## EPR studies of the triangular-lattice antiferromagnet Cs<sub>2</sub>CuBr<sub>4</sub>

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The spin dynamics of the spin-1/2 triangular-lattice antiferromagnet Cs<sub>2</sub>CuBr<sub>4</sub> is probed by means of high-frequency electron paramagnetic resonance (EPR) spectroscopy. Temperature dependences of EPR parameters are studied in a broad temperature range between 1.4 and 200 K for different orientations of the applied magnetic field. In the high-temperature regime ( $T >> J/k_B$ ), an unusually broad and anisotropic resonance line is detected, suggesting a sizeable Dzyaloshinskii–Moriya interaction. Employing the theory of exchange narrowing, the ratio of the Dzyaloshinskii–Moriya vector components,  $D_c/D_a \approx 0.3$ , is estimated.

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A spin-1/2 Heisenberg antiferromagnet (AF) on a triangular lattice is one of the best model systems to probe effects of quantum fluctuation and frustrations in strongly correlated spin systems, exhibiting unusual ground-state properties and a rich excitation spectrum. It was suggested, that quantum fluctuations can be strong enough to destroy the classical 120° order in triangular-lattice spin-1/2 Heisenberg AFs [1], resulting in a two-dimensional (2D) spin liquid with the excitation spectrum formed by fractionalized quasiparticles, spinons. Although the existence of such a 2D spin liquid has been predicted more than four decades ago, theoretical identification and experimental detection of this state of matter has proved challenging.

In general, the Hamiltonian of a spin-1/2 systems with a triangular lattice in zero field is given by

$$\mathcal{H} = J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + J' \sum_{\langle i,j' \rangle} \mathbf{S}_i \cdot \mathbf{S}_{j'} + \mathcal{H}_{\delta}, \tag{1}$$

where  $\mathbf{S}_i$ ,  $\mathbf{S}_j$ , and  $\mathbf{S}_{j'}$  are spin-1/2 operators at sites *i*, *j*, and *j'*, respectively, *J* and *J'* are the exchange-coupling parameters along the horizontal and zigzag bonds [Fig. 1(a)], respectively, and  $\mathcal{H}_{\delta}$  represents various possible small anisotropic contributions. Depending on the *J'/J* ratio, theory [2–7] predicts a rich variety of magnetic struc-

tures, ranging from the 1D collinear phase to an incommensurate triangular order.

The spin-1/2 triangular-lattice AFs  $Cs_2CuCl_4$  and  $Cs_2CuBr_4$  are among the most intensively studied representatives of this class of low-D frustrated materials. These two materials have many common properties. Both have a slightly distorted layered arrangement of Cu<sup>2+</sup> ions in a triangular pattern [Fig. 1(b)]. The materials are character-



*Fig. 1.* (Color online) Schematic picture of exchange paths in  $Cs_2CuBr_4$  in the *bc* plane (a). Schematic view of the crystal structure of  $Cs_2CuBr_4$  in the *bc* plane. The  $Cu^{2+}$  ions form the triangular lattice. Red circles represent copper ions, while green and blue circles represent cesium and bromine ions, respectively (b).

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ized by the same scale of in-plane spin interactions,  $J/k_B = 4.7$  K,  $J'/J \simeq 0.3$  and  $J/k_B = 14.9$  K,  $J'/J \simeq 0.41$ for  $Cs_2CuCl_4$  and  $Cs_2CuBr_4$ , respectively [8,9]. Due to finite interplane interactions, Cs<sub>2</sub>CuCl<sub>4</sub> and Cs<sub>2</sub>CuBr<sub>4</sub> undergo transitions into magnetically ordered incommensurate states, at  $T_N = 0.62$  and 1.4 K, respectively [10,11]. In spite of these (and many other) similarities, the magnetic properties of Cs<sub>2</sub>CuBr<sub>4</sub> appear much richer, including 1/3 and 2/3 saturation magnetization plateaus [12] and a number of additional (still unidentified) field-induced phase transitions [13]. Most importantly, the observation of a relatively large zero-field energy gap,  $\Delta \sim 0.7 J$ , in the excitation spectrum of Cs<sub>2</sub>CuBr<sub>4</sub> [9,14] appears to be inconsistent with the 1D scenario, proposed for Cs<sub>2</sub>CuCl<sub>4</sub> [15,16]. One of the critical issues is to clarify the reason for such a big difference of the magnetic properties of these two frustrated materials.

Electron paramagnetic resonance (EPR, also known as electron spin resonance, ESR) spectroscopy is recognized as a very powerful tool to probe the anisotropy of magnetic interactions in strongly correlated spin systems. Recently performed EPR studies of Cs<sub>2</sub>CuCl<sub>4</sub> [17] provided the important information on the magnetic anisotropy in this material. It was shown that the main source of the high-temperature EPR line broadening is the Dzyaloshinskii–Moriya (DM) interaction. Employing a high-temperature approximation, the vector components of the DM interaction,  $D_a = 0.33$  K and  $D_c = 0.36$  K, were determined from the EPR angular dependence in the *ac* plane.

Cs<sub>2</sub>CuBr<sub>4</sub> realizes a distorted triangular lattice with orthorhombic crystal structure (space group Pnma) and the room-temperature lattice parameters a = 10.195 Å, b = 7.965 Å, c = 12.936 Å, and Z = 4 (the number of formula units per unit cell) [18]. High-quality single crystals of Cs<sub>2</sub>CuBr<sub>4</sub> were grown by slow evaporation of aqueous solutions of CsBr and CuBr<sub>2</sub> similar as described in [18]. Due to a relatively broad line, no resonance absorption was detected using the standard X-band EPR spectrometer. The EPR measurements were performed employing a high-frequency transmission-type spectrometer equipped with a 16 T superconducting magnet, similar to that described in Ref. 19. A VDI modular transmitter (product of Virginia Diodes Inc., USA) was used as a mm-wave radiation source. The EPR measurements were performed at temperatures down to 1.4 K.

The temperature dependences of the EPR linewidth and effective g factors measured at a frequency of 312 GHz for three field orientations are shown in Figs. 2 and 3, respectively. One can see that the linewidth and g factor do not show any significant temperature dependence down to approximately 40–50 K. Below this temperature, the EPR field shifts and line broadening is observed. Such a behavior is an indication of the combined effect of exchange and anisotropic spin-spin interactions. At approximately 14 K, the EPR line splits (the splitting was



*Fig. 2.* (Color online) Temperature dependence of the EPR linewidths measured at 312 GHz. The data for  $H \parallel a, b$  and c are labeled by squares, circles, and triangles, respectively. The lines are guides for the eye.

observed for  $H \parallel a$ , c; some selected spectra for  $H \parallel a$  are shown in Fig. 4), eventually opening a gap,  $\Delta \approx 9.5$  K, in the excitation spectrum [9,14]. From comparison to results of harmonic spin-wave theory calculations for the spin-1/2 triangular AF model (with parameters as defined in Ref. 9) the observed gapped mode was identified as a magnetic excitation at the Brillouin zone boundary, which is observable in Cs<sub>2</sub>CuBr<sub>4</sub> due to the staggered DM interaction [14].

Above approximately 50 K, the system is in the hightemperature regime ( $T >> J/k_B$ ). Remarkably, the EPR linewidth is almost constant at least up to 200 K, suggesting that the phonon-assisted spin-lattice broadening (which should be proportional to the temperature) is not relevant.



*Fig. 3.* (Color online) Temperature dependence of the effective *g* factor measured at 312 GHz. The data for  $H \parallel a, b$  and *c* are labeled by squares, circles, and triangles, respectively. Note that data for  $H \parallel a, c$  are shown only down to 14 K (below this temperature the EPR lines split). The lines are guides for the eye.



*Fig. 4.* (Color online) Selected EPR spectra measured at 312 GHz at different temperatures,  $H \parallel a$ . Resonance absorption maxima are denoted by arrows.

Three spectra obtained at a frequency of 285 GHz for different field orientations (T = 135 K) are shown in Fig. 5. The spectra were fit using the Lorentzian line shape, revealing  $g_a = 2.17(2)$ ,  $g_b = 2.10(2)$ ,  $g_c = 2.22(2)$  and EPR full widths at half maximum (FWHM)  $\Delta H_a = 1.75(1)$  T,  $\Delta H_b = 0.60(1)$  T,  $\Delta H_c = 1.00(3)$  T for  $H \parallel a$ , b, and c, respectively. It is important to mention, that contrary to many other spin-1/2 exchange-coupled spin systems with spin interactions of the same order of magnitude [20–23], the high-temperature EPR line in Cs<sub>2</sub>CuBr<sub>4</sub> is up to two orders of magnitude broader (for comparison, the EPR linewidth in the isostructural compound Cs<sub>2</sub>CuCl<sub>4</sub> measured at T = 100 K is ~0.02–0.03 T [17], which is about 50 times smaller than the EPR linewidth in Cs<sub>2</sub>CuBr<sub>4</sub>). Let us discuss possible contributions, which affect the EPR linewidth.

(i) Following the conventional estimates [24] and assuming that the distance between neighboring  $Cu^{2+}$  ions is ~8 Å, the contribution to the dipole-dipole interaction appears to be negligibly small (~1 Oe).

(ii) The anisotropic Zeeman contribution can be calculated using the equation [25]

$$\Delta H_{AZ} = \left(\frac{\Delta g}{g}\right)^2 \frac{g\mu_B H_{\rm res}^2}{\sqrt{\langle J^2 \rangle}},\tag{2}$$

where  $\Delta g = g_c - g_b$ ,  $g = g_{a,c}$ , and  $\langle J^2 \rangle = \frac{1}{3} (J^2 + 2J'^2)$  or  $\langle J \rangle \approx 10$  K. As result, one obtains  $\Delta H_{AZ} \approx 0.04$  T, which is much smaller than the measured EPR linewidth.

(iii) Rough estimates of two remaining major contributions to the EPR linewidth, the antisymmetric DM interaction and symmetric anisotropic interaction, give  $D \propto (\Delta g/g) \langle J \rangle = 1.65$  K and  $E \propto (\Delta g/g)^2 \langle J \rangle = 0.2$  K, respectively [26]. Based on that, the DM interaction can be regarded as the main reason of the broad anisotropic EPR line observed in our experiments.



*Fig. 5.* (Color online) EPR spectra measured at 285 GHz, T = 135 K, with magnetic field applied along the three different crystallographic axes. The dashed lines are Lorentzian fit results.

Figure 6 shows the angular dependence of the EPR linewidth with magnetic field applied in the *ac* plane, obtained at 312 GHz and T = 80 K.

If the EPR line is of Lorentzian shape, the FWHM  $\Delta H$  can be calculated employing the theory of exchange narrowing [27] as

$$\Delta H = 2C \left(\frac{M_2^3}{M_4}\right)^{1/2},\tag{3}$$

where  $M_2$  and  $M_4$  are the second and fourth moment, *C* is a dimensionless constant,  $C = \pi / \sqrt{2}$  [17]. Following the approach from Ref. 17, 27, the FWHM can be written as

$$\Delta H = C \frac{D^2(\alpha, \beta)k_B}{\langle J \rangle g \mu_B} \frac{1}{\sqrt{2}}.$$
 (4)



*Fig. 6.* (Color online) Angular dependence of the EPR linewidth with magnetic field applied in the *ac* plane, obtained at 312 GHz, T = 80 K. 0° corresponds to  $H \parallel a$ , while  $\pm 90^{\circ}$  correspond to  $H \parallel c$ . The line is a guide for the eye.

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Here,  $k_B$  is the Boltzmann constant,  $\mu_B$  is the Bohr magneton, and

$$\mathcal{D}^{2}(\alpha,\beta) = D_{a}^{2} \left(1 + \sin^{2}\beta\cos^{2}\alpha\right) + D_{c}^{2} \left(1 + \cos^{2}\beta\right) + D_{a}D_{c}\cos\alpha\sin2\beta,$$
(5)

where  $D_a$  and  $D_c$  are the DM vector components along the *a* and *c* axes, respectively. The angles  $\alpha$  and  $\beta$  are defined by

$$\cos \alpha = \frac{A}{\sqrt{A^2 + B^2}}, \qquad \cos \beta = \frac{C}{\sqrt{A^2 + B^2 + C^2}},$$

$$A = g_{aa} \sin \theta \cos \varphi + g_{ab} \sin \theta \sin \varphi + g_{ac} \cos \theta,$$

$$B = g_{ca} \sin \theta \cos \varphi + g_{cb} \sin \theta \sin \varphi + g_{cc} \cos \theta,$$

$$C = g_{ba} \sin \theta \cos \varphi + g_{bb} \sin \theta \sin \varphi + g_{bc} \cos \theta,$$
(6)

Here,  $\varphi$  denotes the azimuthal angle counted from the *a* axis and  $\theta$  denotes the polar angle counted from the *c* axis.

Taking into account that the magnetic field is applied in the *ac* plane (the DM interaction is not allowed along the *b* axis), we can neglect contributions to the moments for  $\varphi \neq 0$ . Our analysis provides  $D_a = (4.7 \pm 0.5)$  K and  $D_c = (1.6 \pm 0.3)$  K for the DM components along the *a* and *c* axes, respectively. These numbers appear to be too big, compared to  $\langle J \rangle = 10$  K, questioning the validity of the used approach for compounds with a substantial DM interaction. Nevertheless, the approach can be employed for estimation of the  $D_c/D_a$  ratio. In our calculations, we neglect offdiagonal elements of the *g* tensor; the corresponding error due to each off-diagonal element does not exceed ~ 10%. Based on these considerations, the ratio  $D_c/D_a$  can be written as

$$\frac{\Delta H_c}{\Delta H_a} = \left(\frac{M_2^3(\varphi = 0^\circ, \theta = 0^\circ)/M_4(\varphi = 0^\circ, \theta = 0^\circ)}{M_2^3(\varphi = 0^\circ, \theta = 90^\circ)/M_4(\varphi = 0^\circ, \theta = 90^\circ)}\right)^{1/2}.$$
 (7)

Using the function  $\mathcal{D}^2$  as introduced in (5) and keeping  $\phi = 0^\circ$  fixed leads to

$$\begin{pmatrix} \frac{M_2^3(\theta = 0^\circ) / M_4(\theta = 0^\circ)}{M_2^3(\theta = 90^\circ) / M_4(\theta = 90^\circ)} \end{pmatrix}^2 = \begin{pmatrix} \frac{\mathcal{D}^2(\theta = 0^\circ)}{\mathcal{D}^2(\theta = 90^\circ)} \end{pmatrix}^2 = \\ = \begin{pmatrix} \frac{2D_c^2 + D_a^2}{2D_a^2 + D_c^2} \end{pmatrix}^2,$$
(8)

we obtain  $D_c / D_a = 0.3(1)$ .

In conclusion, we performed high-frequency EPR studies of the spin-1/2 triangular-lattice antiferromagnet Cs<sub>2</sub>CuBr<sub>4</sub>. In the high-temperature regime ( $T >> J/k_B$ ), a very broad and anisotropic resonance line was detected, suggesting the presence of a sizeable DM interaction. Employing the EPR exchange narrowing theory, the ratio of the DM vector components,  $D_c/D_a \approx 0.3$ , was estimated. Our studies strongly suggest that the effect of the DM interaction is essential and needs to be taken into account, when explaining the cascade of the field-induced transitions and other unusual magnetic properties revealed in  $Cs_2CuBr_4$  at low temperatures.

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- 1. P.W. Anderson, Mater. Res. Bull. 8, 153 (1973).
- O.A. Starykh, H. Katsura, and L. Balents, *Phys. Rev. B* 82, 014421 (2010).
- S. Ghamari, C. Kallin, S.S. Lee, and E.S. Sørensen, *Phys. Rev. B* 84, 174415 (2011).
- 4. D. Heidarian, S. Sorella, and F. Becca, *Phys. Rev. B* 80, 012404 (2009).
- M.Q. Weng, D.N. Sheng, Z.Y. Weng, and R.J. Bursill, *Phys. Rev. B* 74, 012407 (2006).
- A. Weichselbaum and S.R. White, *Phys. Rev. B* 84, 245130 (2011).
- 7. J. Reuther and R. Thomale, Phys. Rev. B 83, 024402 (2011).
- R. Coldea, D.A. Tennant, K. Habicht, P. Smeibidl, C. Wolters, and Z. Tylczynski, *Phys. Rev. Lett.* 88, 137203 (2002).
- S.A. Zvyagin, D. Kamenskyi, M. Ozerov, J. Wosnitza, M. Ikeda, T. Fujita, M. Hagiwara, A.I. Smirnov, T.A. Soldatov, A.Y. Shapiro, J. Krzystek, R. Hu, H. Ryu, C. Petrovic, and M.E. Zhitomirsky, *Phys. Rev. Lett.* **112**, 077206 (2014).
- R. Coldea, D.A. Tennant, R.A. Cowley, D.F. McMorrow, B. Dorner, and Z. Tylczynski, *J. Phys. Condens. Matter* 8, 7473 (1996).
- T. Ono, H. Tanaka, H. Aruga Katori, F. Ishikawa, H. Mitamura, and T. Goto, *Phys. Rev. B* 67, 104431 (2003).
- T. Ono, H. Tanaka, O. Kolomiyets, H. Mitamura, F. Ishikawa, T. Goto, K. Nakajima, A. Oosawa, Y. Koike, K. Kakurai, J. Klenke, P. Smeibidle, M. Meissner, R. Coldea, A.D. Tennant, and J. Ollivier, *Theor. Phys. Suppl.* **159**, 217 (2005).
- N.A. Fortune, S.T. Hannahs, J. Yoshida, T.E. Sherline, T. Ono, H. Tanaka, and Y. Takano, *Phys. Rev. Lett.* **102**, 257201 (2009).
- S.A. Zvyagin, M. Ozerov, D. Kamenskyi, J. Wosnitza, B.J. Krzystek, D. Yoshizawa, M. Hagiwara, R. Hu, H. Ryu, C. Petrovic, and M.E. Zhitomirsky, *New J. Phys.* 17, 113059 (2015).
- M. Kohno, O.A. Starykh, and L. Balents, *Nat. Phys.* 3, 790 (2007).
- 16. K.Yu. Povarov, A.I. Smirnov, O.A. Starykh, S.V. Petrov, and A.Ya. Shipiro, *Phys. Rev. Lett.* **107**, 037204 (2011).
- M.A. Fayzullin, R.M. Eremin, A. Dittl, N. van Well, F. Ritter, W. Aßmus, J. Deisenhofer, H.-A. Krug von Nidda, and A. Loidl, *Phys. Rev. B* 88, 174421 (2013).

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- B. Morosin and E.C. Lingafelter, Acta Crystallogr. 13, 807 (1960).
- S.A. Zvyagin, J. Krzystek, P.H.M. van Loosdrecht, G. Dhalenne, and A. Revcolevschi, *Physica B* 346–347, 1 (2004).
- 20. B. Pilawa, J. Phys.: Condens. Matter 9, 3779 (1997).
- H.-A. Krug von Nidda, L.E. Svistov, M.V. Eremin, R.M. Eremina, A. Loidl, V. Kataev, A. Validov, A. Prokofiev, and W. Aßmus, *Phys. Rev. B* 65, 134445 (2002).
- A.A. Validov, M. Ozerov, J. Wosnitza, S.A. Zvyagin, M.M. Turnbull, C.P. Landee, and G.B. Teitel'baum, *J. Phys.: Condens. Matter* 26, 026003 (2014).
- V.N. Glazkov, M. Fayzullin, Yu. Krasnikova, G. Skoblin, D. Schmidiger, S. Mühlbauer, and A. Zheludev, *Phys. Rev. B* 92, 184403 (2015).
- I. Yamada, M. Nishi, and J. Akimutsu, J. Phys.: Condens. Matter 8, 2625 (1996).
- D.L. Huber, G. Alejandro, A. Caneiro, M.T. Causa, F. Prado, M. Tovar, and S.B. Oseroff, *Phys. Rev. B* 60, 12155 (1999).
- 26. T. Moriya, Phys. Rev. B 120, 92 (1960).
- 27. T.G. Castner, Jr. and M.S. Seehra, Phys. Rev. B 4, 38 (1971).