

## ABSTRACT DATA TYPES IN PROBABILISTIC PROGRAMMING LANGUAGES

**Annotation.** Today, there are quite a few different probabilistic programming languages that to some extent use the concepts of probability theory for their calculations. But we wanted to know what data types exist for solving probabilistic tasks. In the present paper we present a system analysis of abstract data types in selected languages of probabilistic programming.

**Keywords:** Probabilistic programming, Abstract data types, Probabilistic programming languages, Programming languages.

### Formulation of problem

Probabilistic programming languages, in their simple form, extend the well-known deterministic programming language with primitive constructions for random choice [17]. However, over time, there was a creation of new tools for probabilistic inference and the emergence of new complex probabilistic simulation programs. The presence of a large number of probabilistic programming languages led to the idea that there is a certain programming paradigm, the so-called probabilistic programming.

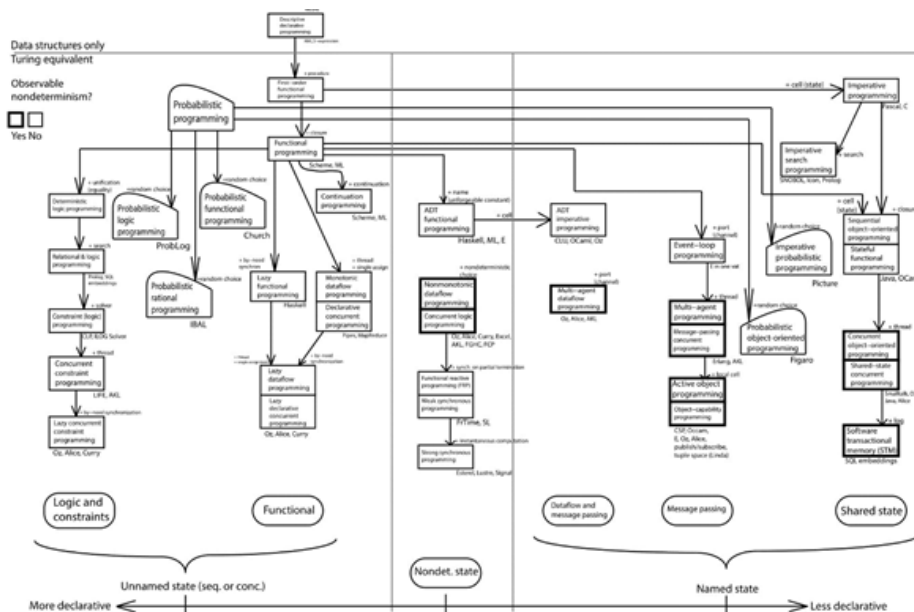


Figure 1 - Classification of programming paradigms [17]

Basic principles language design and probabilistic programming were given in [8]. Also in this article describes the differences between Probabilistic Programming and Probabilistic Model Checking.

### **Literature review**

About each of probabilistic programming languages there are relevant article or the corresponding page on the Internet from their authors. Therefore we will list those languages about which we will speak. Namely: Church (MIT BCS/CSAIL) [5, 13], Anglican (MIT, Oxford University and DARPA PPAML) [2-4, 15], Venture (MIT BCS/CSAIL) [9, 11, 18], Infer.Net (Microsoft Research) [12], TensorFlow [6, 13] (Google) with libraries TensorFlow Distributions (Google, Columbia University) [1] and Edward (Columbia University) [7, 8, 16].

### **The purpose and objectives of Article**

In each of the languages of probabilistic programming with the help of abstract types, the basic concepts of probability theory are realized: probability space set, random variable, probability, probability distribution. These concepts, in our opinion, must necessarily be implemented in languages of probabilistic programming.

In this article, we will analyze the implementation of the basic concepts of probability theory with abstract data types in probabilistic programming languages. Namely: Church, Anglican, Venture, Infer.Net, TensorFlow with libraries TensorFlow Distributions and Edward.

### **Main part**

Church (MIT BCS/CSAIL).

Let's start our analysis with the Church. Church - a universal language for describing stochastic generative processes. Church is based on the Lisp model of lambda calculus, containing a pure Lisp as its deterministic subset.

We will provide the partial description of language with [5]: «Church language is based upon a pure subset of functional language Scheme, a Lisp dialect». What we can understand from the reading: Church uses the same abstract types as Scheme. Feature of Church is the fact that expressions are values and these expressions describe generative processes.

In Church there is one interesting feature – all computation returns to Church in the form of random variable [12].

To specify sets, you can use built-in commands, such as list, vector and map. Using the built-in Scheme types to represent probabilities,

Church uses the type number. And it can be like integer or, if it is necessary to calculate probability, rational.

For calculation of probability a distribution function is used. It returns value from evaluating the body given env and values of formal parameters.

Anglican (MIT, Oxford University and DARPA PPAML).

Because Anglican is like the Clojure programming language, it uses the same data types. Here are just Clojure data types are Java data types, which also means that all values in Clojure are regular Java reference objects.

For representation of sets, Anglican, as well as Church, uses the list, vector or hashmap types. Sample method returns a random sample and roughly corresponds to the default implementation of the sample checkpoint.

For storage and work with probability, Anglican uses library `java.lang.BigDecimal` – decimal values or other classes, because Java primitives are usually boxed in Clojure functions. The observe method returns the log probability of the value, which roughly corresponds to the default implementation of the observe checkpoint.

To determine the distribution used macro `defdist`. It takes care of defining a separate type for every distribution so that Clojure multimethods (or overloaded methods) can be dispatched on distribution types when needed.

Venture (MIT BCS/CSAIL).

Venture is essentially a Lisp-like higher-order language augmented with two novel abstractions:

Probabilistic execution traces (PETs or abbreviated as “traces”) are a first-class object that represents the sequence of random choices that a probabilistic program makes. Each program subcomputation that yields a result corresponds to a random variable. PETs serve as the only native form of mutable storage in Venture, and map dynamic “addresses” assigned over the course of program execution to the manifest values taken by the program at those addresses;

Stochastic procedures (SPs). SPs are used to encapsulate simple probability distributions, as well as user-space VentureScript programs and foreign probabilistic objects. An SP consists of a linked collection of programs and meta-programs that collectively describe aspects of a

probabilistic program that are important for its use in modeling and inference. SPs are designed to allow simple probability distributions, user-space VentureScript, and foreign probabilistic programs to be treated uniformly as building blocks of complex probabilistic computations;

The authors state that Venture uses the usual scalar and symbolic data types from the programming language Scheme. Also in Venture there is support for collections and additional datatypes corresponding to a primitive object from the probability theory and statistics. There is support for the stochastic procedure datatype for using compound procedures returned by lambda.

Here is a list of the most important values:

- Atoms – discrete items with no internal structure or ordering;
- Numbers – data types like as integer, rational, real, and complex;
- Collections – vectors, which map numbers to values and support  $O(1)$  random access, and maps (map values to values) with support  $O(1)$  amortized random access;

- Stochastics procedures – standard library components and can also be created by Lambda and others stochastic procedures.

Infer.NET (Microsoft Research).

Infer.NET framework for running Bayesian inference in graphical models. Infer.NET provides the state-of-the-art message-passing algorithms and statistical routines needed to perform inference for a wide variety of applications.

In Infer.NET it is possible to create three types of variables: random (values are unknown and whose posterior distributions can be calculated during inference), constant (fixed values), observed (values not specified when the model is constructed, but are given before performing inference).

Infer.NET is used to create variables other than simple data types, such as bool, double, int, enum, string, char. Vector and PositiveDefiniteMatrix are used as vector and matrix types for creation of probabilistic sets. In addition, all of them and also TDomain [], ISparseList <>, IList <> can be used for discrete, continuous, multivariate and sequence distributions.

For greater convenience and possible simplicity, the developers provided methods for creating random variables with various distribution factors. It can pass in random variables as arguments e.g. Variable <bool>

instead of int. In [11] you can see examples of such usage, as well as with the description and syntax on Infer.NET. Built-in functionality allows you to use different types of data parameters. For example, with discrete distribution.

TensorFlow (Google), library TensorFlow Distributions (Google, Columbia University) and Edward (Columbia University).

TensorFlow is based on use of so-called tensors. We will give small definition about tensors. Tensors are simply mathematical objects that can be used to describe physical properties, just like scalars and vectors. In fact tensors are merely a generalization of scalars and vectors; a scalar is a zero rank tensor, and a vector is a first rank tensor [18].

The rank (or order) of a tensor is defined by the number of directions (and hence the dimensionality of the array) required to describe it. For example, properties that require one direction (first rank) can be fully described by a 3Ч1 column vector, and properties that require two directions (second rank tensors), can be described by 9 numbers, as a 3Ч3 matrix. As such, in general an nth rank tensor can be described by 3n coefficients.

Tensors are used to represent the data structure in programs written in TensorFlow. Using tensors, TensorFlow represents the probability space is an N-dimensional array or list. The tensor has a static type and a dynamic dimension.

TensorFlow provides several possibilities for creating so-called random tensors with different distributions. In this case, after each call and calculation, new random values are created.

Tensors can be of such data types: bool, half, float, float64, uint8, int8, int16, int32, int64, complex64, complex128, string. But you can also use standard data types with Python. For example, as bool, str, list or tuple.

More recently, for TensorFlow, another library of adaptation of the vision of probability theory to the modern deep-learning paradigm of end-to-end differentiable computation. It is called TensorFlow Distributions [1]. It is constructed on such two abstractions: Distributions and Bijectors. The first provides a collection of approximately 60 distributions with fast, numerically stable methods for sampling, log density, and many statistics. The second one allows composable volumetracking transformations with automatic caching. Together these enable modular

construction of high dimensional distributions and transformations not possible with previous libraries.

Also, this year was presented Edward [15] – deep probabilistic programming library, which expands deep-learning research by enabling new forms of experimentation, faster iteration cycles, and improved reproducibility. Edward provides a language of random variables to construct a broad class of models: directed graphical models, stochastic neural networks, and programs with stochastic control flow. In Edward, random variable is an object parameterized by tensors. For Edward, the TensorFlow Distributions library has a backend.

### **Conclusion and future research directions**

We will write short outputs about each of the probable languages selected by us. We will select several highlights. The first is that all the languages we choose use the data types of their "parent" programming languages. The second is that for the use of distributions and random variables, the built-in functions or methods in each of the languages are used. And the list of these distributions can be different. Depending on various factors (development experience, knowledge in the field of probability theory, etc.), the development of own probabilistic concepts can cause confusion.

### **LITERATURE**

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