatic potential, Ze is the charge of the *f*-electrons, P_j is a dipole term and Q_{jk} is a quadrupole term. The independent terms in $x_j x_k$ of Eq. (19) are the following five: $2z^2 - x^2 - y^2$, $x^2 - y^2$, xy, yz and zx. These are converted into the quadrupole moments $(2J_z^2 - J_x^2 - J_y^2)/\sqrt{3} = O_2^0$, $J_x^2 - J_y^2 = O_2^2$, $J_x J_y + J_y J_x = O_{xy}$, $J_y J_z + J_z J_y = O_{yz}$ and $J_z J_x + J_x J_z = O_{zx}$, respectively, as shown in Fig. 98.

The quadrupole moment $O_{\Gamma\gamma}$ couples to the strain $\varepsilon_{\Gamma\gamma}$ and distorts the crystal. For example, the cubic structure in CeAg is changed into a tetragonal structure when O_2^0 becomes the order parameter below 16 K [140]. This is because O_2^0 couples to the strain ε_u , which brings about expansion along the z-axis and shrinkage along the x-and y-axes.

In the following we discuss the metamagnetic transition based on the quadrupolar interaction $\langle O_2^0 \rangle$ in PrCu₂ [141– 143]. The crystal structure of PrCu₂ is orthorhombic. This can be viewed as a distorted hexagonal AlB₂ type structure, as shown in Fig. 99,*a*. PrCu₂ is a van Vleck paramagnetic compound in which the quadrupolar interaction plays an important role in the magnetic behavior.

Figure 100 shows the magnetization curves at 15 K for three principal axes. The *c*-axis magnetization M_c is the hard-axis magnetization, while M_a corresponds to the easyaxis magnetization. Both magnetizations should show almost the same curves if PrCu₂ forms the hexagonal structure, but they indicate highly different behavior. This is due to the CEF effect based on the orthorhombic symmetry.

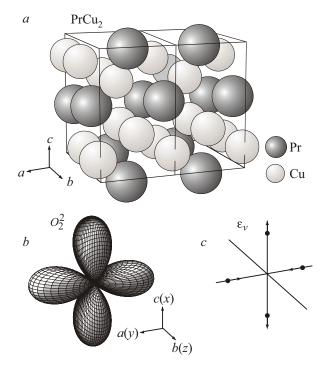


Fig. 99. Crystal structure with two unit cells (*a*), quadrupole moment O_2^2 (*b*) and local distortion ε_{ν} of PrCu₂ (*c*).

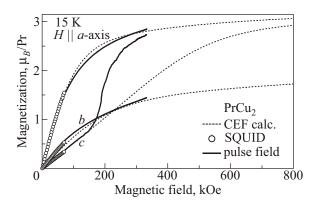


Fig. 100. Magnetization curves of PrCu₂. Thick lines, open circles and dotted lines show the pulse-field experimental curves, SQUID magnetometer data and CEF calculated curves, respectively, cited from Ref. 143.

 M_c shows a metamagnetic transition at $H_c = 200$ kOe and reaches the *a*-axis magnetization M_a at higher fields. In fact it shows the M_a -curve with decreasing magnetic field, showing a large hysteresis. On increasing the field again, M_c is changed into M_a . This metamagnetic transition thus brings about the conversion between the hard *c*-and easy *a*-axis magnetizations. To elucidate this metamagnetic transition, we show in Fig. 100 the calculated magnetizations (broken lines) based on the CEF effect. We also note

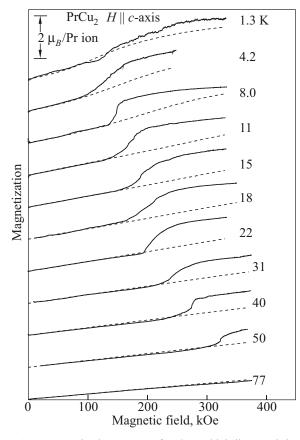


Fig. 101. Magnetization curves of PrCu₂. Thick lines and dotted lines show the experimental and CEF calculated curves, respectively, cited from Ref. 143.

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that the critical field for this metamagnetic transition increases with increasing temperature, from 80–90 kOe at 1.3–4.2 K to 320 kOe at 50 K, as shown in Fig. 101.

The present metamagnetic transition is also observed in the electrical resistivity, magnetostriction and dHvA experiments [141,142]. Figure 102 shows the corresponding magnetostriction curves. First, the magnetic field was applied along the *c*-axis, as shown by open circles in Fig. 102,*a*. The magnetostriction ε_c along the *c*-axis steeply increases at 90 kOe by about 0.5% and then increases smoothly up to 140 kOe; see the processes (1) and (2) in Fig. 102,*a*. On decreasing the field, the magnetostriction decreases slightly, showing a large hysteresis. A large residual strain of 0.5% remains in the sample.

Next we rotated the sample by 90° and applied the field along the *a*-axis. The magnetostriction initially decreases monotonically and shows a step-like decrease at 90 kOe, as shown by the processes (2) and (1'). The strain in the sample, which is brought about by the metamagnetic transition in the field along the *c*-axis, is released by applying the field along the *a*-axis. We note that there is no such a metamagnetic transition if we first apply the field along the *a*-axis.

A similar metamagnetic transition was obtained for the magnetostriction ε_a , as shown in Fig. 102,*b*. The magnetostriction in the field along the *c*-axis steeply decreases at 60 kOe, as shown by the processes (1) and (2) in Fig. 102,*b*. The strain reaches up to 2.7% at 140 kOe. The residual strain at 0 kOe is -1.5%. The strain is released by applying the field along the *a*-axis, as shown by the processes (2) and (1') in Fig 102,*b*, although the residual

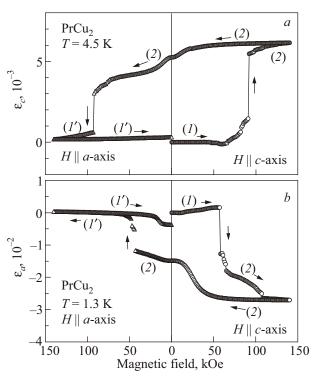


Fig. 102. Magnetostriction along the a(a) and c(b) axes of PrCu₂, cited from Ref. 141.

strain does not recover completely at 0 kOe, retaining a residual value of -0.4%.

The present metamagnetic transition is closely related to the distortion in the *ac*-plane. Namely, the magnetostriction along the *c*-axis, ε_c , is increased and the corresponding ε_a is decreased in magnitude. The strain relation of expansion along the *c*-axis and shrinkage along the *a*axis corresponds to ε_v in Fig. 99,*c*. Therefore, the quadrupolar operator in this system is O_2^0 , as shown in Fig. 99,*b*.

The dHvA effect is a powerful method to detect the metamagnetic transition via the electron scattering [142]. Figure 103 shows the dHvA oscillations for the field along the *a*-axis. When we first apply the magnetic field along the *a*-axis, there is no appreciable change in oscillation, showing a reversible oscillation, as shown in Fig. 103,*a*. On the other hand, the dHvA oscillation is extremely reduced in amplitude after the metamagnetic transition, as shown in Fig. 103,*b*, corresponding to the process (2) in the left-side figure of Fig. 102,*a*. As shown in Fig. 103,*b*, the dHvA oscillation is completely recovered after the metamagnetic transition, i.e. at fields higher than 74 kOe. The corresponding dHvA oscillation is again reversible against the magnetic field, as shown in Fig. 103,*c*.

We explain the present metamagnetic transition on the basis of the quadrupolar interaction $\langle O_2^0 \rangle$. First, we calculated the magnetic susceptibility in the temperature range from about 8 K to room temperature, and determined the CEF parameters and the coupling constant K_M in order to reproduce the susceptibility data and the metamagnetic field transition field on the basis of the following Hamiltonian:

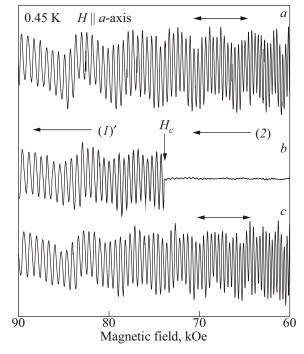


Fig. 103. dHvA oscillations of PrCu₂, cited from Ref. 142. Note that the magnetic field in the left-hand side is larger than that in the right-hand side.

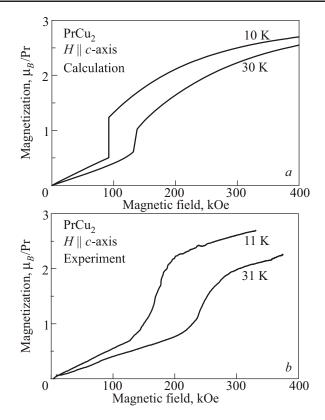


Fig. 104. Calculated (*a*) and experimental (*b*) magnetization curves of PrCu₂, cited from Ref. 141.

$$\mathcal{H} = \mathcal{H}_{CEF} + \mathcal{H}_{Zeeman} - K_M \langle O_2^2 \rangle O_2^2 \,. \tag{20}$$

Figure 104,*a* shows the calculated magnetization curves at 10 and 30 K, where K_M is obtained as 0.3. Here, the magnetization M_{α} ($\alpha = x, y, z$) can be calculated by the following formula:

$$M_{\alpha} = g_J \mu_B \sum_{n} |\langle n | J_{\alpha} | n \rangle| \frac{\mathrm{e}^{-\mathrm{p}E_n}}{\sum_{n} \mathrm{e}^{-\beta E_n}}, \qquad (21)$$

where the eigenvalue E_n and the eigenfunction $|n\rangle$ are determined by diagonalizing the total Hamiltonian in Eq. (20). We note that the *x*-, *y*- and *z*-axes correspond to the *c*-, *a*- and *b*-axes, as shown in Fig. 99,*b*. These calculated results are approximately consistent with the experimental data given in Fig. 104,*b*.

Here we note that the metamagnetic transition occurs when the sign of $\langle O_2^2 \rangle$ changes from negative to positive, as shown in Fig. 105. There are three solutions at zero field for $\langle O_2^2 \rangle$. The ground state possesses the lowest value as indicated by (1) in Fig. 105. The present metamagnetic transition corresponds to the process from (1) to (2). We can say that the present metamagnetic transition corresponds to field-induced ferroquadrupolar ordering.

The metamagnetic transition based on the same quadrupolar interaction is observed in the other compounds: CeCu₂, DyCu₂ and TbCu₂ [144–146].

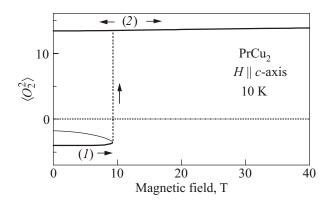


Fig. 105. Field dependence of the calculated quadrupole moment $\langle O_2^2 \rangle$ in PrCu₂, cited from Ref. 141.

7. Change of Fermi surface properties in quantum critical point

The electronic states in Ce, Yb and U compounds can be tuned by applying pressure P and/or magnetic field H. The Néel temperature in the Ce compounds becomes a guiding parameter to tune the electronic state under pressure. The quantum critical point is therefore defined as the electronic state at which the Néel temperature becomes zero at the critical pressure P_c : $T_N \rightarrow 0$ at $P \rightarrow P_c$. We will present the Fermi surface properties as a function of pressure, especially at P_c , for three typical antiferromagnets of CeRh₂Si₂, CeIn₃ and CeRhIn₅.

7.1. Pressure-induced superconductivity in CeRh₂Si₂ based on conduction electrons with the relatively large cyclotron mass

CeRh₂Si₂ crystallizes in a tetragonal ThCr₂Si₂-type structure and orders antiferromagnetically below the Néel temperature $T_N = 36$ K at ambient pressure. The magnetic structure was investigated by neutron diffraction measurements [147], as shown in Fig. 106. Below T_N , the propaga-

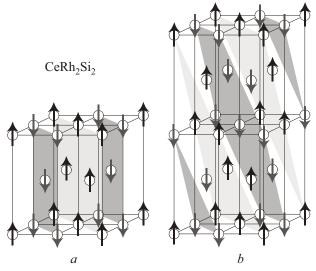


Fig. 106. Magnetic structures of the \mathbf{q}_1 -structure in the temperature range from $T_N = 36$ K to $T'_N = 25$ K (*a*) and the 4**q**-structure below T'_N (*b*) in CeRh₂Si₂, cited from Ref. 147.

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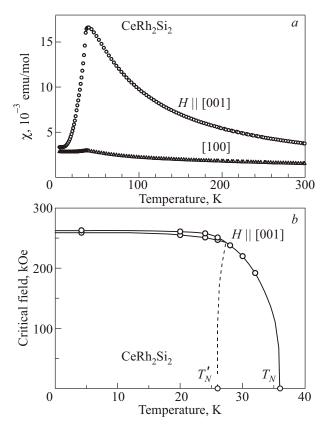


Fig. 107. Temperature dependence of the magnetic susceptibility (*a*) and the magnetic phase diagram (*b*) in CeRh₂Si₂, cited from Ref. 148.

tion vector is $\mathbf{q}_1 = (1/2, 1/2, 0)$, and the magnetic moment is oriented along the [001] direction. Furthermore, the magnetic structure changes to the 4**q** structure with two propagation vectors \mathbf{q}_1 and $\mathbf{q}_2 = (1/2, 1/2, 1/2)$ below $T'_N =$ = 25 K. The magnitude of the ordered moment μ_s is 1.42 μ_B at the corner Ce site of the tetragonal structure and 1.34 μ_B at the body-centered Ce site. The present magnetic structure is clearly reflected in the temperature dependence of the magnetic susceptibility, indicating an easy-axis of magnetization along [001], as shown in Fig. 107,*a*. The magnetic phase diagram for $H \parallel [001]$ is also shown in Fig. 107,*b* [148].

When pressure is applied to CeRh₂Si₂, the Néel temperature $T_N = 36$ K and the magnetic transition temperature T'_N are reduced to 0 K at $P_c \simeq 1.06$ GPa and $P'_c \simeq 2 \simeq 0.6$ GPa, respectively, as shown in Fig. 108. Note that the ordered moment is also reduced with increasing pressure [147], as shown by triangles in Fig. 108. The value of the superconducting transition temperature T_{sc} , which is shown in Fig. 108 as a function of pressure, is enlarged by a factor of ten compared with those of T_N and T'_N . Superconductivity is observed around $P_c \simeq 1.06$ GPa.

The low-temperature resistivity under pressure follows the Fermi liquid form of $\rho = \rho_0 + AT^2$ [149]. Figure 109 shows the T^2 dependence of the electrical resistivity under several constant pressures. Note that the T^2 dependence is satisfied even at around P_c [150,151].

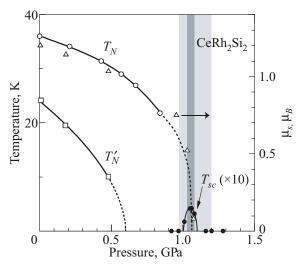


Fig. 108. Pressure dependence of T_N , T'_N , and T_{sc} , shown by open circles, open squares and closed circles, respectively, in CeRh₂Si₂. T_{sc} is enlarged by ten times compared with T_N and T'_N . The ordered moment μ_s is shown by triangles. The data on T'_N and μ_s are cited from Ref. 147.

Figure 110 shows the pressure dependence of A and ρ_0 . The A value has a maximum at 1.0 GPa, very close to P_c . The residual resistivity ρ_0 also has a small anomaly around P_c .

The specific heat measurement under pressure indicated that the electronic specific heat coefficient γ increases almost linearly with increasing pressure from 23 mJ/(K²·mol) at ambient pressure to about 80 mJ/(K²·mol) at P_c [152]. Above P_c , the γ value decreases slightly with increasing pressure. The γ value is found to correlate well with \sqrt{A} .

Superconductivity in CeRh₂Si₂ was first discovered by Movshovich *et al.* for a polycrystal sample [153]. The tran-

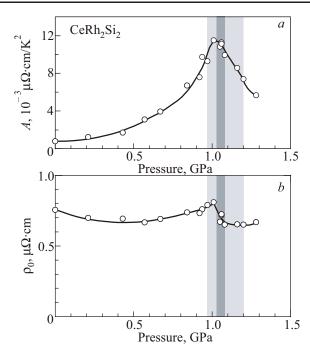


Fig. 110. Pressure dependence of *A* (*a*) and ρ_0 (*b*) in CeRh₂Si₂, cited from Ref. 149.

sition temperature, determined from the onset of the resistivity drop, was $T_{sc} = 0.35$ K, at which superconductivity appeared in the pressure range from 0.6 to 1.6 GPa. Figure 111 shows the low-temperature resistivity for a highquality single crystal sample with $\rho_0 = 0.75 \ \mu\Omega$ cm and $\rho_{RT}/\rho_0 = 100 \ [149]$. An indication of superconductivity appears in the pressure region from 0.97 to 1.20 GPa, which is shown in Fig. 108 as a gray region. As shown in Fig. 111, the resistivity at P = 1.01 and 1.16 GPa decreases rapidly with decreasing temperature below 0.5 K. Zero

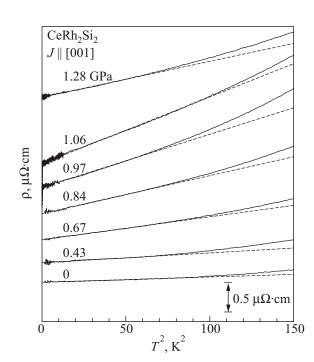


Fig. 109. Quadratic temperature dependence of the electrical resistivity in CeRh₂Si₂ under various pressures, cited from Ref. 149.

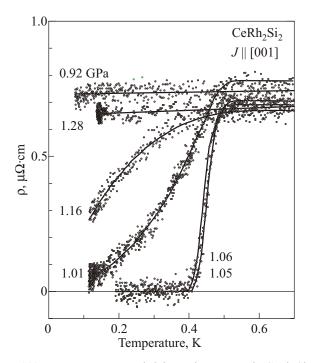


Fig. 111. Low-temperature resistivity under pressure in CeRh₂Si₂, cited from Ref. 149.

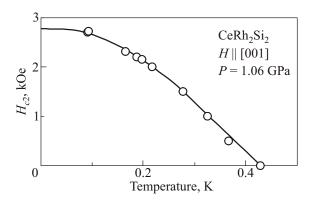


Fig. 112. Temperature dependence of H_{c2} at 1.06 GPa in CeRh₂Si₂, cited from Ref. 149.

resistivity, however, is not attained. The zero resistivity is observed in an extremely narrow pressure region around P_c , which is shown in Fig. 108 as a dark-gray region. Namely, the resistivity at P = 1.05 and 1.06 GPa decreases steeply below 0.5 K and reaches zero at 0.42 K. Note that the onset temperature of superconductivity is 0.4–0.5 K in the pressure region from 0.97 to 1.20 GPa, but the zero resistivity is attained in the pressure region from 1.03 to 1.08 GPa. This implies that homogeneous bulk-superconductivity is realized in an extremely narrow pressure region around $P_c \simeq 1.06$ GPa.

Figure 112 shows the temperature dependence of the upper critical field H_{c2} . The solid line connecting the data in Fig. 112 is a visual guide. The coherence length ξ is simply estimated as 340 Å from a relation of $H_{c2} = \phi_0/2\pi\xi^2$: $H_{c2}(0) = 2.8$ kOe, where ϕ_0 is a quantum fluxoid. Note that the mean free path for the present sample is estimated from the dHvA experiment as about 1000 Å around $P_c \simeq 1.06$ GPa. This indicates that the present sample is close to the clean limit.

The dHvA experiment was carried out under pressure [154,155]. Figures 113,*a* and 113,*b* show the dHvA oscil-

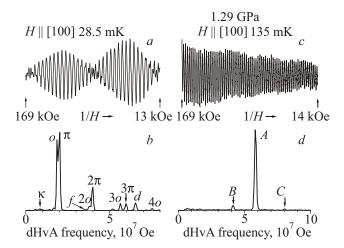


Fig. 113. dHvA oscillation (*a*) and its FFT spectrum at ambient pressure (*b*), dHvA oscillation (*c*) and its FFT spectrum at 1.29 GPa (*d*) in CeRh₂Si₂, cited from Refs. 154, 155.

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lation and its FFT spectrum at ambient pressure and 1.29 GPa, respectively.

The angular dependence of the dHvA branches at ambient pressure in CeRh₂Si₂ is approximately explained by the Fermi surfaces of a non-4f reference compound LaRh₂Si₂, as shown in Fig. 114,a. This is because the 4f electron in CeRh₂Si₂ is localized, as mentioned above; thus, the 4f electron does not significantly contribute to the Fermi surface. These detected dHvA branches are formed by the conduction electrons which break through the antiferromagnetic Brillouin zone boundary and circulate around the original paramagnetic Fermi surface and/or correspond to Fermi surfaces, which are not affected by antiferromagnetic ordering. Antiferromagnetic ordering, however, changes the topology of the Fermi surface. This might be approximated by a band-folding procedure, where the paramagnetic Fermi surface is folded into a small Brillouin zone based on a large magnetic unit cell. The magnetic structure in the ground state is the 4q structure shown in Fig. 106. The magnetic unit cell is eight times larger than the chemical unit cell. Correspondingly, the Brillouin zone of CeRh₂Si₂ in the antiferromagnetic state is reduced to one-eighth of the size of that in the paramagnetic state. It is supposed that dHvA branches such as κ, which are relatively small in dHvA frequency, are thus formed by magnetic ordering. Because the dHvA data are usually obtained over a wide field range from a low field of 25 kOe to a high field of 170 kOe to construct the angular dependence of the dHvA frequency, the experimentally obtained Fermi surfaces consist of the Fermi surfaces in the paramagnetic state and many kinds of small Fermi surfaces produced in the antiferromagnetic state. These are also applicable to the dHvA data in the antiferromagnets of CeIn3 and CeRhIn5 shown later.

Figures 113, c and 113, d indicate the dHvA oscillation and its FFT spectrum at 1.29 GPa, namely, in the paramagnetic state. New branches named A, B, and C appear, which are convincingly explained by the 4f-itinerant Fermi surfaces shown in Fig. 114, b.

The pressure dependence of the dHvA frequency up to 1.54 GPa is plotted in Fig. 115,a. The dHvA branches at ambient pressure, which are identified from the 4flocalized band model, namely, the Fermi surfaces of LaRh₂Si₂, are slightly changed at $P'_c \simeq 0.6$ GPa. Branches o, κ , and ζ disappear completely and new branches named p, q, and r appear above $P'_c \simeq 0.6$ GPa. This is because the magnetic structure changes from the 4q structure to the q_1 structure at $P_c' \simeq 0.6$ GPa, as mentioned above. Branches d and π are, however, unchanged for pressure up to P_c . Note that branches d and π are found at 1.03 GPa, while at 1.08 GPa they disappear completely and a new branch named A appears. With further increasing pressure, two branches named B and C are also detected. These three branches named A, B and C are clearly identified by the 4fitinerant band model, as shown in Fig. 114,b, the detected dHvA frequency is $8.03 \cdot 10^7$ Oe (the corresponding theore-

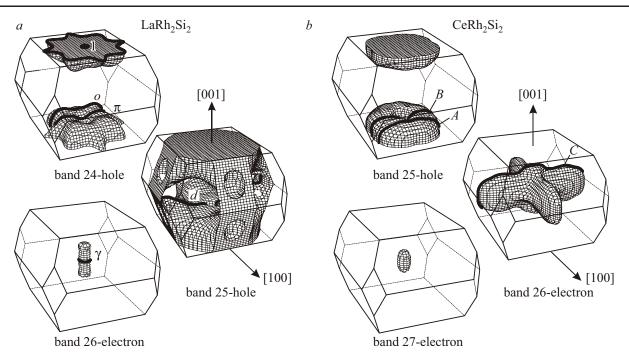


Fig. 114. Theoretical Fermi surfaces in LaRh₂Si₂ (a) and 4f-itinerant CeRh₂Si₂ (b), cited from Refs. 154, 155.

tical dHvA frequency is $9.21 \cdot 10^7$ Oe) for branch *C*, $5.80 \cdot 10^7$ Oe ($4.65 \cdot 10^7$ Oe) for branch *A*, and $4.10 \cdot 10^7$ Oe ($3.43 \cdot 10^7$ Oe) for branch *B*. The Fermi surface of CeRh₂Si₂ in Fig. 114,*b* has one more electron per primitive cell compared with the Fermi surface in LaRh₂Si₂ in Fig. 114,*a*, based on the itinerant electron model for the 4*f* electron. The 4*f* electronic state above P_c in CeRh₂Si₂ is similar to those of CeSn₃, and CeRu₂Si₂ mentioned above.

The cyclotron mass shown in Fig. 115, *b* increases with increasing pressure, reaching $28 m_0$ at 1.03 GPa for branch *d*, which is four to five times larger than that at ambient pressure. Above P_c , the cyclotron masses of branches *A*, *B*,

and *C* are large, ranging from 24 to $34 m_0$. The cyclotron masses are about four times larger than the corresponding band masses. The mass enhancement $m_c^*/m_b \simeq 4$ is consistent with the enhancement of the electronic specific heat coefficient $\gamma/\gamma_b = 4.4$, where $\gamma = 80 \text{ mJ/(K}^2 \cdot \text{mol})$ at 1.3 GPa [152] and $\gamma_b = 18 \text{ mJ/(K}^2 \cdot \text{mol})$.

From these experimental results, it is thus concluded that the detected dHvA frequencies clearly change at $P_c \approx 21.06$ GPa, implying a first-order phase transition. This indicates a discontinuous change in the Fermi surface from 4f-localized to itinerant at P_c , although the Fermi liquid nature holds even at P_c .

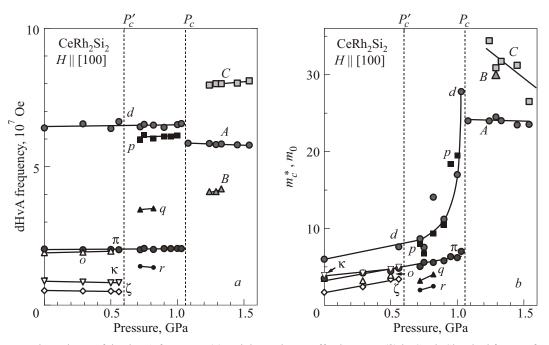


Fig. 115. Pressure dependence of the dHvA frequency (a) and the cyclotron effective mass (b) in CeRh₂Si₂, cited from Refs. 154, 155.

7.2. Pressure-induced heavy fermion superconductivity in CeIn₃

Superconductivity in CeIn₃, which was mentioned in Chap. 3, was also realized under pressure [14]. With increasing pressure, the Néel temperature decreases and reaches zero at a critical pressure of around $P_c \approx 2.6$ GPa, in which the narrow pressure region superconductivity appears below $T_{sc} = 0.21$ K [14,38], as shown in Fig. 116.

The Fermi surface of the antiferromagnet CeIn3 is similar to that of LaIn₃, although the Fermi surface is modified by the antiferromagnetic Brillouin zone boundaries [45]. The antiferromagnetic Brillouin zone in CeIn₃ is the same as that for the face-centered cubic structure. The R point is reduced to the Γ point in this Brillouin zone. The Fermi surface of LaIn₃ consists of two sheets of bands 6 and 7, as shown again in Figs. 117,a and 117,b, respectively [38,39]. The band 7-electron Fermi surface named a is essentially a sphere centered at the R point. The band 6-hole Fermi surface looks complex and possesses the same volume as the band 7-electron Fermi surface, indicating that LaIn3 is a compensated metal. An inner orbit circulating along the hole Fermi surface, denoted by d, is electron in dispersion and is spherical in topology but possesses slender arms along the (111) direction, as in the Fermi surface of copper. The present small electron Fermi surface denoted by d becomes a closed Fermi surface in a similar non-4f reference compound

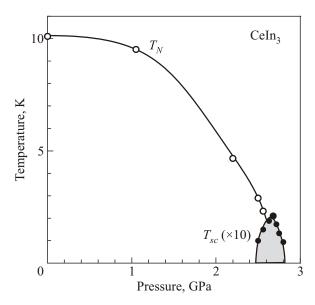


Fig. 116. Phase diagram for the Néel temperature T_N and the superconducting transition temperature T_{sc} in CeIn₃, cited from Ref. 38.

LuIn₃ [49], as shown in Fig. 117,*c*′, where the main Fermi surfaces in LuIn₃ are shown in Figs. 117,*c*,*d*.

In CeIn₃, the detected dHvA branch named d is very close to that of LaIn₃ or LuIn₃. The dHvA branch d in CeIn₃ is, however, observed in the whole angle region, as shown in Fig. 21, and possesses no arms, indicating that

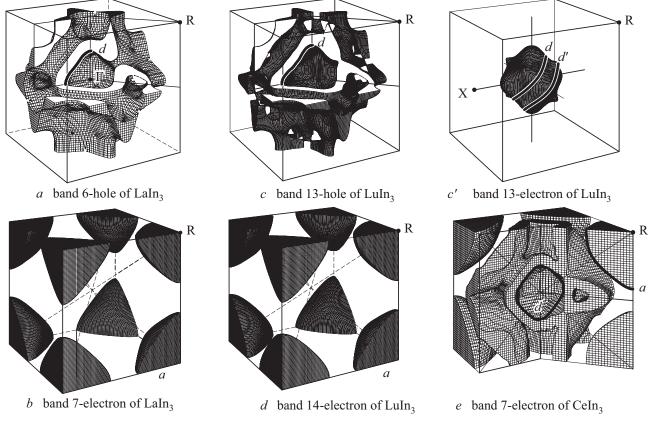


Fig. 117. Fermi surfaces of LaIn₃, LuIn₃, and 4*f*-itinerant CeIn₃, cited from Ref. 38. The vacant space centered at Γ in the band 13-hole Fermi surface of LuIn₃, shown in (*c*), corresponds to the closed band 13-electron Fermi surface shown in (*c*').

the Fermi surface is a closed spherical Fermi surface as in LuIn₃. The cyclotron mass m_c^* of branch d is highly anisotropic regarding the magnetic field direction: $m_c^* = 2-3 m_0$ for the (100) direction and $12-16 m_0$ for (110), as mentioned in Chap. 3 [45,51]. Moreover, two kinds of branches named d and d' are observed only for $H \parallel \langle 111 \rangle$: $m_c^* = 3 m_0$ for branch d and $m_c^* = 13 m_0$ for branch d', compared with $m_c^* = 0.37 m_0$ for branch d in LaIn₃. The large spherical Fermi surface centered at the R point, which is observed in LaIn₃, is not observed in CeIn₃. This is due to the influence of the band folding based on the antiferromagnetic ordering, as discussed by Biasini et al. [156], whereas branch d is not significantly influenced by the antiferromagnetic Brillouin zone except for the disappearance of the arms, because this Fermi surface is small in volume and centered at Γ . The cyclotron mass is strongly enhanced in CeIn3. This is reflected in the electronic specific heat coefficient γ : $\gamma = 150 \text{ mJ/(K}^2 \cdot \text{mol})$ in CeIn₃ and 7.2 mJ/($K^2 \cdot mol$) in LaIn₃ [38].

The dHvA experiment was performed at ambient pressure and also under pressures up to 3GPa [38,157]. Figure 118 shows the pressure dependence of the dHvA frequency *F* and its cyclotron effective mass m_c^* for the magnetic field along the principal axes $H \parallel \langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$. The dHvA frequency and the cyclotron mass for branch *d* increase slightly with increasing pressure: $F = 3.22 \cdot 10^7$ Oe $(m_c^* = 2.9 m_0)$ at ambient pressure and $3.56 \cdot 10^7$ Oe $(4.4 m_0)$ at 2.4 GPa for $H \parallel \langle 100 \rangle$, as shown in Figs. 118,*a* and 118,*a'*. Similar pressure dependences of the dHvA frequency and the cyclotron mass are also observed for $H \parallel \langle 110 \rangle$: $F = 3.60 \cdot 10^7$ Oe $(m_c^* = 17 m_0)$ at ambient pressure and F = $= 4.0 \cdot 10^7$ Oe (21 m₀) at 2.4 GPa, as shown in Figs. 118,b and 118,b'. Here, note that the cyclotron mass of branch d is strongly enhanced for $H \parallel \langle 110 \rangle$ compared with $H \parallel (100)$, although the dHvA frequency is almost the same as that for $H \parallel (100)$. Branch d splits into two branches d and d' for $H \parallel (111)$, as shown in Fig. 118,c. Branch d', which is observed for $H \parallel \langle 111 \rangle$, is considered to be due to the shape of the spherical Fermi surface with humps along the (111) direction as in LuIn₃, as mentioned above. The cyclotron mass of branch d for $H \parallel \langle 111 \rangle$ is $3.0 m_0$ at ambient pressure and $7 m_0$ at 2.4 GPa. On the other hand, branch d' for $H \parallel \langle 111 \rangle$ possesses a relatively large cyclotron mass: $10 m_0$ at ambient pressure and $14 m_0$ at 2.4 GPa. A new branch shown by reverse triangles appears near branch d at 2.86 and 2.90 GPa for $H \parallel (100)$ and at 2.60 GPa for $H \parallel \langle 110 \rangle$.

Interestingly, branch *a* appears abruptly above 2.7 GPa, where the Néel temperature reaches zero and the antiferromagnetic state disappears completely. The appearance of branch *a* indicates that CeIn₃ is paramagnetic above 2.7 GPa. It is very important to elucidate the origin of branch *a* in order to clarify the 4*f* electron character above P_c . Also note that the cyclotron mass of branch *a* is extremely large: $m_c^* \simeq 60m_0$ for $H \parallel \langle 100 \rangle$. Considering the cyclotron effective mass $m_c^* = 0.57m_0$ of branch *a* [39] and the electronic specific heat coefficient $\gamma = 7.2 \text{ mJ/(K}^2 \cdot \text{mol})$ is realized in CeIn₃ around P_c , where the γ value in CeIn₃ at ambient pressure is 150 mJ/(K² \cdot \text{mol}), as mentioned above.

The strongly enhanced cyclotron mass of branch a decreases with increasing pressure, as shown in Fig. 118,a'.

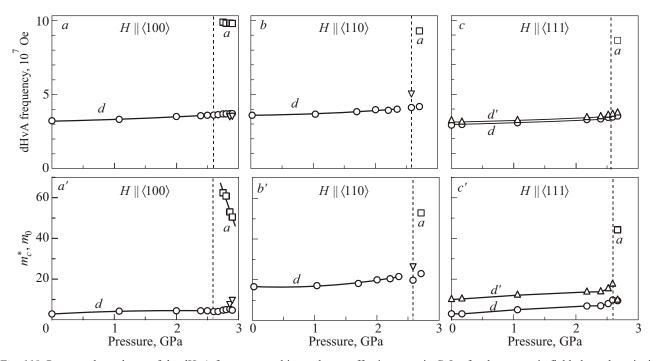


Fig. 118. Pressure dependence of the dHvA frequency and its cyclotron effective mass in CeIn₃ for the magnetic field along the principal axes $H \parallel \langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 111 \rangle$, cited from Ref. 38. Open circles, triangles, and squares indicate branches *d*, *d'*, and *a*, respectively. A new branch indicated by reverse triangles appears at 2.86 and 2.90 GPa for $H \parallel \langle 100 \rangle$ and at 2.60 GPa for $H \parallel \langle 110 \rangle$.

The reduction of the cyclotron mass with increasing pressure is a characteristic feature of the heavy fermion state.

A new dHvA branch named a was observed above 2.7 GPa, which corresponds to a main Fermi surface, judging from the large value of dHvA frequency. The abrupt appearance of branch a implies that the electronic state in CeIn₃ is changed at high pressures and correspondingly the antiferromagnetic state is changed into the paramagnetic state. The paramagnetic state under the magnetic field might be realized not only by a change in the character of the 4f electronic state by applying pressure, but also by a metamagnetic transition from the antiferromagnetic state to the field-induced ferromagnetic (or paramagnetic) state. At ambient pressure, no metamagnetic transition was observed for the magnetic fields of up to 400 kOe. In order to consider a possibility of the metamagnetic transition under pressure, a magnetic phase diagram under pressure was constructed from the temperature dependence of the ac susceptibility. The ac susceptibility was measured using the same experimental setup as that for the dHvA experiment. The antiferromagnetic ordering reflected in the ac susceptibility was observed up to 2.56 GPa, but was not seen above 2.63 GPa. Therefore, the critical pressure P_c of CeIn₃ is between 2.56 and 2.63 GPa, namely, $P_c \simeq$ $\simeq 2.6$ GPa. From these experiments, the phase diagram for the Néel temperature was constructed, as shown in Fig. 119, at 2.20 and 2.56 GPa. The antiferromagnetic state is robust to the magnetic field even slightly below the critical pressure, namely, 2.56 GPa. Note that no metamagnetic transition was observed in the present dHvA measurements. From these experimental results, it is concluded that the present experiments below $P_c \simeq 2.6$ GPa under magnetic fields were performed in the antiferromagnetic state, and the appearance of branch a is not due to the change from the antiferromagnetic state to the field-induced ferromagnetic (or paramagnetic) state but due to the change in the 4f electronic state.

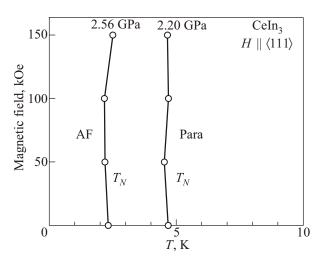


Fig. 119. Magnetic phase diagram for the paramagnetic (Para) and antiferromagnetic (AF) phases at 2.20 and 2.56 GPa for $H \parallel \langle 111 \rangle$ in CeIn₃, cited from Ref. 38.

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A large spherical Fermi surface named a also exists in 4f-itinerant CeIn₃. Figure 117, e shows the band 7-electron Fermi surface based on the 4f-itinerant band model [158]. The theoretical dHvA frequency of branch a in CeIn₃ is 8.82·10⁷ Oe for the 4*f*-itinerant band model for $H \parallel (100)$, while it is $F = 6.84 \cdot 10^7$ Oe for LaIn₃. The Fermi surface of branch a in CeIn₃ on the basis of the 4f-itinerant model is larger than that in LaIn₃ or the 4f-localized model, because the 4f electron considerably contribute to a conduction electron. Namely, the band 6-hole Fermi surface in LaIn₃ is completely occupied by the electron, and the band 7electron Fermi surface in LaIn3 is changed into an enlarged spherical Fermi surface centered at R in the 4f-itinerant CeIn₃, although a complicated multiply connected electron Fermi surface centered at Γ appears in the band 7-electron Fermi surface of the 4f-itinerant CeIn₃. Branches a and d are similar in shape for LaIn3 and the 4f-itinerant CeIn3. Therefore, the volume of the main Fermi surface *a* is very important for determining the character of the 4f electron in CeIn3. The experimentally obtained dHvA frequency of $9.39 \cdot 10^7$ Oe for $H \parallel (100)$ at 2.7 GPa in CeIn₃ is close to $F = 8.82 \cdot 10^7$ Oe in the 4*f*-itinerant model, although the experimental result is larger than the theoretical value. It is important that the volume of the spherical Fermi surface of branch *a* in CeIn₃ above $P_c \simeq 2.6$ GPa is larger than that in LaIn₃, as shown in Fig. 120. This enlarged spherical Fermi surface in CeIn₃ indicates that the 4f electron is itinerant and contributes to the Fermi surface.

It is interesting to compare the dHvA data of CeIn₃ under P = 2.7 GPa with those of ThIn₃ because the number of valence electrons is the same between two compounds [59]. ThIn₃, with the tetravalent electrons ($6d^2 7s^2$) of thorium, is a good candidate for investigating the topology of the 4*f*-itinerant Fermi surface in CeIn₃, which has tetravalent electrons ($4f^1 5d^1 6s^2$) of cerium. The dHvA frequency of the main Fermi surface a in ThIn₃ is very close to that of CeIn₃ at 2.7 GPa, as shown in Fig. 120,*b*. This result also

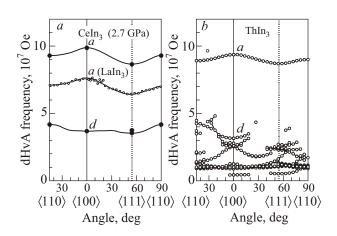


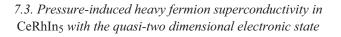
Fig. 120. Angular dependence of the dHvA frequency in CeIn₃ at 2.7 GPa (closed circles), together with those of branch a in LaIn₃ (open circles) [38] (*a*) and ThIn₃ [59] (*b*). Solid lines connecting the data are visual guides.

supports the existence of a 4f-itinerant Fermi surface in CeIn₃ above P_c . These dHvA experiments under pressure indicate that a change of electronic states at P_c is of the first-order.

Superconductivity was observed in the pressure range from 2.50 to 2.81 GPa. Note that the change in the ac susceptibility at the superconducting transition in CeIn₃ is almost the same magnitude as that at the superconducting transition of aluminum with the same volume, indicating that bulk superconductivity is realized in the narrow pressure region from 2.50 to 2.81 GPa. The pressure dependence of the superconducting transition temperature T_{sc} is shown by closed circles in Fig. 116, where the superconducting transition temperature is enlarged by a factor of ten because of a low T_{sc} of about 0.2 K.

Next, the temperature dependence of upper critical field H_{c2} was determined from the ac susceptibility measurement. The superconducting transition temperature under a magnetic field was defined as the temperature corresponding to the onset of the susceptibility drop. Figure 121 shows the temperature dependence of H_{c2} at 2.68 GPa. A solid curve is a visual guide based on Werthamer–Helfand–Hohenberg (WHH) theory [159]. H_{c2} (0) at 2.68 GPa is estimated as 4.4 kOe, indicating a coherence length $\xi = 270$ Å. Heavy fermion superconductivity is realized in the quantum critical region of of CeIn₃.

In an ¹¹⁵In-NQR experiment, no coherence peak is observed at T_{sc} , and the nuclear spin lattice relaxation rate $1/T_1$ at P = 2.50 GPa has a T^3 dependence below $T_{sc} = 0.19$ K, indicating a line-node gap [160]. In the quantum critical region, the electrical resistivity does not follow the Fermi liquid relation $\rho = \rho_0 + AT^n$ (n = 2), which indicates that $n \approx 1.6-1.7$ [161] or 1.6 ± 0.2 [14]. The *d*-wave pairing state is theoretically proposed on the basis of the three-dimensional spin fluctuations near the propagation vector $\mathbf{q} = (1/2, 1/2, 1/2)$ [162].



The detected dHvA branches of CeRhIn₅ are convincingly explained by the result of energy band calculations for LaRhIn₅, as described in Chap. 5. The corresponding topologies of the main Fermi surfaces in CeRhIn₅ are nearly cylindrical, and are found to be approximately the same as those in LaRhIn₅, as shown in Fig. 122,*a*, indicating that the 4*f*-electron in CeRhIn₅ is localized and does not contribute to the Fermi surfaces [77,163,164].

The dHvA experiment was also carried out for CeCoIn5 [79,165–167], as described in Chap. 5. The detected dHvA branches are consistent with the 4f-itinerant band model. The main Fermi surfaces in CeCoIn5 are also nearly cylindrical, as shown in Fig. 122, b. The topologies of the two kinds of cylindrical electron Fermi surfaces in CeCoIn5 are similar to those in LaRhIn₅ (CeRhIn₅), but the Fermi surfaces of CeCoIn5 are larger than those of LaRhIn5 in volume. Moreover, the band 13-hole Fermi surface in LaRhIn5, not shown in Fig. 122, is considerably reduced in volume for CeCoIn₅. This is because one 4f-electron in each Ce site becomes a valence electron in CeCoIn5 and contributes to the Fermi surface. The contribution of the 4f electron to the density of states at the Fermi energy is about 60%. The corresponding cyclotron masses of $5-87 m_0$ in CeCoIn₅ are extremely large, reflecting a large γ value of $1070 \text{ mJ/(K}^2 \cdot \text{mol})$ [101,102].

Keeping in mind that the 4f electron is localized in the antiferromagnet CeRhIn₅ but becomes itinerant at low temperatures in CeCoIn₅, the dHvA experiment in CeRhIn₅ was carried out under pressure [78]. Figures 123,*a* and 123,*b* show the dHvA oscillation in the field range from 30 to 169 kOe and its FFT spectrum, respec-

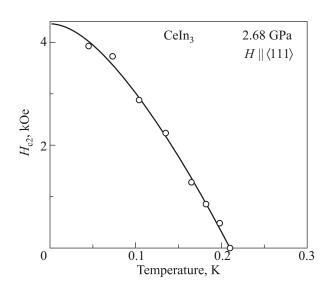


Fig. 121. Temperature dependence of the upper critical field H_{c2} in CeIn₃ at 2.68 GPa, cited from Ref. 38.

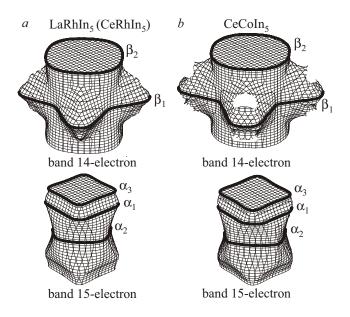
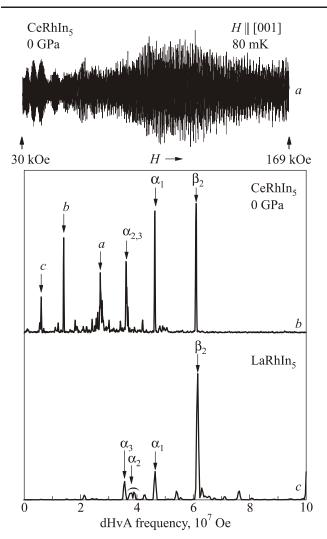
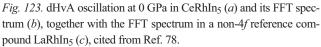


Fig. 122. Theoretical Fermi surfaces in LaRhIn₅ (CeRhIn₅) (a) and CeCoIn₅ (b), cited from Ref. 78. Small Fermi surfaces are not shown.





tively, at ambient pressure. Two kinds of main cylindrical Fermi surfaces named α_i (i = 1, 2, 3) and β_2 are detected. The dHvA frequencies F and the cyclotron effective masses m_c^* are $F = 6.13 \cdot 10^7$ Oe ($m_c^* = 5.5 m_0$) in β_2 , $4.67 \cdot 10^7$ Oe ($6.0 m_0$) in α_1 , and $3.67 \cdot 10^7$ Oe ($3.5 m_0$) in $\alpha_{2,3}$. These dHvA frequencies are in good agreement with those of LaRhIn5, shown in Fig. 123,*c*: $F = 6.13 \cdot 10^7$ Oe ($0.73 m_0$) in β_2 , $4.62 \cdot 10^7$ Oe ($0.69 m_0$) in α_1 , $3.76 \cdot 10^7$ Oe ($0.51 m_0$) in α_2 , and $3.56 \cdot 10^7$ Oe ($0.64 m_0$) in α_3 [77]. The mass enhancement observed in CeRhIn5 is also consistent with the γ value: $\gamma = 50-60 \text{ mJ/(K}^2 \cdot \text{mol)}$ in CeRhIn5 and 5.7 mJ/(K² \cdot \text{mol}) in LaRhIn5 [77,168].

Next, the dHvA oscillation in the field range from 82 to 169 kOe and its FFT spectrum at pressure P = 2.9 GPa are shown in Figs. 124,*a* and 124,*b*, respectively. Four kinds of dHvA branches are observed: $F = 5.43 \cdot 10^7$ Oe ($m_c^* = 23 m_0$) in α_1 , $4.96 \cdot 10^7$ Oe ($30 m_0$) in α_2 , $4.58 \cdot 10^7$ Oe ($24 m_0$) in c α_3 , and $1.98 \cdot 10^7$ Oe ($9 m_0$) in branch *A*. The dHvA frequencies of these branches are larger than those at ambient pressure, but are approximately the same as those of

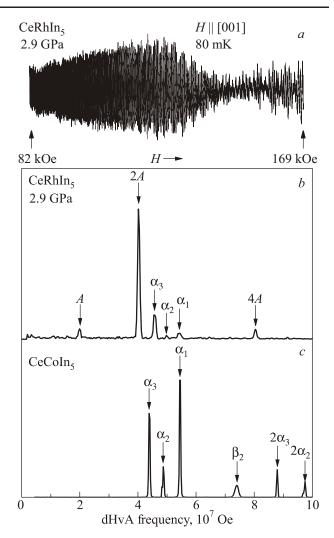


Fig. 124. dHvA oscillation at 2.9 GPa in CeRhIn₅ (*a*) and its FFT spectrum (*b*), together with the FFT spectrum in CeCoIn₅ at ambient pressure (*c*), cited from Ref. 78.

CeCoIn₅ at ambient pressure: $F = 5.56 \cdot 10^7$ Oe $(15 m_0)$ in α_1 , $4.53 \cdot 10^7$ Oe $(18 m_0)$ in α_2 , and $4.24 \cdot 10^7$ Oe $(8.4 m_0)$ in α_3 , as shown in Fig. 124, *c* [79]. The origin of branch *A* is not clear, but it is close to branch ε with $F = 0.79 \cdot 10^7$ Oe in CeCoIn₅, which was, however, not observed experimentally along $H \parallel [001]$ in CeCoIn₅ [79]. Here, branch ε in CeCoIn₅ is identified as a band 13-hole nearly spherical Fermi surface, not shown in Fig. 122, *b*.

To elucidate a change in the Fermi surface properties under pressure, the pressure dependences of the dHvA frequency and the cyclotron mass were measured, as shown in Figs. 125,*a*,*b*, respectively. The dHvA frequencies for the main dHvA branches named β_2 , α_1 and $\alpha_{2,3}$, together with those for branches named *a*, *b*, and *c* in Fig. 125,*a*, are approximately unchanged up to about 2.3 GPa [78]. These branches, however, disappear completely at 2.35 GPa, and another two branches with $F = 4.23 \cdot 10^7$ Oe ($m_c^* \approx 30 m_0$) and $4.03 \cdot 10^7$ Oe ($20 m_0$) appear. Furthermore, new branches α_3 and *A* appear abruptly at 2.4 GPa, which are connected with the branches at 2.9 GPa.

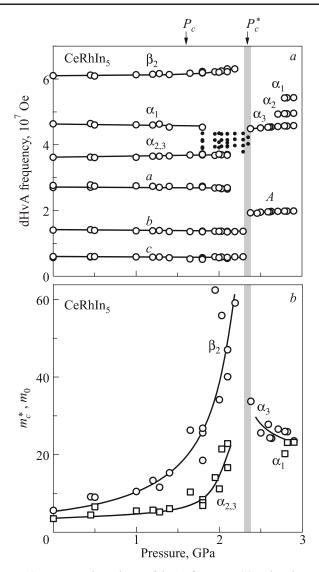


Fig. 125. Pressure dependence of dHvA frequency (*a*) and cyclotron mass (*b*) in CeRhIn₅, cited from Ref. 78.

Note that the branches at 2.35 GPa appear from 1.80 to 2.35 GPa, which are shown by small closed circles in Fig. 125. The origin of these branches is unknown, but they might be related to the magnetic and/or electronic state, because at a zero field the antiferromagnetic ordering disappears above $P_c \simeq 2.0$ GPa but persists up to $P_c^* \simeq$ $\simeq 2.4$ GPa in magnetic fields, as mentioned above. It is observed from the neutron-scattering experiment that the helical magnetic structure and the ordered moment remain up to 1.63 GPa [86]. Furthermore, the present dHvA experiment was carried out in high magnetic fields up to 169 kOe. Even in these high fields, CeRhIn₅ is in the antiferromagnetic state at ambient pressure, because the magnetization for $H \parallel [001]$ indicated neither a metamagnetic transition nor a saturated feature in magnetic fields of up to 500 kOe [169]. The dHvA branches a, b, etc., which are not observed in LaRhIn5, are characteristic in the antiferromagnet CeRhIn₅. These branches are observed continuously in the present measured field range even under pressures up to approximately P_c^* , indicating that an antiferromagnetic state persists up to $P_c^* \approx 2.4$ GPa in the present dHvA experiment.

As shown in Fig. 125,b, the cyclotron masses of the main branches β_2 and $\alpha_{2,3}$ increase rapidly above 1.6 GPa, where superconductivity occurs: $5.5 m_0$ at ambient pressure, $20 m_0$ at 1.6 GPa, and $60 m_0$ at 2.2 GPa for branch β_2 , where the cyclotron mass was determined in the field range from 100 to 169 kOe, namely, at an effective field $H_{\rm eff}$ = = 126 kOe. This is approximately consistent with the pressure dependence of the γ value: 50–60 mJ/(K²·mol) at ambient pressure and 380 mJ/(K²·mol) at 2.1 GPa [168]. On the other hand, the cyclotron mass of the new branch α_3 , which was observed above 2.4 GPa, decreases slightly with increasing pressure: about $30m_0$ at 2.4 GPa and $24m_0$ at 2.9 GPa. Branch β_2 was, however, not detected above 2.4 GPa. This is mainly due to the existence of a large cyclotron effective mass close to $100 m_0$. Anyway, it is remarkable that the pressure dependence of the cyclotron mass indicates a divergent tendency at $P_c^* \simeq 2.4$ GPa.

It has also been reported from other experiments that the residual resistivity ρ_0 [87], and the \sqrt{A} value become maximum at P_c^* [170].

It is concluded from the present dHvA experiment that the Fermi surface in CeRhIn₅ under pressure is changed from a 4*f*-localized Fermi surface to a 4*f*-itinerant Fermi surface. A notable change in the Fermi surface occurs $P_c^* \simeq 2.4$ GPa, revealing a first-order phase transition. Pressure-induced superconductivity is not related to the topology of the Fermi surface, but to the heavy fermion state, although the Fermi surface is very similar between $P < P_c^*$ and $P > P_c^*$.

8. Split Fermi surfaces in the non-centrosymmetric crystal structure

Recently superconductivity in the non-centrosymmetric crystal structure has been reported in CePt₃Si [171,172] with the tetragonal structure (P4mm), UIr [18,173] with the monoclinic structure ($P2_1$), CeRhSi₃ [174–176], CeIrSi₃ [23,29,177], CeCoGe₃ [178,179] and CeIrGe₃ [180] with the tetragonal BaNiSn₃ type structure (I4mm). We show in Fig. 126 the crystal structure of CePt₃Si and CeIrSi₃, which lack inversion symmetry along the tetragonal [001] direction (*c*-axis). In CeIrSi₃, the Ce atoms occupy the four corners and the body center of the tetragonal structure, similar to the well-known tetragonal CeCu₂Si₂ (ThCr₂Si₂-type), but the Ir and Si atoms lack inversion symmetry along the [001] direction.

Inversion is an essential symmetry for the formation of Cooper pairs. In non-centrosymmetric metals, a splitting of Fermi surfaces with different spins occurs, restricting the possible Cooper pair states which can be formed keeping the total momentum zero. In the case of CePt₃Si, CeRhSi₃, CeIrSi₃, CeCoGe₃ and CeIrGe₃, split Fermi surfaces,

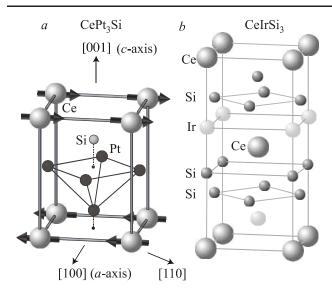


Fig. 126. Crystal and magnetic structure of CePt₃Si (a), and the crystal structure of CeIrSi₃ (b), which also lack inversion symmetry along the [001] direction.

which are very similar to each other in topology but different in volume, are formed due to the presence of a Rashbatype antisymmetric spin-orbit interaction:

$$\mathcal{H}_{so} = -\frac{\hbar}{4m^{*2}c_2} (\nabla V(\mathbf{r}) \times \mathbf{p}) \cdot \boldsymbol{\sigma} = \alpha(\mathbf{n} \times \mathbf{p}) \cdot \boldsymbol{\sigma} = \alpha \mathbf{p}_{\perp} \cdot \boldsymbol{\sigma} (22)$$

where α denotes the strength of the spin-orbit coupling, **n** is a unit vector derived from $\nabla V(\mathbf{r})$, which lies along the [001] direction (*c*-axis) for these compounds, and $\boldsymbol{\sigma}$ is the Pauli matrix [181,182]. This additional term in the electron Hamiltonian separates the spin degenerate bands into two given by [181,183,184],

$$\varepsilon_{p\pm} = \frac{\mathbf{p}^2}{2m^*} \mp |\alpha \mathbf{p}_{\perp}|, \qquad (23)$$

where $\mathbf{p}_{\perp} = (p_{y}, -p_{x}, 0)$. This splitting appears in the absence of a magnetic field and introduces a characteristic momentum-dependent spin structure to the electronic states, as shown in Fig. 127,*c*, which is compared with a spherical Fermi surface with degenerated up and down spin states in Fig. 127,*a*. Note that the spins of the conduction electrons are rotated for the direction of the effective magnetic field, $\mathbf{n} \times \mathbf{p}$, clockwise or anti-clockwise, depending on the up and down spin states. For comparison, in Fig. 127,*b*, we show the well-known Zeeman splitting, where the degenerated Fermi surface is split into two Fermi surfaces corresponding to a

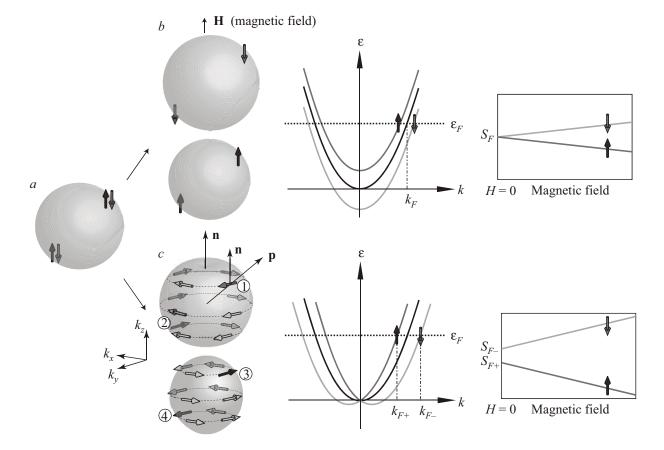


Fig. 127. Spherical Fermi surface with degenerated up (\uparrow) and down (\downarrow) spin states (*a*), and the Fermi surface and the corresponding energy bands are split into two components depending on the up and down spin states when the magnetic field *H* is applied to the material. The maximum cross-sectional areas *S_F* are also split into two components as a function of the magnetic field, well known as Zeeman splitting (*b*). The Fermi surface and the corresponding energy band are split into two components depending on the up and down spin states due to the antisymmetric spin-orbit interaction even when *H* = 0. The field dependence of the maximum cross-sectional areas *S_F*- and *S_{F+}* are also shown in the non-centrosymmetric structure (*c*).

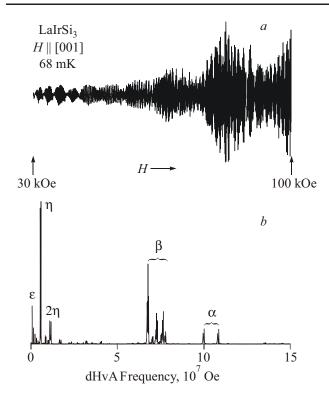


Fig. 128. Typical dHvA oscillation for $H \parallel [001]$ (*a*) and its FFT spectrum (*b*) in LaIrSi₃, cited from [23].

majority and minority spin, respectively, for a given quantization axis parallel to an applied magnetic field.

Due to the Fermi surface splitting in Fig. 127,*c*, the dHvA frequency *F* is split into two dHvA frequencies, F_+ and F_- . Using the relations of $\varepsilon_F = \hbar^2 k_F^2 / 2m_c^*$, $S_F = \pi k_F^2$, and $S_F = (2\pi e/c\hbar)F$, we obtain from Eq. (21)

$$|F_{+} - F_{-}| = \frac{2c}{\hbar e} |\alpha p_{\perp}| m_{c}^{*}.$$
 (24)

We can thus determine the magnitude of the antisymmetric spin-orbit interaction $2|\alpha p_{\perp}|$ via the dHvA experiment.

As noted above, the existence of inversion symmetry in the crystal structure is believed to be an important factor for the formation of Cooper pairs, particular for the spintriplet configuration. For example, parallel spin pairing is prohibited in the non-centrosymmetric structure because one conduction electron with a momentum **p** and an upspin state, named ①, and the other conduction electron with a momentum $-\mathbf{p}$ and an up-spin state, named ④, belong to two different Fermi surfaces, as shown in Fig. 127,*c*. The possible existence of a spin-triplet pairing state in the non-centrosymmetric tetragonal crystal structure was, however, proposed theoretically [185,186].

First, we show the Fermi surface properties of LaTX₃ (T = Co, Rh, Ir and X = Si, Ge). In Fig. 128,*a* we show the typical dHvA oscillations of LaIrSi₃ for the magnetic field *H* along the [001] direction (*c*-axis) and its FFT spectrum [23]. The observed dHvA branches, α , β , ε , and η , are depicted in Fig. 128,*b*. The signal α with the largest dHvA frequency is clearly split into two branches, each of which separates once more into two branches. The former splitting is due to antisymmetric spin-orbit coupling, while the latter one is mainly due to the slight corrugation of each Fermi surface, possessing two extremal (maximum and minimum) cross-sections.

Figures 129,*a* and 129,*b* show the angular dependence of the dHvA frequency in LaIrSi₃, together with the theoretical one [23]. The detected dHvA branches are well explained by the result of the energy band calculation. The corresponding theoretical Fermi surfaces are shown in Fig. 130. The dHvA branches are identified as follows:

— branches α and η correspond to outer and inner orbits of the electron-Fermi surfaces belonging to band 41 and 42, respectively. These Fermi surfaces have a void around the center of the Brillouin zone (Γ point). Also the branches α' and α'' are due to these Fermi surfaces;

— branch β is due to the hole-Fermi surfaces corresponding to band 39 and 40;

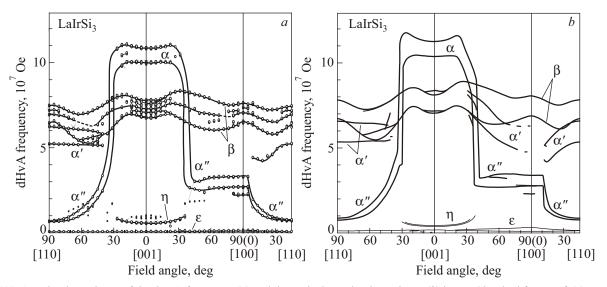


Fig. 129. Angular dependence of the dHvA frequency (a) and theoretical angular dependence (b) in LaIrSi₃, cited from Ref. 23.

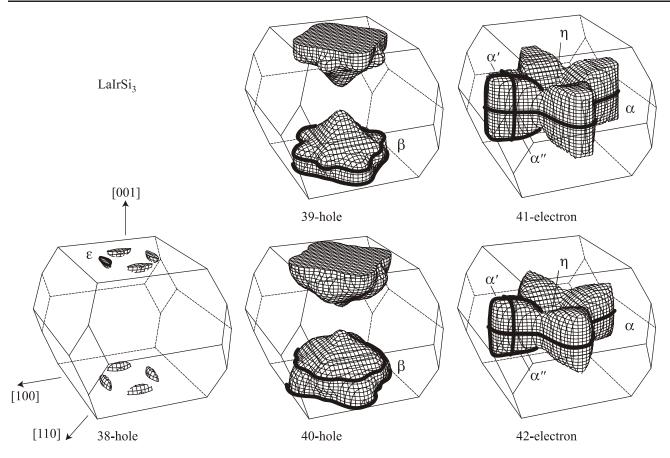


Fig. 130. Theoretical Fermi surfaces in LaIrSi₃, cited from Ref. 23.

— branch ϵ originates from the hole-Fermi surface of band 38.

We determine the cyclotron effective mass m_c^* from the temperature dependence of the dHvA amplitude and find, for example, $1.03 m_0$ for branch α in the magnetic field along the [001] direction. Fermi surface properties are summarized in Table 9, where the dHvA data for LaTGe₃ (T: Co, Rh, Ir) and a paramagnet PrCoGe₃ with the singlet CEF scheme are also presented.

The dHvA results of LaIrSi₃ are also compared with that of LaIrGe₃, as shown in Fig. 131 [26]. The valence electrons are $3s^23p^2$ in Si and $4s^24p^2$ in Ge. The dHvA

frequency of LaIrGe₃ is slightly smaller than that of LaIrSi₃, because the lattice constants of a = 4.4343 Å and c = 10.0638 Å in LaIrGe₃ are larger than a = 4.2820 Å and c = 9.8391 Å in LaIrSi₃ and the corresponding Brillouin zone of LaIrGe₃ has a smaller volume than that of LaIrSi₃. However, the $2|\alpha p_{\perp}|$ value is almost the same for the two compounds as listed in Table 9.

We now discuss the Fermi surface properties and the magnitude of the antisymmetric spin-orbit coupling in LaTGe₃ (T: Co, Rh, Ir) [26]. Figure 132 shows the angular dependence of the dHvA frequency. The topologies of the Fermi surfaces are essentially the same in LaTGe₃(T = Co,

Table 9. Experimental dHvA frequency *F*, the cyclotron mass m_c^* , and the antisymmetric spin-orbit interaction $2|\alpha p_{\perp}|$ for $H \parallel [001]$ in LaTX₃ (T = Co, Rh, Ir and X = Si, Ge) and PrCoGe₃, cited from Ref. 26

	branch α			branch β		
	<i>F</i> , 10 ⁷ Oe	m_{c}^{*}, m_{0}	$2 \alpha p_{\perp} , K$	<i>F</i> , 10 ⁷ Oe	m_{c}^{*}, m_{0}	$2 \alpha p_{\perp} , K$
LaCoGe ₃	9.15 8.74	1.19 1.20	461	7.09 6.72	1.28 1.11	416
LaRhGe ₃	10.4 10.0	1.04 1.04	511	6.98 6.67	0.83 0.85	505
LaIrGe ₃	10.4 9.29	1.13 1.51	1090	7.25 6.22	1.32 1.29	1066
LaIrSi ₃	10.9 10.0	0.97 1.03	1100	7.64 6.76	0.97 0.92	1250
PrCoGe ₃	9.04 8.64	1.80 1.97	284	7.13 6.71	2.04 1.70	302

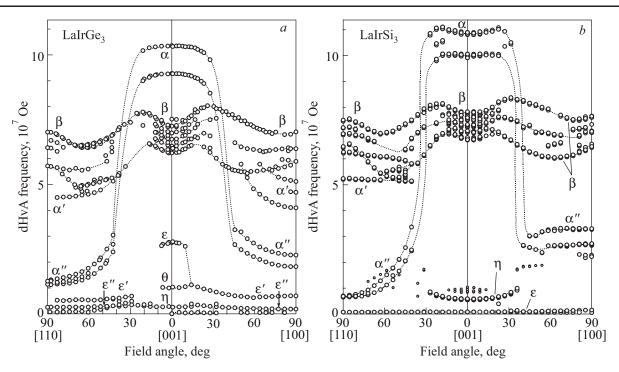


Fig. 131. Angular dependence of the dHvA frequency in LaIrGe₃ (a) and LaIrSi₃ (b), cited from Ref. 26.

Rh, Ir). This is plausible in view of the fact that the valence electron configurations do not differ in LaTGe₃: $3d^7 4s^2$ in Co, $4d^8 5s^1$ in Rh and $5d^9$ in Ir. Note, however, that the dHvA frequency of branch α in LaCoGe₃ is smaller than those in both LaRhGe₃ and LaIrGe₃, and the width of the split dHvA frequencies, $|F_+ - F_-|$, for branch α in LaIrGe₃ is larger than those in LaCoGe₃ and LaRhGe₃. Hence the Fermi surface in LaCoGe₃ is slightly smaller in volume than those in LaRhGe₃ and LaIrGe₃. Moreover, we may conclude that the antisymmetric spin-orbit coupling $2|\alpha p_{\perp}|$ in LaIrGe₃ is larger than in LaCoGe₃ and LaRhGe₃: $2|\alpha p_{\perp}| = 460$ K in LaCoGe₃, 510 K in LaRhGe₃ and 1090 K in LaIrGe₃ for branch α . Precise values for branches α and β are given in Table 9.

In this series of dHvA experiments, the potentials can be varied by changing the transition metal ions T = Co, Rh and Ir in LaTGe₃. This may explain the reason why the antisymmetric spin-orbit coupling in LaIrGe₃ is relatively large compared with those in LaCoGe₃ and LaRhGe₃. The difference is connected with both the characteristic radial wave function $\phi(r)$ of Ir-5*d* electrons and the relatively large effective atomic number Z_{eff} in Ir close to the nuclear center. Here we simply calculate the spin-orbit interaction for the *d* electrons, not in the lattice but in the isolated atom, following the method presented by Koelling and Harmon [187].

Figure 133 shows the *r*-dependence of the radial wave function $r\phi(r)$ for Ir-5*d*, Rh-4*d* and Co-3*d* electrons. We

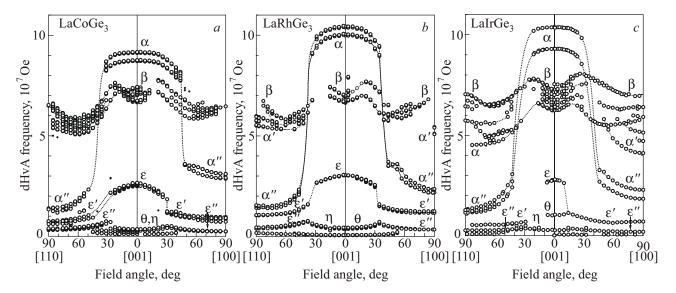


Fig. 132. Angular dependence of the dHvA frequency in LaCoGe₃ (a), LaRhGe₃ (b) and LaIrGe₃ (c), cited from Ref. 26.

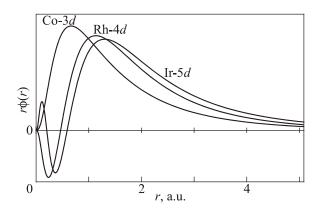


Fig. 133. Radial wave function $r\phi(r)$ as a function of the distance *r* for Ir-5*d*, Rh-4*d* and Co-3*d* electrons in the isolated atoms, cited from Ref. 26.

assumed the valence electrons to be $3d^74s^2$ in Co, $4d^75s^2$ in Rh and $5d^76s^2$ in Ir. The $r\phi(r)$ function of Ir-5d electrons possesses a maximum at r = 0.11 a.u. (atomic units), very close to the atomic center, while the corresponding distance r is 0.37 a.u. in Rh-4d and 0.66 a.u. in Co-3d, farther from the atomic center.

Next we will consider the potential V(r), which corresponds to the sum of the nuclear potential, and the classical Coulomb and exchange-correlation potentials derived from electrons. Figure 134,*a* shows the coupling constant of the spin-orbit interaction, $r^2 dV(r)/dr$. Simply thinking, this value corresponds to the effective atomic number Z_{eff} in

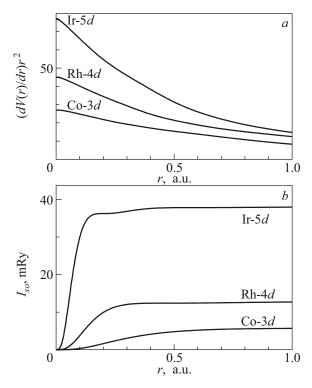


Fig. 134. Coupling constant of the spin-orbit interaction $(dV(r)/dr)r^2$ (*a*) and the spin-orbit interaction I_{so} as a function of the distance r (*b*) for Ir-5*d*, Rh-4*d* and Co-3*d* electrons in the isolated atoms, cited from Ref. 26.

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the potential $V(r) = -Z_{\text{eff}}/r$. Z_{eff} at r = 0 is very close to the atomic number Z in the nuclear potential V(r) = -Z/r, where Z is 77, 45 and 27 for Ir, Rh and Co, respectively. As seen in Fig. 134,*a*, the coupling constant of the spin-orbit interaction is reduced strongly as a function of the distance r, because of screening of the nuclear charge by the electron cloud, reaching $Z_{\text{eff}} \rightarrow 1$ for $r \rightarrow \infty$.

Finally we calculate the spin-orbit interaction, *I*_{so}:

$$I_{so}(r) = \frac{\hbar^2}{2m^2c^2} \int_0^r \frac{1}{r'} \frac{dV(r')}{dr'} |r'\phi(r')|^2 dr', \quad (25)$$

which is shown in Fig. 134,*b* as a function of the distance *r*. I_{so} becomes constant at about 1.0 a.u., but approximately reaches this constant value at r = 0.11 a.u. for Ir-5*d*, 0.37 a.u. for Rh-4*d* and 0.66 a.u. for Co-3*d*, where the corresponding radial wave functions possess the extremal values, as mentioned above. The spin-orbit coupling is, thus, obtained to be 38.0 mRy (6000 K) for Ir-5*d*, 12.8 mRy (2020 K) for Rh-4*d* and 5.72 mRy (900 K) for Co-3*d*. These calculations suggest that the radial wave function of Ir-5*d* electrons have a larger weight at distances close to the center, compared with those of Rh-4*d* and Co-3*d*, and develops a relatively strong spin-orbit coupling in Ir, closely connected with the relatively large effective atomic number Z_{eff} for Ir at the distance *r* close to the atomic center.

This result of the spin-orbit interaction for an isolated atom is applied to the non-centrosymmetric crystal lattice. In this case, the degenerate Fermi surface is split into two Fermi surfaces of which the magnitude of the antisymmetric spin-orbit interaction is approximately proportional to the spin-orbit coupling of Eq. (25), because the same potential is in principle used in the band structure calculation. The *d* electrons in the transition atom as well as the 5delectrons in the La atom and the other electrons contribute to the conduction electrons in LaTGe3. This is the main reason why the antisymmetric spin-orbit interaction $2|\alpha p_{\perp}|$ in LaIrGe3 and LaIrSi3 is larger than in LaCoGe3 and LaRhGe₃. These results may also be applied to Li₂Pt₃B and Li₂Pd₃B [188], where the spin-orbit coupling in Li₂Pt₃B, which originates mainly form Pt-5d electrons, is expected to be larger than the contribution from Pd-4d orbitals in Li₂Pd₃B. The magnitude of the antisymmetric spin-orbit coupling of CeIrSi3 cannot be determined from the result of the present dHvA experiments, but can be roughly estimated from the γ value: we estimate $2|\alpha p_{\perp}| \simeq$ $\simeq 40$ K from $\gamma = 120$ mJ/(K²·mol) in CeIrSi₃ based on $2|\alpha p_{\perp}| \simeq 1000$ K and $\gamma = 4.5$ mJ/(K²·mol) for LaIrSi₃ [23]. This value is much larger than the superconducting transition temperature $T_{sc} = 1.6$ K at 2.65 GPa in CeIrSi₃, as shown below.

To understand the electronic properties of CeTX₃, we plot the Néel temperature and the electronic specific heat coefficient γ as a function of the average lattice constant $\sqrt[3]{a^2c}$ for CeTX₃, in Figs. 135,*a* and 135,*b*, respectively. It

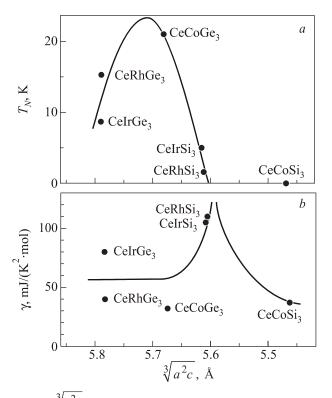


Fig. 135. $\sqrt[3]{a^2c}$ -dependence of the Néel temperature (*a*) and the γ value (*b*) in CeTSi₃ and CeTGe₃ (T: Co, Rh, Ir), cited from Refs. 23, 176, 189, 190.

is noted that the lattice constant on the left hand side is larger than that in the right hand side (data from Refs. 23, 176, 189, 190). The observed relation of T_N vs $\sqrt[3]{a^2c}$ in Fig. 135,*a* roughly corresponds to the Doniach phase diagram [4], which indicates a competition between the RKKY interaction and the Kondo screening effect, as mentioned in Chap. 1. CeRhSi₃ and CeIrSi₃ are close to the quantum critical point in the electronic state, with a relatively large γ value, as shown in Fig. 135,*b*. In fact, the Néel temperatures in CeRhSi₃ and CeIrSi₃ become zero at a relatively small value of pressure, $P_c \simeq 2$ GPa.

Figure 136 shows the pressure dependence of the Néel temperature T_N , the superconducting transition temperature T_{sc} , the specific heat jump at T_{sc} , $\Delta C_{ac}/C_{ac}(T_{sc})$, and the upper critical field at 0 K, $H_{c2}(0)$ for $H \parallel [001]$ [191,192]. The critical pressure, where the Néel temperature becomes zero, is estimated to be $P_c = 2.25$ GPa. The superconducting transition temperature becomes maximum at about 2.6 GPa, as shown in Fig. 136,*a*. Simultaneously, the jump of the specific heat at T_{sc} becomes extremely large at 2.58 GPa: $\Delta C_{ac}/C_{ac}(T_{sc}) = 5.8$ as shown in Fig. 136,*b*, indicating a strong-coupling superconductivity for CeIrSi₃. The upper critical field $H_{c2}(0)$ for $H \parallel [001]$ becomes maximum at $P_{c2}^* = 2.63$ GPa, as shown in Fig. 136,*c*.

As shown in Fig. 137, the upper critical field deviates substantially between $H \parallel [001]$ and [110] [191]. The superconducting properties become highly anisotropic: $-dH_{c2}/dT =$ = 170 kOe/K at $T_{sc} = 1.56$ K, and $H_{c2}(0) \approx 450$ kOe for

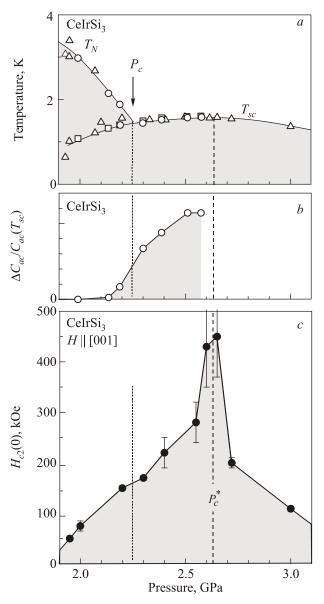


Fig. 136. Pressure dependences of the Néel temperature T_N and superconducting transition temperature $T_{sc}(a)$, specific heat jump $\Delta C_{ac}/C_{ac}(T_{sc})(b)$, cited from Ref. 192, and the upper critical field $H_{c2}(0)$ for $H \parallel [001](c)$ in CeIrSi₃, cited from Ref. 191.

H || [001], and $-dH_{c2}/dT = 145$ kOe/K at $T_{sc} = 1.59$ K, and $H_{c2}(0) = 95$ kOe for $H \parallel [110]$ at 2.65 GPa. The upper critical field H_{c2} for $H \parallel [110]$ shows strong signs of Pauli paramagnetic suppression with decreasing temperature because the orbital limiting field $H_{orb} = -0.73(dH_{c2}/dT)T_{sc})$ is estimated to be 170 kOe [159], which is larger than $H_{c2}(0) = 95$ kOe for $H \parallel [110]$. On the other hand, the upper critical field $H \parallel [001]$ is not destroyed by spin polarization based on Zeeman coupling but possesses an upturn curvature below 1 K, reflecting a strong-coupling nature of superconductivity. This is because all the spins of conduction electrons are perpendicular to the magnetic field direction of $H \parallel [001]$, as shown in Fig. 127,*c*, revealing that the spin susceptibility for $H \parallel [001]$ is unchanged below T_{sc} in this non-centro-

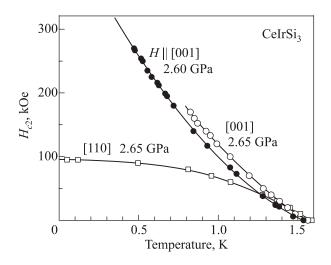


Fig. 137. Temperature dependence of upper critical field H_{c2} for the magnetic field along [001] at 2.60 GPa, together with those at 2.65 GPa in CeIrSi₃, cited from Ref. 191.

symmetric crystal structure and then the Pauli paramagnetic suppression of H_{c2} is not realized for $H \parallel [001]$. Moreover, the electronic state at P_c^* is found to correspond to an antiferromagnetic quantum critical point from the result of the ²⁹Si-NMR experiment [193].

The magnetic quantum phase transition thus occurs in CeIrSi₃ at $P_c^* \simeq 2.6$ GPa, coinciding with a huge H_{c2} value of $H_{c2}(0) \simeq 450$ kOe for $H \parallel [001]$ for a low $T_{sc} = 1.6$ K value. A similar result is also obtained for CeRhSi₃ [174,175].

9. de Haas-van Alphen oscillation in the superconducting mixed state

To our surprise, the dHvA oscillation was observed even in the superconducting mixed state of type II-superconductors [194]. Here we show the dHvA oscillation in felectron superconductors CeRu₂ [195], CeCoIn₅ [79], URu₂Si₂ [196] and UPd₂Al₃ [197] in both the normal and superconducting mixed states, as shown in Fig. 138. The main Fermi surface named α_i in CeCoIn₅ was detected in magnetic fields very close to H_{c2} [79]. Surprisingly, a small Fermi surface in CeRu₂, URu₂Si₂ and UPd₂Al₃ was detected in low fields down to $H/H_{c2} = 0.3-0.5$, for example down to a low field of 15 kOe or $0.3H_{c2}$ in CeRu₂. It is questionable whether the small Fermi surface has a superconducting energy gap in magnetic fields far below H_{c2} . This might indicate the growth of a pair-breaking effect far below H_{c2} for the small Fermi surface. More importantly, there is a possibility that the superconducting state for the small Fermi surface is changed into a normal state far below H_{c2} .

Till now, the dHvA oscillation in the mixed state has been observed for several compounds such as NbSe₂ [198], V₃Si [199], Nb₃Sn [200], YNi₂B₂C [201,202] as well as *f*-electron system of CeRu₂, CeCoIn₅, URu₂Si₂ and UPd₂Al₂.

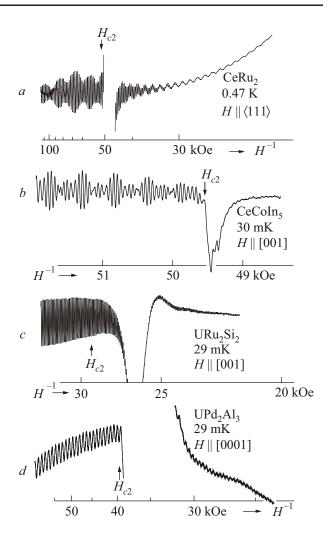


Fig. 138. dHvA oscillations in the superconducting mixed states of CeRu₂ [195], CeCoIn₅ [79], URu₂Si₂ [196] and UPd₂Al₃ [197].

10. Conclusion

We summarize the present Fermi surface studies in the *f*-electron systems of rare earth and actinide compounds.

1. Fermi surface studies are very important to know the ground-state properties of these various *f*-electron compounds. Even in the 4f-electron localized system, the presence of 4f-electron alter the Fermi surface through the 4felectron contribution to the crystal potential and through the introduction of new Brillouin zone boundaries and magnetic energy gaps which occur when 4f-electron moments order. The latter effect may be approximated by a band-folding procedure where the paramagnetic Fermi surface, which is similar to the Fermi surface of the corresponding La compound, is folded into a smaller Brillouin zone based on the magnetic unit cell, which is larger than the chemical unit cell. If the magnetic energy gaps associated with the magnetic structure are small enough, conduction electrons undergoing the cyclotron motion in the presence of a magnetic field can tunnel through these gaps and circulate the orbits on the paramagnetic Fermi surface. If this magnetic breakthrough occurs, the paramagnetic Fermi surface is observed in the dHvA effect even in the presence of magnetic order. The typical example was an antiferromagnet NdIn₃ in RIn₃ (R: rare earth). A nearly spherical Fermi surface in the paramagnetic state, which corresponds to branch a of the band 7-electron Fermi surface of LaIn₃, is changed into a multiply-connected Fermi surface based on the magnetic Brillouin zone in the antiferromagnetic state. Even in the antiferromagnetic state, the dHvA oscillation for branch a was observed, with an extremely small dHvA amplitude based on the breakthrough effect.

2. Mass enhancement due to the electron-magnon interaction in the 4f localized compounds RIn₃ is large compared with the one due to the electron-phonon interaction. The cyclotron mass is enhanced by twice or three times in RIn₃ compared with the cyclotron mass in LaIn₃. An antiferroquadrupolar ordering in PrPb3 is also found to enhance the cyclotron mass. An exceptionally large mass enhancement is observed in a Kondo-lattice compound with magnetic ordering such as CeIn₃ in RIn₃. The Fermi surface of CeIn₃ is similar to a non-4*f* reference compound LuIn₃ or LaIn₃ in topology, especially for branch d, but is altered by the magnetic Brillouin zone boundaries for branch a. Nevertheless, the cyclotron mass is extremely large compared with the corresponding one of LuIn₃. In this system, a small amount of 4f electron most likely contributes to make a sharp density of states at the Fermi energy. Thus the energy band becomes flat around the Fermi energy, which brings about the large effective mass. It is stressed that the heavy electronic state exists locally in the Fermi surface. The Fermi surface named branch d is a nearly spherical Fermi surface with humps. The hump region on the Fermi surface is extremely heavy.

3. The *f*-itinerant band model is well applicable to the topology of the Fermi surface in enhanced Pauli paramagnets such as CeSn₃, YbAl₃, UAl₃, UX₃ (X: Si, Ge), NpGe₃ and PuIn3 in RX3 and AnX3 compounds. These compounds are called a valence fluctuating compound or a spin fluctuating compound. The magnetic susceptibility in these compounds increases with decreasing temperature, roughly following the Curie-Weiss law at high temperatures, with an *f*-localized magnetic moment, has a maximum at $T_{\gamma max}$ and reaches an enhanced Pauli paramagnetic susceptibility $\chi(0)$ for $T \rightarrow 0$ K. A characteristic feature is that $T_{\chi max}$ is in the range from 50 to 200 K. $T_{\chi max}$ roughly corresponds to a Kondo temperature. The f electrons in a Kondo lattice compound with a relatively large value of T_K are itinerant. It is, however, stressed that the cyclotron mass is larger than the corresponding band mass because the many-body Kondo effect is not included in the conventional energy band calculations.

4. It is interesting that the topology of Fermi surface is very similar between two compounds: LaPb₃ vs UAl₃, LaIn₃ vs NpIn₃, and YbIn₃ vs PuIn₃, although the cyclotron mass is extremely different between two compounds. It is also noticed that the topology of a divalent compound YbIn₃ is very similar to a 4*f*-itinerant compound YbAl₃. It is also noted that YbCu₂Ge₂ is similar to YbCu₂Si₂ in topology of the Fermi surface. Furthermore, 4*f*-itinerant Ce compounds are similar to the corresponding non-5*f* Th compounds in the topology of the Fermi surface: CeIn₃ under pressure vs ThIn₃, and CeRhIn₅ under pressure and CeCoIn₅ vs ThRhIn₅.

5. 5*f* electrons in magnetically ordered U and Np compounds reveal dual nature: localized and itinerant. Namely, the 5*f* electrons contribute to the magnetic moment and also to the Fermi surface. The topology of the Fermi surface of antiferromagnets UPtGa₅ and NpRhGa₅ is approximately explained by the spin-and orbital-polarized 5*f*-itinerant band model.

6. RTIn₅ (T: Co, Rh, Ir) and AnTGa₅ (T: transition metal) with the tetragonal structure possess the quasi-two dimensional electronic state. Simply thinking, a conductive RIn₃ (AnGa₃) layer and an insulating TIn₂ (AnGa₂) layer stack along the tetragonal c-axis. The quasi-two dimensional electronic state, together with the heavy fermion state, enhances heavy fermion superconductivity, as in CeRhIn5 under pressure, CeCoIn5, PuRhGa5, PuCoGa5 and also NpPd₅Al₂. Interesting is the relation between the superconducting transition temperature T_{sc} and the γ value: $T_{sc} = 2.3 \text{ K} (\gamma = 1070 \text{ mJ/(K}^2 \cdot \text{mol}))$ in CeCoIn₅, 4.9 K (400 mJ/(K²·mol)) in NpRh5Al₂, 8.6 K (70 mJ/(K²·mol)) in PuRhGa₅ and 18.5 K (77 mJ/(K²·mol)) in PuCoGa₅. It is also stressed that $T_{sc} = 0.2 \text{K} (\gamma = 1000 \text{ mJ/(K}^2 \cdot \text{mol}))$ in a three dimensional electronic state of CeIn3 under pressure is enhanced by one order, $T_{sc} = 2.3$ K in a two dimensional electronic state of CeCoIn5. It is also noted that heavy fermion superconductivity of CeCoIn5 and NpPd5Al2 is realized in the non-Fermi liquid state

7. Heavy fermion compounds with a small $T_{\chi max}$ value, less than 50 K, indicate a metamagnetic behavior or an abrupt nonlinear increase of magnetization at H_m . We obtained a simple relation for CeRu₂Si₂, UPt₃ and YbT₂Zn₂0 (T: Co, Rh, Ir): H_m (kOe) = $15T_{\chi max}$, K or, $k_B T_{\chi max}$ = $= \mu_B H_m$. A superheavy fermion state is realized in YbCo₂Zn₂₀: $\gamma = 8000 \text{ mJ/(K}^2 \cdot \text{mol}))$, $T_{\gamma \text{max}} = 0.32 \text{ K}$ and $H_m = 6$ kOe, and also under pressure for YbIr₂Zn₂₀, exceeding $\gamma = 10 \text{ J/(K}^2 \cdot \text{mol})$ at 5.0 GPa. The present superheavy fermion state is, however, drastically reduced in magnetic fields. It is also noted that the metamagnetic field H_m is a good guiding parameter to reach the quantum critical point in heavy fermion Yb compounds without magnetic ordering: $P \rightarrow P_c$ for $H_m \rightarrow 0$. The topology of the Fermi surface is changed at H_m in CeRu₂Si₂, but not in YbIr₂Si₂₀, although the cyclotron mass in both compounds possesses a maximum at H_m and reduces extremely in magnetic fields larger than H_m . The metamagnetic transition based on the field-induced ferroquadrupolar ordering was also studied in PrCu₂.

8. From the dHvA experiments under pressure for antiferromagnets CeRh₂Si₂, CeIn₃ and CeRhIn₅, it was clarified that a drastic change in the 4*f* electronic state from a 4*f*-localized Fermi surface to a 4*f*-itinerant Fermi surface occurs when pressure *P* crosses a critical pressure P_c or P_c^* . The Fermi surface instability occurs at $P_c(P_c^*)$, indicating a first-order phase transition. The cyclotron mass is enhanced around $P_c(P_c^*)$, especially indicating a divergent tendency at P_c^* in CeRhIn₅. Superconductivity in these compounds is observed in the heavy fermion state around $P_c(P_c^*)$.

9. The split Fermi surface properties based on the noncentrosymmetric tetragonal crystal structure in LaTX₃ (T: Co, Rh, Ir; X: Si, Ge) were studied by the dHvA experiments, together with the energy band calculations. The magnitude of the antisymmetric spin-orbit interaction $2|\alpha p_{\perp}|$ is found to vary when LaTGe₃ is changed from T = Co, Rh, to Ir, but remains unchanged in LaIrX₃ from X = Si to Ge: $2|\alpha p_{\perp}|$ = 460 K in LaCoGe₃, 510 K in LaRhGe₃, 1090 K in LaIrGe₃, and 1100 K in LaIrSi₃ for the main orbit named α of bands 69 and 70 electron-Fermi surfaces, for example. The corresponding superconducting properties were also studied in CeTX₃ compounds under pressure. One of the characteristic superconducting properties in CeIrSi₃ is the upper critical field H_{c2} at pressure of about 2.6 GPa. A huge value of $H_{c2}(0) \simeq 450$ kOe was found for the magnetic field along the non-centrosymmetric tetragonal [001] direction, with a very small T_{sc} = = 1.6 K, while $H_{c2}(0) = 95$ kOe for $H \parallel [110]$. The present superconductivity is realized in the electronic instability at $P_c^* \simeq 2.6$ GPa, strong-coupling nature and non-centrosymmetric electronic state.

10. The dHvA oscillation was observed clearly in both the normal and superconducting mixed states in CeRu₂, CeCoIn₅, URu₂Si₂ and UPd₂Al₃.

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- Y. Ōnuki, T. Goto, and T. Kasuya, *Materials Science and Technology*, K.H.J. Buschow (ed.), VCH, Weinheim (1991), Vol. 3A, Part I, Ch. 7, p. 545.
- Y. Ōnuki and A. Hasegawa, *Handbook on the Physics and Chemistry of Rare Earths*, K.A. Gschneidner, Jr., and L. Eyring (eds.), Elsevier Science, Amsterdam (1995), Vol. 20, p. 1.
- Y. Ōnuki, R. Settai, K. Sugiyama, T. Takeuchi, T.C. Kobayashi, Y. Haga, and E. Yamamoto, *J. Phys. Soc. Jpn.* 73, 769 (2004).
- S. Doniach, Valence Instabilities and Related Narrow Band Phenomena, R.D. Parks (ed.), Plenum, New York (1977), p. 169.
- Low Temperature Physics/Fizika Nizkikh Temperatur, 2012, v. 38, No. 2

- Y. Ōnuki, Y. Inada, H. Ohkuni, R. Settai, N. Kimura, H. Aoki, Y. Haga, and E. Yamamoto, *Physica* B280, 276 (2000).
- 6. M. Sigrist and K. Ueda, Rev. Mod. Phys. 63, 239 (1991).
- N. Metoki, Y. Haga, Y. Koike, and Y. Ōnuki, *Phys. Rev. Lett.* **80**, 5417 (1998).
- N. Bernhoeft, N. Sato, B. Roessli, N. Aso, A. Heiss, G.H. Lander, Y. Endoh, and T. Komatsubara, *Phys. Rev. Lett.* 81, 4244 (1998).
- N.K. Sato, N. Aso, K. Miyake, R. Siina, P. Thalmeier, G. Varelogiannis, C. Geibel, F. Steglich, P. Fulde, and T. Komatsubara, *Nature* 410, 340 (2001).
- M. Kyogaku, Y. Kitaoka, K. Asayama, C. Geibel, C. Schank, and F. Steglich, *J. Phys. Soc. Jpn.* 62, 4016 (1993).
- H. Tou, Y. Kitaoka, K. Ishida, K. Asayama, N. Kimura, Y. Önuki, E. Yamamoto, Y. Haga, and K. Maezawa, *Phys. Rev. Lett.* 80, 3129 (1998).
- K. Tenya, M. Ikeda, T. Sakakibara, E. Yamamoto, K. Maezawa, N. Kimura, R. Settai, and Y. Ōnuki, *Phys. Rev. Lett.* 77, 3193 (1996).
- D. Jaccard, H. Wilhelm, K. Alami-Yadri, and E. Vargoz, *Physica* B259–261, 1 (1999).
- N.D. Mathur, F.M. Grosche, S.R. Julian, I.R. Walker, D.M. Freye, R.K.W. Haselwimmer, and G.G. Lonzarich, *Nature* 394, 39 (1998).
- H. Hegger, C. Petrovic, E.G. Moshopoulou, M.F. Hundley, J.L. Sarrao, Z. Fisk, and J.D. Thompson, *Phys. Rev. Lett.* 84, 4986 (2000).
- S.S. Saxena, P. Agarwal, K. Ahilan, F.M. Grosche, R.K.W. Haselwimmer, M.J. Steiner, E. Pugh, I.R. Walker, S.R. Julian, P. Monthoux, G.G. Lonzarich, A. Huxley, I. Sheikin, D. Braithwaite, and J. Flouquet, *Nature* 406, 587 (2000).
- D. Aoki, A. Huxley, E. Ressouche, D. Braithwaite, J. Flouquet, J.P. Brison, E. Lhotel, and C. Paulsen, *Nature* 413, 613 (2001).
- T. Akazawa, H. Hidaka, T. Fujiwara, T.C. Kobayashi, E. Yamamoto, Y. Haga, R. Settai, and Y. Ōnuki, *J. Phys.: Condens. Matter* 16, L29 (2004).
- N.T. Huy, A. Gasparini, D.E. de Nijs, Y. Huang, J.C.P. Klaasse, T. Gortenmulder, A. de Visser, A. Hamann, T. Görlach, and H. v. Lühneysen, *Phys. Rev. Lett.* **99**, 067006 (2007).
- H.R. Ott and Z. Fisk, in: *Handbook on the Physics and Chemistry of the Actinides*, A.J. Freeman and G.H. Lander (eds.), Elsevier Science, Amsterdam (1987), Vol. 5, Ch. 2, p. 85.
- Y. Haga, H. Sakai, and S. Kambe, J. Phys. Soc. Jpn. 76, 051012 (2007).
- Y. Ōnuki, R. Settai, K. Sugiyama, Y. Inada, T. Takeuchi, Y. Haga, E. Yamamoto, H. Harima, and H. Yamagami, J. *Phys.: Condens. Matter* 19, 125203 (2007).
- Y. Okuda, Y. Miyauchi, Y. Ida, T. Yamada, Y. Ooduchi, T.D. Matsuda, Y. Haga, T. Takeuchi, K. Kindo, M. Hagiwara, H. Harima, K. Sugiyama, R. Settai, and Y. Ōnuki, J. *Phys. Soc. Jpn.* **76**, 044708 (2007).
- Y. Haga, T. Honma, E. Yamamoto, H. Ohkuni, Y. Ōnuki, M. Ito, and N. Kimura, *Jpn. J. Appl. Phys.* 37, 3604 (1998).
- R. Settai, T. Kawai, T. Endo, H. Muranaka, Y. Doi, Y. Onuki, and H. Harima, *J. Phys. Soc. Jpn.* A77, 339 (2008).

- T. Kawai, H. Muranaka, T. Endo, N.D. Dung, Y. Doi, S. Ikeda, T.D. Matsuda, Y. Haga, H. Harima, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 77, 064717 (2008).
- H. Sugawara, R. Settai, Y. Doi, H. Muranaka, K. Katayama, H. Yamagami, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 77, 113711 (2008).
- D. Shoenberg, *Magnetic Oscillations in Metals*, Cambridge University Press, Cambridge (1984).
- R. Settai, T. Takeuchi, and Y. Ōnuki, J. Phys. Soc. Jpn. 76, 051003 (2007).
- Y. Ōnuki, R. Settai, K. Sugiyama, T. Takeuchi, T.C. Kobayashi, Y. Haga, and E. Yamamoto, *Physica* B300, 61 (2001).
- Y. Haga, E. Yamamoto, Y. Tokiwa, D. Aoki, Y. Inada, R. Settai, T. Maehira, H. Yamagami, H. Harima, and Y. Ōnuki, *J. Nucl. Sci. Technol. Suppl.* 3, 56 (2002).
- 32. I. Harris and G. Raynor, J. Less-Common Met. 9, 7 (1965).
- R.M. Galera and P. Morin, J. Magn. Magn. Mater. 116, 159 (1992).
- K.H.J. Buschow, H.W. de Wijn, and A.M. van Diepen, J. Chem. Phys. 50, 137 (1969).
- J.M. Lawrence and S.M. Shapiro, *Phys. Rev.* B22, 4379 (1980).
- A. Benoit, J.X. Boucherle, P. Convert, J. Flouquet, J. Pellau, and J. Schweizer, *Solid State Commun.* 34, 293 (1980).
- Y. Kohori, T. Kohara, Y. Yamato, G. Tomka, and P.C. Riedi, *Physica* B281–282, 12 (2000).
- R. Settai, T. Kubo, T. Shiromoto, D. Honda, H. Shishido, K. Sugiyama, Y. Haga, T.D. Matsuda, K. Betsuyaku, H. Harima, T.C. Kobayashi, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 74, 3016 (2005).
- I. Umehara, N. Nagai, and Y. Ōnuki, J. Phys. Soc. Jpn. 60, 591 (1991).
- A. Hasegawa, in: Crystalline Electric Field Effects in f-Electron Magnetism, R.P. Guetin, W. Suski, and Z. Zolnierek (eds.), Plenum, New York (1982), p. 201.
- 41. I. Umehara, T. Ebihara, N. Nagai, K. Satoh, Y. Fujimaki, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **61**, 1633 (1992).
- R. Settai, T. Ebihara, H. Sugawara, N. Kimura, M. Takashita, H. Ikezawa, K. Ichihashi, and Y. Ōnuki, *Physica* B201, 102 (1994).
- P. Lethuillier, J. Pierre, G. Fillion, and B. Barbara, *Phys. Status Solidi* A15, 613 (1973).
- A. Czopnik, N. Iliev, B. Stalihski, C. Bazan, H. Madge, and R. Pott, *Physica* B130, 259 (1985).
- T. Ebihara, I. Umehara, A.K. Albessard, K. Satoh, and Y. Onuki, *Physica* B186–188, 123 (1993).
- I. Umehara, N. Nagai, and Y. Ōnuki, J. Phys. Soc. Jpn. 60, 3150 (1991).
- T. Ebihara, I. Umehara, A.K. Albessard, Y. Fujimaki, K. Satoh, Y. Ōnuki, B. Liu, and M. Kasaya, *J. Phys. Soc. Jpn.* 61, 2104 (1992).
- I. Umehara, T. Ebihara, N. Nagai, Y. Fujimaki, K. Satoh, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 61, 19 (1992).
- S. Nojiri, Y. Katayama, D. Aoki, N. Suzuki, K. Sugiyama, R. Settai, Y. Inada, Y. Ōnuki, and H. Harima, *Physica* B28– 282, 747 (2000).

- N. Nagai, I. Umehara, T. Ebihara, A.K. Albessard, H. Sugawara, T. Yamazaki, K. Satoh, and Y. Ōnuki, *Physica* B186–188, 139 (1993).
- R. Settai, T. Ebihara, M. Takashita, H. Sugawara, N. Kimura, K. Metoki, Y. Ōnuki, S. Uji, and H. Aoki, *J. Magn. Magn. Mater.* 140–144, 1153 (1995).
- T. Ebihara, N. Harrison, M. Jaime, S. Uji, and J.C. Lashley, *Phys. Rev. Lett.* 93, 246401 (2004).
- T. Ebihara, I. Umehara, A.K. Albessard, K. Satoh, and Y. Onuki, J. Phys. Soc. Jpn. 61, 1472 (1992).
- N. Harrison, S.E. Sebastian, C.H. Mielke, A. Paris, M.J. Gordon, C.A. Swenson, D.G. Rickel, M.D. Pacheco, P.F. Ruminer. J.B. Schillig, J.R. Sims, A.H. Lacerda, M.-T. Suzuki, H. Harima, and T. Ebihara, *Phys. Rev. Lett.* **99**, 056401 (2007).
- V.B. Pluzhnikov, A. Czopnik, and I.V. Svechkarev, *Physica* B212, 375 (1995).
- T. Ebihara, Y. Inada, M. Murakawa, S. Uji, C. Terakura, T. Terashima, E. Yamamoto, Y. Haga, Y. Ōnuki, and H. Harima, *J. Phys. Soc. Jpn.* 69, 895 (2000).
- N.D. Dung, T.D. Matsuda, Y. Haga, S. Ikeda, E. Yamamoto, T. Ishikura, T. Endo, S. Tatsuoka, Y. Aoki, H. Sato, T. Takeuchi, R. Settai, H. Harima, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 78, 084711 (2009).
- D. Aoki, Y. Homma, H. Sakai, S. Ikeda, Y. Shiokawa, E. Yamamoto, A. Nakamura, Y. Haga, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 75, 084710 (2006).
- T.D. Matsuda, Y. Haga, E. Yamamoto, S. Ikeda, H. Shishido, R. Settai, H. Harima, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 74, 3276 (2005).
- I. Sakamoto, S. Ohara, I. Oguro, E. Yamamoto, Y. Haga, Y. Ōnuki, and S. Maruno, J. Alloys Comp. 275–277, 505 (1998).
- D. Aoki, Y. Katayama, R. Settai, N. Suzuki, K. Sugiyama, K. Kindo, H. Harima, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 67, 4251 (1998).
- I. Umehara, N. Nagai, and Y. Ōnuki, J. Phys. Soc. Jpn. 60, 1294 (1991).
- D. Aoki, Y. Katayama, R. Settai, Y. Inada, Y. Ōnuki, H. Harima, and Z. Kletowski, *J. Phys. Soc. Jpn.* 66, 3988 (1997).
- D. Aoki, N. Watanabe, Y. Inada, R. Settai, K. Sugiyama, H. Harima, T. Inoue, K. Kindo, E. Yamamoto, Y. Haga, and Y. Önuki, *J. Phys. Soc. Jpn.* 69, 2609 (2000).
- D. Aoki, N. Suzuki, K. Miyake, Y. Inada, R. Settai, K. Sugiyama, E. Yamamoto, Y. Haga, Y. Ōnuki, T. Inoue, K. Kindo, H. Sugawara, H. Sato, and H. Yamagami, *J. Phys. Soc. Jpn.* **70**, 538 (2001).
- Y. Tokiwa, D. Aoki, Y. Haga, E. Yamamoto, S. Ikeda, R. Settai, A. Nakamura, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 70, 3326 (2001).
- I. Umehara, Y. Kurosawa, N. Nagai, M. Kikuchi, K. Satoh, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **59**, 2848 (1990).
- Y. Haga, D. Aoki, H. Yamagami, T.D. Matsuda, K. Nakajima, Y. Arai, E. Yamamoto, A. Nakamura, Y. Homma, Y. Shiokawa, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 74, 2889 (2005).

- Y. Tokiwa, H. Harima, D. Aoki, S. Nojiri, M. Murakawa, K. Miyake, N. Watanabe, R. Settai, Y. Inada, H. Sugawara, H. Sato, Y. Haga, E. Yamamoto, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 69, 1105 (2000).
- 70. J. Arko and D.D. Koelling, Phys. Rev. B17, 3104 (1978).
- D. Aoki, H. Yamagami, Y. Homma, Y. Shiokawa, E. Yamamoto, A. Nakamura, Y. Haga, R. Settai, and Y. Ōnuki, J. *Phys. Soc. Jpn.* 74, 2149 (2005).
- A. Hasegawa and H. Yamagami, J. Phys. Soc. Jpn. 60, 1654 (1991).
- A. Hasegawa, H. Yamagami, and H. Johbettoh, J. Phys. Soc. Jpn. 59, 2457 (1990).
- A. Galatanu, Y. Haga, T.D. Matsuda, S. Ikeda, E. Yamamoto, D. Aoki, T. Takeuchi, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 74, 1582 (2005).
- P. Dervenagas, D. Kaczorowski, F. Bourdarot, P. Burlet, A. Czopnik, and G.H. Lander, *Physica* B269, 368 (1999).
- J.P. Sanchez, E. Colineau, P. Vulliet, and K. Tomala, J. Alloys Comp. 275–277, 195 (1998).
- H. Shishido, R. Settai, D. Aoki, S. Ikeda, H. Nakawaki, T. Iizuka, Y. Inada, K. Sugiyama, T. Takeuchi, K. Kindo, T.C. Kobayashi, Y. Haga, H. Harima, Y. Aoki, T. Namiki, H. Sato, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **71**, 162 (2002).
- H. Shishido, R. Settai, H. Harima, and Y. Ōnuki, J. Phys. Soc. Jpn. 74, 1103 (2005).
- R. Settai, H. Shishido, S. Ikeda, Y. Murakawa, M. Nakashima, D. Aoki, Y. Haga, H. Harima, and Y. Ōnuki, *J. Phys.*: *Condens. Matter* 13, L627 (2001).
- T.D. Matsuda, Y. Haga, E. Yamamoto, S. Ikeda, H. Shishido, R. Settai, H. Harima, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **76**, 064712 (2007).
- Y. Tokiwa, T. Maehira, S. Ikeda, Y. Haga, E. Yamamoto, A. Nakamura, Y. Ōnuki, M. Higuchi, and A. Hasegawa, J. *Phys. Soc. Jpn.* 70, 2982 (2001).
- S. Ikeda, Y. Tokiwa, T. Okubo, Y. Haga, E. Yamamoto, Y. Inada, R. Settai, and Y. Ōnuki, *J. Nucl. Sci. Technol. Suppl.* 3, 206 (2002).
- S. Ikeda, Y. Tokiwa, Y. Haga, E. Yamamoto, T. Okubo, M. Yamada, N. Nakamura, K. Sugiyama, K. Kindo, Y. Inada, H. Yamagami, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 72, 576 (2003).
- D. Aoki, H. Yamagami, Y. Homma, Y. Shiokawa, E. Yamamoto, A. Nakamura, Y. Haga, R. Settai, and Y. Ōnuki, J. *Phys.: Condens. Matter* 17, L169 (2005).
- T. Maehira, T. Hotta, K. Ueda, and A. Hasegawa, *Phys. Rev. Lett.* **90**, 207007 (2003).
- A. Llobet, J.S. Gardner, E.G. Moshopoulou, J.-M. Mignot, M. Nicklas, W. Bao, N.O. Moreno, P.G. Pagliuso, I.N. Goncharenko, J.L. Sarrao, and J.D. Thompson, *Phys. Rev.* B69, 024403 (2004).
- T. Muramatsu, N. Tateiwa, T.C. Kobayashi, K. Shimizu, K. Amaya, D. Aoki, H. Shishido, Y. Haga, and Y. Ōnuki, J. Phys. Soc. Jpn. 70, 3362 (2001).
- S. Kawasaki, T. Mito, G.-Q. Zheng, C. Thessiu, Y. Kawasaki, K. Ishida, Y. Kitaoka, T. Muramatsu, T.C. Kobayashi, D.

Aoki, S. Araki, Y. Haga, R. Settai, and Y. Ōnuki, *Phys. Rev.* **B65**, 020504 (2002).

- H. Shishido, T. Ueda, S. Hashimoto, T. Kubo, R. Settai, H. Harima, and Y. Ōnuki, *J. Phys.: Condens. Matter* 15, L499 (2003).
- J.L. Sarrao, L.A. Morales, J.D. Thompson, B.L. Scott, G.R. Stewart, F. Wastin, J. Rebizant, P. Boulet, E. Colineau, and G.H. Lander, *Nature (London)* 420, 297 (2002).
- Y. Kitaoka, H. Mukuda, M. Yashima, and A. Harada, J. Phys. Soc. Jpn. 76, 051001 (2007).
- T. Park, F. Ronning, H.Q. Yuan, M.B. Salamon, R. Movshovich, J.L. Sarrao, and J.D. Thompson, *Nature* 440, 65 (2006).
- G. Knebel, D. Aoki, D. Braithwaite, B. Salce, and J. Flouquet, *Phys. Rev.* B74, 020501 (2006).
- Y. Ida, R. Settai, Y. Ota, F. Honda, and Y. Ōnuki, J. Phys. Soc. Jpn. 77, 084708 (2008).
- Y. Haga, D. Aoki, T.D. Matsuda, K. Nakajima, Y. Arai, E. Yamamoto, A. Nakamura, Y. Homma, Y. Shiokawa, and Y. Önuki, *J. Phys. Soc. Jpn.* 74, 1698 (2005).
- D. Aoki, Y. Haga, T.D. Matsuda, N. Tateiwa, S. Ikeda, Y. Homma, H. Sakai, Y. Shiokawa, E. Yamamoto, A. Nakamura, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 76, 063701 (2007).
- A. Bianchi, R. Movshovich, C. Capan, P.G. Pagliuso, and J.L. Sarrao, *Phys. Rev. Lett.* **91**, 187004 (2003).
- K. Kakuyanagi, M. Saitoh, K. Kumagai, S. Takashima, M. Nohara, H. Takagi, and Y. Matsuda, *Phys. Rev. Lett.* 94, 0476202 (2005).
- K. Izawa, H. Yamaguchi, Y. Matsuda, H. Shishido, R. Settai, and Y. Ōnuki, *Phys. Rev. Lett.* 87, 057002 (2001).
- T. Tayama, A. Harita, T. Sakakibara, Y. Haga, H. Shishido, R. Settai, and Y. Ōnuki, *Phys. Rev.* B65, 180504(R) (2002).
- 101. C. Petrovic, P.G. Pagliuso, M.F. Hundley, R. Movshovich, J.L. Sarrao, J.D. Thompson, Z. Fisk, and P. Monthoux, J. *Phys.: Condens. Matter* **13**, L337 (2001).
- 102. S. Ikeda, H. Shishido, M. Nakashima, R. Settai, D. Aoki, Y. Haga, H. Harima, Y. Aoki, T. Namiki, H. Sato, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **70**, 2248 (2001) [*Errata*; **70**, 3187 (2001)].
- 103. K. Kaneko, N. Metoki, N. Bernhoeft, G.H. Lander, Y. Ishii, S. Ikeda, Y. Tokiwa, Y. Haga, and Y. Ōnuki, *Phys. Rev.* B68, 214419 (2003).
- 104. S. Jonen, N. Metoki, F. Honda, K. Kaneko, E. Yamamoto, Y. Haga, D. Aoki, Y. Homma, Y. Shiokawa, and Y. Ōnuki, *Phys. Rev.* B74, 144412 (2006).
- 105. K. Sugiyama, H. Nakashima, D. Aoki, Y. Haga, E. Yamamoto, A. Nakamura, Y. Homma, Y. Shiokawa, K. Kindo, M. Hagiwara, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **75**, 094707 (2006).
- 106. A. Kiss and Y. Kuramoto, J. Phys. Soc. Jpn. 75, 034709 (2006).
- 107. F. Wastin, P. Boulet, J. Rebizant, E. Colineau, and G.H. Lander, J. Phys.: Condens. Matter 15, S2279 (2003).
- 108. H. Yamagami, D. Aoki, Y. Haga, and Y. Onuki, J. Phys. Soc. Jpn. 76, 083708 (2007).

- 109. T. Sakakibara, T. Tayama, K. Matsuhira, H. Mitamura, H. Amitsuka, K. Maezawa, and Y. Ōnuki, *Phys. Rev.* B51, 12030 (1995).
- 110. T. Sakakibara, T. Tayama, K. matsuhira, A. Nomachi, S. Honma, T. Tayama, H. Amitsuka, K. Maezawa, and Y. Ōnuki, *Jpn. J. Appl. Phys.*, Ser. **11**, 6 (1999).
- 111. H. Aoki, S. Uji, A.K. Albessard, and Y. Ōnuki, *Phys. Rev. Lett.* **71**, 2110 (1993).
- 112. H. Aoki, S. Uji, A.K. Albessard, and Y. Ōnuki, J. Phys. Soc. Jpn. 62, 3157 (1993).
- 113. M. Takashita, H. Aoki, T. Terashima, S. Uji, K. Maezawa, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **65**, 515 (1996).
- 114. H. Yamagami and A. Hasegawa, J. Phys. Soc. Jpn. 65, 592 (1993).
- 115. H. Yamagami and A. Hasegawa, J. Phys. Soc. Jpn. 61, 2388 (1992).
- 116. Y. Aoki, T.D. Matsuda, H. Sugawara, H. Sato, H. Ohkuni, R. Settai, Y. Ōnuki, E. Yamamoto, Y. Haga, A.V. Andreev, V. Sechovsky, L. Havela, H. Ikeda, and K. Miyake, *J. Magn. Magn. Mater.* **177–181**, 271 (1998).
- S. Holtmeier, P. Haen, A. Lacerda, P. Lejay, J.L. Tholence, J. Voiron, and J. Flouquet, *Physica* B204, 250 (1995).
- 118. T. Kasuya, J. Phys. Soc. Jpn. 67, 2372 (1998).
- 119. K. Hanzawa, K. Ohara, and K. Yosida, J. Phys. Soc. Jpn. 66, 3001 (1997).
- 120. Y. Ono, J. Phys. Soc. Jpn. 65, 19 (1996).
- 121. K. Sugawara, Y. Aoki, H. Sato, N. Mushnikov, and T. Goto, J. Phys. Soc. Jpn. 68, 1094 (1999).
- 122. H. von Löhneysen, H.G. Schlager, and A. Schröder, *Physica* B186–188, 590 (1993).
- 123. Y. Ōnuki, S. Yasui, M. Matsushita, S. Yoshiuchi, M. Ohya, Y. Hirose, N.D. Dung, F. Honda, T. Takeuchi, R. Settai, K. Sugiyama, E. Yamamoto, T.D. Matsuda, Y. Haga, T. Tanaka, Y. Kubo, and H. Harima, *J. Phys. Soc. Jpn.* **80**, SA003 (2011).
- 124. N. Kimura, T. Komatsubara, D. Aoki, Y. Ōnuki, Y. Haga, E. Yamamoto, H. Aoki, and H. Harima, *J. Phys. Soc. Jpn.* 67, 2185 (1998).
- 125. N. Kimura, T. Tani, H. Aoki, T. Komatsubara, S. Uji, D. Aoki, Y. Inada, Y. Ōnuki, Y. Haga, E. Yamamoto, and H. Harima, *Physica* B281–282, 710 (2000).
- 126. K. Sugiyama, M. Nakashima, D. Aoki, K. Kindo, N. Kimura, H. Aoki, T. Komatsubara, S. Uji, Y. Haga, E. Yamamoto, H. Harima, and Y. Ōnuki, *Phys. Rev.* B60, 9248 (1999).
- 127. H.P. van der Meulen, Z. Tarnawski, A. de Visser, J.J.M. Franse J., A.A.J. Perenboom, D. Althof, and H. van Kempen, *Phys. Rev.* B41, 9352 (1990).
- 128. G. Knopp, A. Loidl, K. Knorr, L. Pawlak, M. Duczmal, R. Caspary, U. Gottwick, H. Spille, F. Steglich, and A.P. Murani, Z. Phys. B77, 95 (1989).
- 129. F. Steglich, J. Aarts, C.D. Bredl, W. Lieke, D. Meschede, W. Franz, and J. Schäfer, *Phys. Rev. Lett.* **43**, 1892 (1979).
- 130. D. Jaccard, K. Behnia, and J. Sierro, *Phys. Lett.* A163, 475 (1992).
- 131. T. Takeuchi, S. Yasui, M. Toda, M. Matsushita, S. Yoshiuchi, M. Ohya, K. Katayama, Y. Hirose, N. Yoshitani, F.

Honda, K. Sugiyama, M. Hagiwara, K. Kindo, E. Yamamoto, Y. Haga, T. Tanaka, Y. Kubo, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **79**, 064609 (2010).

- 132. M.S. Torikachvili, S. Jia, E.D. Mun, S.T. Hannahs, R.C. Black, W.K. Neils, Dinesh Martien, S.L. Bud'ko, and P.C. Canfield, *Proc. Natl. Acad. Sci. U.S.A.* 104, 9960 (2007).
- 133. S. Yoshiuchi, M. Toda, M. Matsushita, S. Yasui, Y. Hirose, M. Ohya, K. Katayama, F. Honda, K. Sugiyama, M. Hagiwara, K. Kindo, T. Takeuchi, E. Yamamoto, Y. Haga, R. Settai, T. Tanaka, Y. Kubo, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 78, 123711 (2009).
- 134. M. Ohya, M. Matsushita, S. Yoshiuchi, T. Takeuchi, F. Honda, R. Settai, T. Tanaka, Y. Kubo, and Y. Ōnuki, J. Phys. Soc. Jpn. 79, 083601 (2010).
- 135. F. Honda, S. Yasui, S. Yoshiuchi, T. Takeuchi, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **79**, 083709 (2010).
- 136. K. Sugimaya and Y. Ōnuki, *High Magnetic Fields*, F. Herlach and N. Miura (eds.), World Scientific, Singapore (2003), p. 139.
- 137. K. Kadowaki and S.B. Woods, *Solid State Commun.* 58, 507 (1986).
- 138. K. Miyake, T. Maatsuura, and C.M. Varma, *Solid State Commun.* **71**, 1149 (1989).
- N. Tsujii, H. Kontani, and K. Yoshimura, *Phys. Rev. Lett.* 94, 057201 (2005).
- 140. P. Morin, J. Magn. Magn. Mater. 71, 151 (1988).
- 141. R. Settai, S. Araki, P. Ahmet, M. Abliz, K. Sugiyama, Y. Ōnuki, T. Goto, H. Mitamura, T. Goto, and S. Takayanagi, J. Phys. Soc. Jpn. 67, 636 (1998).
- 142. M. Abliz, R. Settai, P. Ahmet, D. Aoki, K. Sugiyama, and Y. Ōnuki, *Philos. Mag.* B75, 443 (1997).
- 143. P. Ahmet, M. Abliz, R. Settai, K. Sugiyama, Y. Ōnuki, T. Takeuchi, K. Kindo, and S. Takayanagi, J. Phys. Soc. Jpn. 65, 1077 (1996).
- 144. K. Sugiyama, M. Nakashima, Y. Yoshida, R. Settai, T. Takeuchi, K. Kindo, and Y. Ōnuki, *Physica* B256–261, 896 (1999).
- 145. K. Sugiyama, M. Nakashima, Y. Yoshida, Y. Kimura, K. Kindo, T. Takeuchi, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 67, 3244 (1998).
- 146. Y. Yoshida, K. Sugiyama, T. Takeuchi, Y. Kimura, D. Aoki, M. Kozaki, R. Settai, K. Kindo, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 67, 1421 (1998).
- 147. S. Kawarazaki, M. Sato, Y. Miyako, N. Chigusa, K. Watanabe, N. Metoki, Y. Koike, and M. Nishi, *Phys. Rev.* B61, 4167 (2000).
- 148. R. Settai, A. Misawa, S. Araki, M. Kosaki, K. Sugiyama, T. Takeuchi, K. Kindo, Y. Haga, E. Yamamoto, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 66, 2260 (1997).
- 149. S. Araki, M. Nakashima, R. Settai, T.C. Kobayashi, and Y. Ōnuki, J. Phys.: Condens. Matter 14, L377 (2002).
- 150. F.M. Grosche, S.R. Julian, N.D. Mathur, F.V. Carter, and G.G. Lonzarich, *Physica* B237–238, 197 (1997).
- 151. M. Ohashi, F. Honda, T. Eto, S. Kaji, I. Minamidake, G. Oomi, S. Koiwai, and Y. Uwatoko, *Physica* B312–313, 443 (2002).

- 152. T. Graf, J.D. Thompson, M.F. Hundley, R. Movshovich, Z. Fisk, D. Mandrus, R.A. Fisher, and N.E. Phillips, *Phys. Rev. Lett.* 78, 3769 (1997).
- 153. R. Movshovich, T. Graf, D. Mandrus, J.D. Thompson, J.L. Smith, and Z. Fisk, *Phys. Rev.* B53, 8241 (1996).
- 154. S. Araki, R. Settai, T.C. Kobayashi, H. Harima, and Y. Ōnuki, *Phys. Rev.* **B64**, 224417 (2001).
- 156. M. Biasini, G. Ferro, and A. Czopnik, *Phys. Rev.* B68, 094513 (2003).
- 157. M. Endo, N. Kimura, H. Aoki, T. Terashima, S. Uji, T. Matsumoto, and T. Ebihara, *Phys. Rev. Lett.* **93**, 247003 (2004).
- 158. K. Betsuyaku and H. Harima, J. Magn. Magn. Mater. 272– 276, 187 (2004).
- 159. N.R. Werthamer, E. Helfand, and P.C. Hohenberg, *Phys. Rev.* 147, 295 (1966).
- 160. S. Kawasaki, T. Mito, Y. Kawasaki, H. Kotegawa, G.-Q. Zheng, Y. Kitaoka, H. Shishido, S. Araki, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **73**, 1647 (2004).
- 161. G. Knebel , D. Braithwaite, P.C. Canfield, G. Lapertot, and J. Flouquet, *Phys. Rev.* B65, 024425 (2001).
- 162. H. Fukazawa and K. Yamada, *J. Phys.: Condens. Matter* **15**, S2259 (2003).
- 163. D. Hall, E.C. Palm, T.P. Murphy, S.W. Tozer, C. Petrovic, E. Miller-Ricci, L. Peabody, C.Q. H. Li, U. Alver, R.G. Goodrich, J.L. Sarrao, P.G. Pagliuso, J.M. Wills, and Z. Fisk, *Phys. Rev.* B64, 064506 (2001).
- 164. S. Elgazzar, I. Opahle, R. Hayn, and P.M. Oppeneer, *Phys. Rev.* B69, 214510 (2004).
- 165. D. Hall, E.C. Palm, T.P. Murphys, S.W. Tozer, Z. Fisk, U. Alver, R.G. Goodrich, J.L. Sarrao, P.G. Pagliuso, and T. Ebihara, *Phys. Rev.* B64, 212508 (2001).
- 166. A. McCollam, S.R. Julian, P.M. C. Rourke, D. Aoki, and J. Flouquet, *Phys. Rev. Lett.* 94, 186401 (2005).
- 167. I. Sheikin, H. Jin, R. Bel, K. Behnia, C. Proust, J. Flouquet, Y. Matsuda, D. Aoki, and Y. Ōnuki, *Phys. Rev. Lett.* **96**, 077207 (2006).
- 168. N.F. Phillips, R.A. Fisher, F. Bouquet, M.F. Hundley, P.G. Pagliuso, J.L. Sarrao, Z. Fisk, and J.D. Thompson, *J. Phys.: Condens. Matter* 15, S2095 (2003).
- 169. T. Takeuchi, T. Inoue, K. Sugiyama, D. Aoki, Y. Tokiwa, Y. Haga, K. Kindo, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **70**, 877 (2001).
- 170. G. Knebel, D. Aoki, J.-P. Brison, and J. Flouquet, J. Phys. Soc. Jpn. 77, 114704 (2008).
- 171. E. Bauer, G. Hilscher, H. Michor, C. Paul, E.W. Scheidt, A. Gribanov, Y. Seropegin, H. Noel, M. Sigrist, and P. Rogl, *Phys. Rev. Lett.* **92**, 027003 (2004).
- 172. E. Bauer, H. Kaldarar, A. Prokofiev, E. Royanian, A. Amato, J. Sereni, W. Brämer-Escamilla, and I. Bonalde, *J. Phys. Soc. Jpn.* **76**, 051009 (2007).

- 173. T.C. Kobayashi, A. Hori, S. Fukushima, H. Hidaka, H. Kotegawa, T. Akazawa, K. Takeda, Y. Ohishi, and E. Yamamoto, *J. Phys. Soc. Jpn.* **76**, 051007 (2007).
- 174. N. Kimura, K. Ito, K. Saitoh, Y. Umeda, H. Aoki, and T. Terashima, *Phys. Rev. Lett.* **95**, 247004 (2005).
- 175. N. Kimura, K. Ito, H. Aoki, S. Uji, and T. Terashima, *Phys. Rev. Lett.* **98**, 197001 (2007).
- 176. N. Kimura, Y. Muro, and H. Aoki, J. Phys. Soc. Jpn. 76, 051010 (2007).
- 177. I. Sugitani, T.D. Matsuda, Y. Haga, T. Takeuchi, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* **76**, 043703 (2006).
- 178. R. Settai, Y. Okuda, I. Sugitani, Y. Ōnuki, T.D. Matsuda, Y. Haga, and H. Harima, *Int. J. Mod. Phys.* B21, 3238 (2007).
- 179. T. Kawai, H. Muranaka, M.-A. Measson, T. Shimoda, Y. Doi, T.D. Matsuda, Y. Haga, G. Knebel, G. Lapertot, D. Aoki, J. Flouquet, T. Takeuchi, R. Settai, and Y. Ōnuki, J. Phys. Soc. Jpn. 77, 064716 (2008).
- 180. F. Honda, I. Bonalde, K. Shimizu, S. Yoshiuchi, Y. Hirose, T. Nakamura, R. Settai, and Y. Ōnuki, *Phys. Rev.* B81, 140507(R) (2010).
- 181. E.I. Rashba, Sov. Phys. Solid State 2, 1109 (1960).
- 182. P.A. Frigeri, D.F. Agterberg, A. Koga, and M. Sigrist, *Phys. Rev. Lett.* **92**, 097001 (2004) [*Errata*; **93**, 099903 (2004)].
- 183. K.V. Samokhin, E.S. Zijlstra, and S.K. Bose, *Phys. Rev.* B69, 094514 (2004).
- 184. V.P. Mineev and K.V. Samokhin, *Phys. Rev.* B72, 212504 (2005).
- 185. P.A. Frigeri, D.F. Agterberg, and M. Sigrist, *New J. Phys.* 6, 115 (2004).
- 186. S. Fujimoto, J. Phys. Soc. Jpn. 76, 051008 (2007).
- 187. D.D. Koelling and B.N. Harmon, J. Phys. C: Solid State Phys. 10, 3107 (1977).
- 188. M. Nishiyama, Y. Inada, and G.-Q. Zheng, *Phys. Rev. Lett.* 98, (2007) 047002.
- 189. Y. Muro, D.H. Eom, N. Takeda, and M. Ishikawa, J. Phys. Soc. Jpn. 67, 3601 (1998).
- 190. A. Thamizhavel, T. Takeuchi, T.D. Matsuda, Y. Haga, K. Sugiyama, R. Settai, and Y. Ōnuki, J. Phys. Soc. Jpn. 74, 1858 (2005).
- 191. R. Settai, Y. Miyauchi, T. Takeuchi, I. Sheikin, F. Lévy, and Y. Ōnuki, J. Phys. Soc. Jpn. 77, 073705 (2008).
- 192. N. Tateiwa, Y. Haga, T.D. Matsuda, S. Ikeda, E. Yamamoto, Y. Okuda, Y. Miyauchi, R. Settai, and Y. Ōnuki, *J. Phys. Soc. Jpn.* 76, 083706 (2007).
- 193. H. Mukuda, T. Fujii, T. Ohara, A. Harada, M. Yashima, Y. Kitaoka, Y. Okuda, R. Settai, and Y. Ōnuki, *Phys. Rev. Lett.* 100, 107003 (2008).
- 194. Y. Inada and Y. Ōnuki, Fiz. Nizk. Temp. 25, 775 (1999) [Low Temp. Phys. 25, 573 (1999)].
- 195. M. Hedo, Y. Inada, K. Sakurai, E. Yamamoto, Y. Haga, Y. Ōnuki, S. Takahashi, M. Higuchi, T. Maehira, and A. Hasegawa, *Philos. Mag.* B77, 975 (1998).
- 196. H. Ohkuni, Y. Inada, Y. Tokiwa, K. Sakurai, R. Settai, T. Honma, Y. Haga, E. Yamamoto, Y. Ōnuki, H. Yamagami, S. Takahashi, and T. Yanagisawa, *Philos. Mag.* B79, 1045 (1999).

- 197. Y. Inada, H. Yamagami, Y. Haga, K. Sakurai, Y. Tokiwa, T. Honma, E. Yamamoto, Y. Ōnuki, and T. Yanagisawa, J. Phys. Soc. Jpn. 68, 3643 (1999).
- 198. Y. Ōnuki, I. Umehara, T. Ebihara, A.K. Albessard, K. Satoh, K. Takita, H. Aoki, S. Uji, and T. Shimizu, *Physica* B186– 188, 1050 (1993).
- 199. R. Corcoran, N. Harrison, S.M. Hayden, P. Meeson, M. Springford, and P.J. van der Wel, *Phys. Rev. Lett.* **72**, 701 (1994).
- 200. H. Harrison, S.M. Hayden, P. Meeson, M. Springford, P.J. van der Wel, and A.A. Menovsky, *Phys. Rev.* B50, 4208 (1994).
- 201. T. Terashima, H. Takeya, S. Uji, K. Kadowaki, and H. Aoki, *Solid State Commun.* **96**, 459 (1995).
- 202. G. Goll, M. Heinecke, A.G.M. Jansen, W. Joss, L. Nguyen,E. Steep, K. Winzer, and P. Wyder, *Phys. Rev.* B53, 8871 (1996).